

thm_2Erich_list_2EEVERY_DROP
(TML8UBvCvBbWb31uLv42SVPDs7ZCzCrvun9)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \tag{1}$$

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \tag{2}$$

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow nonempty\ (ty_2Elist_2Elist\ A0) \tag{3}$$

Let $c_2Elist_2EDROP : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Elist_2EDROP\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum}) \tag{4}$$

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o\ (x = y)$ of type $\iota \Rightarrow \iota$.

Let $c_2Erich_list_2ESEG : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Erich_list_2ESEG\ A_27a \in (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \tag{5}$$

Let $c_2Elist_2ELENGTH : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Elist_2ELENGTH\ A_27a \in (ty_2Enum_2Enum)^{(ty_2Elist_2Elist\ A_27a)} \tag{6}$$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum)^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \tag{7}$$

Definition 2 We define c_2Ebool_2ET to be $(ap\ (ap\ (c_2Emin_2E_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_Ebool_2E_21$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap (ap (c_Emin_2E_3D (2^{A_27a})))$

Definition 4 We define c_Ebool_2EF to be $(ap (c_Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_Emin_2E_3D_3D_3E$ to be $\lambda P \in 2. \lambda Q \in 2. inj_o (p P \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_Ebool_2E_7E$ to be $(\lambda V0t \in 2. (ap (ap c_Emin_2E_3D_3D_3E V0t) c_Ebool_2EF$

Definition 7 We define $c_Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_Ebool_2E_21 2) (\lambda V2t \in 2$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (8)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (9)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (10)$$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum. (ap c_2Enum_2EABS_num ($

Definition 9 We define $c_Emin_2E_40$ to be $\lambda A. \lambda P \in 2^A. \mathbf{if} (\exists x \in A. p (ap P x)) \mathbf{then} (the (\lambda x. x \in A \wedge p$ of type $\iota \Rightarrow \iota$.

Definition 10 We define $c_Ebool_2E_3F$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap V0P (ap (c_Emin_2E_40$

Definition 11 We define $c_Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum$

Definition 12 We define $c_Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (ap (c_Ebool_2E_21 2) (\lambda V2t \in 2$

Definition 13 We define $c_2Earithmetic_2E_3C_3D$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum$

Let $c_2Elist_2EEVERY : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty A_27a \Rightarrow c_2Elist_2EEVERY A_27a \in ((2^{(ty_2Elist_2Elist A_27a)})^{(2^{A_27a})}) \quad (11)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (\\ & (p (ap (ap c_2Earithmetic_2E_3C_3D V1n) V0m)) \Rightarrow ((ap (ap c_2Earithmetic_2E_2B \\ & (ap (ap c_2Earithmetic_2E_2D V0m) V1n)) V1n) = V0m)))) \end{aligned} \quad (12)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (p (ap (ap c_2Earithmetic_2E_3C_3D V0m) V0m))) \quad (13)$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0n \in \text{ty_2Enum_2Enum}. (\\
& \quad \forall V1l \in (\text{ty_2Elist_2Elist } A_{27a}). ((p (ap (ap \text{c_2Earithmetic_2E_3C_3D} \\
& \quad V0n) (ap (c_2Elist_2ELENGTH } A_{27a}) V1l))) \Rightarrow ((ap (ap (c_2Elist_2EDROP \\
& \quad A_{27a}) V0n) V1l) = (ap (ap (ap (c_2Erich_list_2ESEG } A_{27a}) (ap (\\
& \quad \text{ap } c_2Earithmetic_2E_2D (ap (c_2Elist_2ELENGTH } A_{27a}) V1l)) V0n)) \\
& \quad V0n) V1l))))))
\end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0P \in (2^{A_{27a}}). (\forall V1l \in \\
& \quad (\text{ty_2Elist_2Elist } A_{27a}). ((p (ap (ap (c_2Elist_2EEVERY } A_{27a}) \\
& \quad V0P) V1l)) \Rightarrow (\forall V2m \in \text{ty_2Enum_2Enum}. (\forall V3k \in \text{ty_2Enum_2Enum}. \\
& \quad ((p (ap (ap \text{c_2Earithmetic_2E_3C_3D} (ap (ap \text{c_2Earithmetic_2E_2B} \\
& \quad V2m) V3k)) (ap (c_2Elist_2ELENGTH } A_{27a}) V1l))) \Rightarrow (p (ap (ap (c_2Elist_2EEVERY \\
& \quad A_{27a}) V0P) (ap (ap (ap (c_2Erich_list_2ESEG } A_{27a}) V2m) V3k) V1l)))))))))
\end{aligned} \tag{15}$$

Theorem 1

$$\begin{aligned}
& \forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0P \in (2^{A_{27a}}). (\forall V1l \in \\
& \quad (\text{ty_2Elist_2Elist } A_{27a}). ((p (ap (ap (c_2Elist_2EEVERY } A_{27a}) \\
& \quad V0P) V1l)) \Rightarrow (\forall V2m \in \text{ty_2Enum_2Enum}. ((p (ap (ap \text{c_2Earithmetic_2E_3C_3D} \\
& \quad V2m) (ap (c_2Elist_2ELENGTH } A_{27a}) V1l))) \Rightarrow (p (ap (ap (c_2Elist_2EEVERY \\
& \quad A_{27a}) V0P) (ap (ap (c_2Elist_2EDROP } A_{27a}) V2m) V1l)))))))))
\end{aligned}$$