

# thm\_2Erelation\_2Etransitive\_\_RTC (TMM- PRf9DShyWnmwwAgkKkwu41TyCKEk2dPF)

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**Definition 1** We define `c_2Emin_2E_3D_3D_3E` to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 2** We define `c_2Emin_2E_3D` to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define `c_2Ebool_2E_2T` to be  $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

**Definition 4** We define `c_2Ebool_2E_21` to be  $\lambda A_{27a} : \iota.(\lambda V0P \in (2^{A_{27a}}).(ap (ap (c_2Emin_2E_3D (2^{A_{27a}}))$

**Definition 5** We define `c_2Ebool_2E_2F_5C` to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in 2.V2t)))$

**Definition 6** We define `c_2Erelation_2ERTC` to be  $\lambda A_{27a} : \iota.\lambda V0R \in ((2^{A_{27a}})^{A_{27a}}).\lambda V1a \in A_{27a}.\lambda V2b \in A_{27a}.$

**Definition 7** We define `c_2Erelation_2Etransitive` to be  $\lambda A_{27a} : \iota.\lambda V0R \in ((2^{A_{27a}})^{A_{27a}}).(ap (c_2Ebool_2E_2F_5C$

Assume the following.

$$\begin{aligned} & \forall A_{27a}.nonempty A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). \\ & (p (ap (c_2Erelation_2Etransitive A_{27a}) (ap (c_2Erelation_2ERTC \\ & \quad A_{27a}) V0R)))) \end{aligned} \quad (1)$$

**Theorem 1**

$$\begin{aligned} & \forall A_{27a}.nonempty A_{27a} \Rightarrow (\forall V0R \in ((2^{A_{27a}})^{A_{27a}}). \\ & (p (ap (c_2Erelation_2Etransitive A_{27a}) (ap (c_2Erelation_2ERTC \\ & \quad A_{27a}) V0R)))) \end{aligned}$$