



Let  $c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epred\_set\_2EGSPEC\ A\_27a\ A\_27b \in ((2^{A\_27a})^{(ty\_2Epair\_2Eprod\ A\_27a\ 2)^{A\_27b}})$$
(3)

**Definition 11** We define  $c\_2Eset\_relation\_2Erangle$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)})$

Let  $c\_2Epair\_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epair\_2ESND\ A\_27a\ A\_27b \in (A\_27b^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)})$$
(4)

Let  $c\_2Epair\_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow c\_2Epair\_2EFST\ A\_27a\ A\_27b \in (A\_27a^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)})$$
(5)

**Definition 12** We define  $c\_2Epair\_2EUNCURRY$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda A\_27c : \iota.\lambda V0f \in ((A\_27c^{A\_27a})^{A\_27b})$

**Definition 13** We define  $c\_2Eset\_relation\_2Errestrict$  to be  $\lambda A\_27a : \iota.\lambda V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)})$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0y \in A\_27a.(\forall V1r \in (2^{(ty\_2Epair\_2Eprod\ A\_27b\ A\_27a)}). \\ & ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V0y)\ (ap\ (c\_2Eset\_relation\_2Erangle\ A\_27a\ A\_27b)\ V1r))) \Leftrightarrow (\exists V2x \in A\_27b.(p\ (ap\ (ap\ (c\_2Ebool\_2EIN \\ & \quad (ty\_2Epair\_2Eprod\ A\_27b\ A\_27a))\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27b\ A\_27a)\ V2x)\ V0y))\ V1r)))))) \end{aligned}$$
(6)

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a.(\forall V1y \in \\ & \quad A\_27a.(\forall V2r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)}).(\forall V3s \in \\ & \quad (2^{A\_27a}).((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)\ V0x)\ V1y))\ (ap\ (ap\ ( \\ & \quad c\_2Eset\_relation\_2Errestrict\ A\_27a)\ V2r)\ V3s))) \Leftrightarrow ((p\ (ap\ (ap \\ & \quad (c\_2Ebool\_2EIN\ (ty\_2Epair\_2Eprod\ A\_27a\ A\_27a))\ (ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27a\ A\_27a)\ V0x)\ V1y))\ V2r)) \wedge ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a \\ & \quad V0x)\ V3s)) \wedge (p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V1y)\ V3s)))))))))) \end{aligned}$$
(7)

**Theorem 1**

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)}). \\ & \quad (\forall V1s \in (2^{A\_27a}).(p\ (ap\ (ap\ (c\_2Epred\_set\_2ESUBSET\ A\_27a)\ (ap\ (c\_2Eset\_relation\_2Erangle\ A\_27a\ A\_27a)\ (ap\ (ap\ (c\_2Eset\_relation\_2Errestrict\ A\_27a)\ V0r)\ V1s)))\ V1s)))) \end{aligned}$$