

thm_Erich_list_EDROP_FUNPOW_TL
(TMQQxFzm9B5dcp3XGnYAoara6D2sZzhVc8u)

October 26, 2020

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $c_2Earithmetic_2EFUNPOW : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Earithmetic_2EFUNPOW\ A_27a \in ((A_27a^{A_27a})^{ty_2Enum_2Enum})^{(A_27a^{A_27a})} \tag{2}$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define $c_2Ebool_2E_2T$ to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.if\ (\exists x \in A.p\ (ap\ P\ x))\ then\ (the\ (\lambda x.x \in A \wedge p\ x))$ of type $\iota \Rightarrow \iota$.

Definition 4 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ V0P\ (ap\ (c_2Emin_2E_40\ A_27a\ P))))$

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o\ (p\ P \Rightarrow p\ Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ (ap\ (c_2Emin_2E_3D\ (2^{A_27a}\ P))))$

Definition 7 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in 2.V2t))))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in omega \tag{3}$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{omega}) \tag{4}$$

Definition 8 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 9 We define $c_Earithmetic_EZERO$ to be c_Enum_E0 .

Let $c_Enum_EREP_num : \iota$ be given. Assume the following.

$$c_Enum_EREP_num \in (\omega^{ty_Enum_Enum}) \quad (5)$$

Let $c_Enum_ESUC_REP : \iota$ be given. Assume the following.

$$c_Enum_ESUC_REP \in (\omega^{\omega}) \quad (6)$$

Definition 10 We define c_Enum_ESUC to be $\lambda V0m \in ty_Enum_Enum.(ap\ c_Enum_EABS_num$

Let $c_Earithmetic_E_2B : \iota$ be given. Assume the following.

$$c_Earithmetic_E_2B \in ((ty_Enum_Enum)^{ty_Enum_Enum})^{ty_Enum_Enum} \quad (7)$$

Definition 11 We define $c_Earithmetic_EBIT1$ to be $\lambda V0n \in ty_Enum_Enum.(ap\ (ap\ c_Earithmetic$

Definition 12 We define $c_Earithmetic_ENUMERAL$ to be $\lambda V0x \in ty_Enum_Enum.V0x$.

Let $c_Earithmetic_E_2D : \iota$ be given. Assume the following.

$$c_Earithmetic_E_2D \in ((ty_Enum_Enum)^{ty_Enum_Enum})^{ty_Enum_Enum} \quad (8)$$

Definition 13 We define c_Ebool_EF to be $(ap\ (c_Ebool_E_21\ 2))\ (\lambda V0t \in 2.V0t)$.

Definition 14 We define $c_Ebool_E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_Ebool_E_21\ 2))\ (\lambda V2t \in$

Definition 15 We define c_Ebool_ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.($

Let $ty_Elist_Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_Elist_Elist\ A0) \quad (9)$$

Let $c_Elist_ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Elist_ENIL\ A_27a \in (ty_Elist_Elist\ A_27a) \quad (10)$$

Let $c_Erich_list_ETL_T : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Erich_list_ETL_T\ A_27a \in ((ty_Elist_Elist\ A_27a)^{(ty_Elist_Elist\ A_27a)}) \quad (11)$$

Let $c_Elist_ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_Elist_ECONS\ A_27a \in (((ty_Elist_Elist\ A_27a)^{(ty_Elist_Elist\ A_27a)})^{A_27a}) \quad (12)$$

Let $c_2Elist_2EDROP : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Elist_2EDROP\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum}) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow & ((\forall V0f \in (A_27a^{A_27a}).(\forall V1x \in \\ & A_27a.((ap\ (ap\ (ap\ (c_2Earithmetic_2EFUNPOW\ A_27a)\ V0f)\ c_2Enum_2E0) \\ & V1x) = V1x))) \wedge (\forall V2f \in (A_27a^{A_27a}).(\forall V3n \in ty_2Enum_2Enum. \\ & (\forall V4x \in A_27a.((ap\ (ap\ (ap\ (c_2Earithmetic_2EFUNPOW\ A_27a) \\ & V2f)\ (ap\ c_2Enum_2ESUC\ V3n))\ V4x) = (ap\ (ap\ (ap\ (c_2Earithmetic_2EFUNPOW \\ & A_27a)\ V2f)\ V3n)\ (ap\ V2f\ V4x)))))))) \end{aligned} \quad (14)$$

