

thm_2Erich_list_2ESUM__REVERSE
 (TMEjkQc3ngjwNW73QPb3iMYuZ7YFBGx3ahk)

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Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2ET to be $(ap (ap (c_2Emin_2E_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota. (\lambda V0P \in (2^{A_27a}). (ap (ap (c_2Emin_2E_3D (2^{A_27a})) (\lambda V1P \in 2.V1P)) (\lambda V2P \in 2.V2P)))$

Definition 4 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2. \lambda Q \in 2. inj_o (p \Rightarrow p Q)$ of type ι .

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2. (ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2EF))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^\omega) \quad (3)$$

Definition 7 We define c_2Enum_2E0 to be $(ap c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Let $ty_2Elist_2Elist : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow nonempty\ (ty_2Elist_2Elist\ A0) \quad (4)$$

Let $c_2Elist_2ECONS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall A_27a. nonempty\ A_27a \Rightarrow c_2Elist_2ECONS\ A_27a \in & (((ty_2Elist_2Elist\ A_27a)^{(ty_2Elist_2Elist\ A_27a)})^{A_27a}) \\ & (5) \end{aligned}$$

Let $c_2Elist_2ENIL : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A _27a. \text{nonempty } A _27a \Rightarrow c _2Elist _2ENIL \ A _27a \in (\text{ty} _2Elist _2Elist A _27a) \quad (6)$$

Let $c_2Elist_2EREVERSE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A \in \text{nonempty } A \Rightarrow c \in \text{Elist } A \text{ REVERSE } A \in ((\text{ty Elist Elist } A)^{(\text{ty Elist Elist } A)}) \quad (7)$$

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})ty_2Enum_2Enum)$ (8)

Let $c_2Elist_2ESNOC : \iota \Rightarrow \iota$ be given. Assume the following

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2Elist_2ESNOC A_27a \in (((ty_2Elist_2Elist A_27a)^{(ty_2Elist_2Elist A_27a)})^A_27a) \quad (9)$$

Let $c_2Elist_2ESUM : \iota$ be given. Assume the following.

$$c_Elist_ESUM \in (ty_Enum_Enum^{(ty_Elist_Elist\ ty_Enum_Enum)}) \quad (10)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum. (\forall V1n \in ty_2Enum_2Enum. (ap (ap c_2Earithmetic_2E_2B V0m) V1n) = ap (ap c_2Earithmetic_2E_2B V1n) V0m))) \quad (11)$$

Assume the following.

True (12)

Assume the following.

$$\forall A _27a. nonempty\ A _27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A _27a. (p _V0t)) \Leftrightarrow (p _V0t))) \quad (13)$$

Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow \text{True})) \quad (14)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow (\neg(p\ V0t))) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p\ V0t))))))) \quad (15)$$

Assume the following.

$$\begin{aligned}
 & (((ap\ c_2Elist_2ESUM\ (c_2Elist_2ENIL\ ty_2Enum_2Enum)) = c_2Enum_2E0) \wedge \\
 & \quad (\forall V0h \in ty_2Enum_2Enum. (\forall V1t \in (ty_2Elist_2Elist \\
 & \quad ty_2Enum_2Enum). ((ap\ c_2Elist_2ESUM\ (ap\ (ap\ (c_2Elist_2ECONS \\
 & \quad ty_2Enum_2Enum)\ V0h)\ V1t)) = (ap\ (ap\ c_2Earithmetic_2E_2B\ V0h) \\
 & \quad (ap\ c_2Elist_2ESUM\ V1t)))))))
 \end{aligned} \tag{16}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0P \in (2^{(ty_2Elist_2Elist\ A_27a)}). \\
 & \quad (((p\ (ap\ V0P\ (c_2Elist_2ENIL\ A_27a))) \wedge (\forall V1t \in (ty_2Elist_2Elist \\
 & \quad A_27a). ((p\ (ap\ V0P\ V1t)) \Rightarrow (\forall V2h \in A_27a. (p\ (ap\ V0P\ (ap\ (ap\ \\
 & \quad c_2Elist_2ECONS\ A_27a)\ V2h)\ V1t)))))) \Rightarrow (\forall V3l \in (ty_2Elist_2Elist \\
 & \quad A_27a). (p\ (ap\ V0P\ V3l))))))
 \end{aligned} \tag{17}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow \\
 & \quad (((ap\ (c_2Elist_2EREVERSE\ A_27b)\ (c_2Elist_2ENIL\ A_27b)) = (c_2Elist_2ENIL \\
 & \quad A_27b)) \wedge (\forall V0x \in A_27a. (\forall V1l \in (ty_2Elist_2Elist \\
 & \quad A_27a). ((ap\ (c_2Elist_2EREVERSE\ A_27a)\ (ap\ (ap\ (c_2Elist_2ECONS \\
 & \quad A_27a)\ V0x)\ V1l)) = (ap\ (ap\ (c_2Elist_2ESNOC\ A_27a)\ V0x)\ (ap\ (c_2Elist_2EREVERSE \\
 & \quad A_27a)\ V1l)))))))
 \end{aligned} \tag{18}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0x \in ty_2Enum_2Enum. (\forall V1l \in (ty_2Elist_2Elist \\
 & \quad ty_2Enum_2Enum). ((ap\ c_2Elist_2ESUM\ (ap\ (ap\ (c_2Elist_2ESNOC \\
 & \quad ty_2Enum_2Enum)\ V0x)\ V1l)) = (ap\ (ap\ c_2Earithmetic_2E_2B\ (ap\ c_2Elist_2ESUM \\
 & \quad V1l))\ V0x))))
 \end{aligned} \tag{19}$$

Theorem 1

$$(\forall V0l \in (ty_2Elist_2Elist\ ty_2Enum_2Enum). ((ap\ c_2Elist_2ESUM \\
 (ap\ (c_2Elist_2EREVERSE\ ty_2Enum_2Enum)\ V0l)) = (ap\ c_2Elist_2ESUM \\
 V0l)))$$