

thm_2Erelation_2ESC_MONOTONE (TMJB- vAdxPCJkYAjPW7eqVea2ws6oQkxXTcT)

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Definition 1 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \Rightarrow p \Rightarrow Q)$ of type ι .

Definition 2 We define `c_2Emin_2E_3D` to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define `c_2Ebool_2ET` to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 4 We define `c_2Ebool_2E_21` to be $\lambda A.27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c_2Emin_2E_3D (2^{A-27a}))$

Definition 5 We define `c_2Ebool_2EF` to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 6 We define `c_2Ebool_2E_7E` to be $(\lambda V0t \in 2.(ap (ap (c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF$

Definition 7 We define `c_2Ebool_2E_2F_5C` to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2$

Definition 8 We define `c_2Ebool_2E_5C_2F` to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2$

Definition 9 We define `c_2Erelation_2ESC` to be $\lambda A.27a : \iota.\lambda V0R \in ((2^{A-27a})^{A-27a}).\lambda V1x \in A.27a.\lambda V2y \in$

Assume the following.

$$True \tag{1}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \vee (p \vee V0t)) \Leftrightarrow True) \wedge (((p \vee V0t) \vee True) \Leftrightarrow True) \wedge \\ & (((False \vee (p \vee V0t)) \Leftrightarrow (p \vee V0t)) \wedge (((p \vee V0t) \vee False) \Leftrightarrow (p \vee V0t)) \wedge (((p \vee V0t) \vee \\ & (p \vee V0t)) \Leftrightarrow (p \vee V0t)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p \vee V0t)) \Leftrightarrow (p \vee V0t)) \wedge (((p \vee V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p \vee V0t)) \wedge (((False \Leftrightarrow (p \vee V0t)) \Leftrightarrow \neg(p \vee V0t)) \wedge (((p \vee V0t) \Leftrightarrow False) \Leftrightarrow \neg(\\ & p \vee V0t)))))) \end{aligned} \tag{3}$$

Theorem 1

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0R \in ((2^{A_27a})^{A_27a}). \\ & (\forall V1Q \in ((2^{A_27a})^{A_27a}). (\forall V2x \in A_27a. (\forall V3y \in \\ & A_27a. ((\forall V4x \in A_27a. (\forall V5y \in A_27a. ((p\ (ap\ (ap\ V0R \\ V4x)\ V5y)) \Rightarrow (p\ (ap\ (ap\ V1Q\ V4x)\ V5y)))))) \Rightarrow ((p\ (ap\ (ap\ (ap\ (c_2Erelation_2ESC \\ A_27a)\ V0R)\ V2x)\ V3y)) \Rightarrow (p\ (ap\ (ap\ (ap\ (c_2Erelation_2ESC\ A_27a) \\ V1Q)\ V2x)\ V3y)))))))))) \end{aligned}$$