Assume the following.

$$True \quad (15)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A_27a.(p\ V0t)) \Leftrightarrow (p\ V0t))) \quad (16)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (17)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow & (\forall V0l \in (ty_2Elist_2Elist\ A_27a).((V0l = (c_2Elist_2ENIL\ A_27a)) \vee (\exists V1h \in A_27a. \\ & \exists V2t \in (ty_2Elist_2Elist\ A_27a).(V0l = (ap\ (ap\ (c_2Elist_2ECONS\ A_27a)\ V1h)\ V2t)))))) \end{aligned} \quad (18)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow & ((\forall V0n \in ty_2Enum_2Enum. \\ & ((ap\ (ap\ (c_2Elist_2EDROP\ A_27a)\ V0n)\ (c_2Elist_2ENIL\ A_27a)) = \\ & (c_2Elist_2ENIL\ A_27a))) \wedge (\forall V1n \in ty_2Enum_2Enum.(\forall V2x \in \\ & A_27a.(\forall V3xs \in (ty_2Elist_2Elist\ A_27a).((ap\ (ap\ (c_2Elist_2EDROP \\ & A_27a)\ V1n)\ (ap\ (ap\ (c_2Elist_2ECONS\ A_27a)\ V2x)\ V3xs)) = (ap\ (ap \\ & (ap\ (c_2Ebool_2ECOND\ (ty_2Elist_2Elist\ A_27a))\ (ap\ (ap\ (c_2Emin_2E_3D \\ & ty_2Enum_2Enum)\ V1n)\ c_2Enum_2E0))\ (ap\ (ap\ (c_2Elist_2ECONS\ A_27a) \\ & V2x)\ V3xs))\ (ap\ (ap\ (c_2Elist_2EDROP\ A_27a)\ (ap\ (ap\ c_2Earithmetic_2E_2D \\ & V1n)\ (ap\ c_2Earithmetic_2ENUMERAL\ (ap\ c_2Earithmetic_2EBIT1 \\ & c_2Earithmetic_2EZERO))))\ V3xs)))))) \end{aligned} \quad (19)$$

Assume the following.

$$\begin{aligned}
& (\forall V0P \in (2^{ty_2Enum_2Enum}).(((p (ap V0P c_2Enum_2E0)) \wedge \\
& (\forall V1n \in ty_2Enum_2Enum.((p (ap V0P V1n)) \Rightarrow (p (ap V0P (ap c_2Enum_2ESUC \\
& V1n)))))) \Rightarrow (\forall V2n \in ty_2Enum_2Enum.(p (ap V0P V2n))))))
\end{aligned} \tag{20}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow ((ap (c_2Erich_list_2ETL_T \\
& A_27a) (c_2Elist_2ENIL A_27a)) = (c_2Elist_2ENIL A_27a)) \wedge (\forall V0h \in \\
& A_27a.(\forall V1t \in (ty_2Elist_2Elist A_27a).((ap (c_2Erich_list_2ETL_T \\
& A_27a) (ap (ap (c_2Elist_2ECONS A_27a) V0h) V1t)) = V1t))))
\end{aligned} \tag{21}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow ((\forall V0l \in (ty_2Elist_2Elist \\
& A_27a).((ap (ap (c_2Elist_2EDROP A_27a) c_2Enum_2E0) V0l) = V0l)) \wedge \\
& (\forall V1n \in ty_2Enum_2Enum.(\forall V2x \in A_27a.(\forall V3l \in \\
& (ty_2Elist_2Elist A_27a).((ap (ap (c_2Elist_2EDROP A_27a) (ap \\
& c_2Enum_2ESUC V1n)) (ap (ap (c_2Elist_2ECONS A_27a) V2x) V3l)) = \\
& (ap (ap (c_2Elist_2EDROP A_27a) V1n) V3l))))))
\end{aligned} \tag{22}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.nonempty A_27a \Rightarrow (\forall V0n \in ty_2Enum_2Enum.(\\
& \forall V1l \in (ty_2Elist_2Elist A_27a).((ap (ap (c_2Elist_2EDROP \\
& A_27a) V0n) V1l) = (ap (ap (ap (c_2Earithmetic_2EFUNPOW (ty_2Elist_2Elist \\
& A_27a)) (c_2Erich_list_2ETL_T A_27a)) V0n) V1l))))
\end{aligned}$$