

thm_2Eseq_2ESEQ__DIRECT (TMXGU_nK- tyMi8o4RF35zruypVTsAmuYV1DAg)

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Definition 1 We define `c_2Emin_2E_40` to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \text{ (ap } P \ x)) \text{ then (the } (\lambda x. x \in A \wedge p \ x)) \text{ of type } \iota \Rightarrow \iota$.

Definition 2 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define `c_2Ebool_2E_3F` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } V0P \text{ (ap } (c_2Emin_2E_40 \ A \ P))$

Let `ty_2Enum_2Enum` : ι be given. Assume the following.

$$\text{nonempty } \text{ty_2Enum_2Enum} \tag{1}$$

Definition 4 We define `c_2Ebool_2E_T` to be $(\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^2)) \ (\lambda V0x \in 2. V0x)) \ (\lambda V1x \in 2. V1x))$

Definition 5 We define `c_2Ebool_2E_21` to be $\lambda A. 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (c_2Emin_2E_3D \ (2^{A-27a} \ P))$

Definition 6 We define `c_2Ebool_2E_F` to be $(\text{ap } (c_2Ebool_2E_21 \ 2) \ (\lambda V0t \in 2. V0t))$.

Definition 7 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2. \lambda Q \in 2. \text{inj_o } (p \Rightarrow q)$ of type ι .

Definition 8 We define `c_2Ebool_2E_7E` to be $(\lambda V0t \in 2. (\text{ap } (\text{ap } c_2Emin_2E_3D_3D_3E \ V0t) \ c_2Ebool_2E_F))$

Definition 9 We define `c_2Ebool_2E_2F_5C` to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (\text{ap } (c_2Ebool_2E_21 \ 2) \ (\lambda V2t \in 2. V2t))$

Let `c_2Enum_2EREP__num` : ι be given. Assume the following.

$$c_2Enum_2EREP_num \in (\text{omega}^{\text{ty_2Enum_2Enum}}) \tag{2}$$

Let `c_2Enum_2ESUC__REP` : ι be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\text{omega}^{\text{omega}}) \tag{3}$$

Let `c_2Enum_2EABS__num` : ι be given. Assume the following.

$$c_2Enum_2EABS_num \in (\text{ty_2Enum_2Enum}^{\text{omega}}) \tag{4}$$

Definition 10 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num$

Definition 11 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 12 We define $c_2Earithmetic_2E_3E$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 13 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in$

Definition 14 We define $c_2Earithmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 15 We define $c_2Earithmetic_2E_3C_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 16 We define $c_2Eseq_2Esubseq$ to be $\lambda V0f \in (ty_2Enum_2Enum^{ty_2Enum_2Enum}).(ap\ (c_2Ebo$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\ & \forall V2p \in ty_2Enum_2Enum.(((p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\ & V0m)\ V1n))) \wedge (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V1n)\ V2p)))) \Rightarrow (p\ (\\ & ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ V2p)))))) \end{aligned} \quad (5)$$

Assume the following.

$$(\forall V0m \in ty_2Enum_2Enum.(p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ V0m))) \quad (6)$$

Assume the following.

$$\begin{aligned} & (\forall V0n \in ty_2Enum_2Enum.(\forall V1m \in ty_2Enum_2Enum.(\\ & (p\ (ap\ (ap\ c_2Earithmetic_2E_3E_3D\ V0n)\ V1m))) \Leftrightarrow (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\ & V1m)\ V0n)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & (\forall V0m \in ty_2Enum_2Enum.(\forall V1n \in ty_2Enum_2Enum.(\\ & (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D\ V0m)\ V1n))) \vee (p\ (ap\ (ap\ c_2Earithmetic_2E_3C_3D \\ & V1n)\ V0m)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \wedge True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \wedge (p\ V0t)) \Leftrightarrow False) \wedge (((p\ V0t) \wedge False) \Leftrightarrow False) \wedge \\ & (((p\ V0t) \wedge (p\ V0t)) \Leftrightarrow (p\ V0t)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg(\\ & p\ V0t)))))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned}
 & (\forall V0f \in (ty_2Enum_2Enum^{ty_2Enum_2Enum}).((p (ap c_2Eseq_2Esubseq \\
 & V0f)) \Rightarrow (\forall V1n \in ty_2Enum_2Enum.(p (ap (ap c_2Earithmetic_2E_3C_3D \\
 & V1n) (ap V0f V1n))))))
 \end{aligned} \tag{11}$$

Theorem 1

$$\begin{aligned}
 & (\forall V0f \in (ty_2Enum_2Enum^{ty_2Enum_2Enum}).((p (ap c_2Eseq_2Esubseq \\
 & V0f)) \Rightarrow (\forall V1N1 \in ty_2Enum_2Enum.(\forall V2N2 \in ty_2Enum_2Enum. \\
 & (\exists V3n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E_3D \\
 & V3n) V1N1)) \wedge (p (ap (ap c_2Earithmetic_2E_3E_3D (ap V0f V3n)) V2N2))))))))))
 \end{aligned}$$