

thm_2Erelation_2ESC_IDEM (TMT4ufT7nhj15EqY8Ek17aSt97Hit3vNAuV)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Ebool_2E_2T$ to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap (ap (c_2Emin_2E_3D (2^{A_27a}))$

Definition 4 We define $c_2Ebool_2E_2F$ to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_27E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E_2F))$

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t)))$

Definition 8 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t)))$

Definition 9 We define $c_2Erelation_2ESC$ to be $\lambda A_27a : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1x \in A_27a.\lambda V2y \in A_27a.$

Definition 10 We define $c_2Erelation_2Esymmetric$ to be $\lambda A_27a : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).(ap (c_2Ebool_2E_27E$

Assume the following.

$$True \tag{1}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A_27a.(p V0t)) \Leftrightarrow (p V0t))) \tag{2}$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \tag{3}$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \Leftrightarrow True) \Leftrightarrow (p \ V0t)) \wedge (((False \Leftrightarrow (p \ V0t)) \Leftrightarrow \neg(p \ V0t)) \wedge (((p \ V0t) \Leftrightarrow False) \Leftrightarrow \neg(p \ V0t)))))) \quad (4)$$

Assume the following.

$$\forall A_{27a}.nonempty \ A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). (p \ (ap \ (c_2Erelation_2Esymmetric \ A_{27a}) \ (ap \ (c_2Erelation_2ESC \ A_{27a}) \ V0R)))) \quad (5)$$

Assume the following.

$$\forall A_{27a}.nonempty \ A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). ((p \ (ap \ (c_2Erelation_2Esymmetric \ A_{27a}) \ V0R)) \Rightarrow ((ap \ (c_2Erelation_2ESC \ A_{27a}) \ V0R) = V0R))) \quad (6)$$

Theorem 1

$$\forall A_{27a}.nonempty \ A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). ((ap \ (c_2Erelation_2ESC \ A_{27a}) \ (ap \ (c_2Erelation_2ESC \ A_{27a}) \ V0R)) = (ap \ (c_2Erelation_2ESC \ A_{27a}) \ V0R)))$$