

thm\_2Estring\_2ECHR\_\_ONTO  
(TMQLfZedH4CvXCVxtfr6uDgpxtGwwm5nDgD)

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**Definition 1** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.$ if  $(\exists x \in A.p (ap P x))$  then (the  $(\lambda x.x \in A \wedge p$  of type  $\iota \Rightarrow \iota$ ).

**Definition 2** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define  $c\_2Ebool\_2E\_3F$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap V0P (ap (c\_2Emin\_2E\_40 A$

**Definition 4** We define  $c\_2Ebool\_2E\_2ET$  to be  $(ap (ap (c\_2Emin\_2E\_3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V$

**Definition 5** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c\_2Emin\_2E\_3D (2^{A-27$

**Definition 6** We define  $c\_2Ebool\_2E\_2EF$  to be  $(ap (c\_2Ebool\_2E\_21 2) (\lambda V0t \in 2.V0t))$ .

**Definition 7** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p P \Rightarrow p Q)$  of type  $\iota$ .

**Definition 8** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2.(ap (ap c\_2Emin\_2E\_3D\_3D\_3E V0t) c\_2Ebool\_2E\_2EF$

Let  $c\_2Enum\_2EZERO\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2EZERO\_REP \in \omega \tag{1}$$

Let  $ty\_2Enum\_2Enum : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Enum\_2Enum \tag{2}$$

Let  $c\_2Enum\_2EABS\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EABS\_num \in (ty\_2Enum\_2Enum^{\omega}) \tag{3}$$

**Definition 9** We define  $c\_2Enum\_2E0$  to be  $(ap c\_2Enum\_2EABS\_num c\_2Enum\_2EZERO\_REP)$ .

**Definition 10** We define  $c\_2Earithmetic\_2EZERO$  to be  $c\_2Enum\_2E0$ .

Let  $c\_2Enum\_2EREP\_num : \iota$  be given. Assume the following.

$$c\_2Enum\_2EREP\_num \in (\omega^{ty\_2Enum\_2Enum}) \quad (4)$$

Let  $c\_2Enum\_2ESUC\_REP : \iota$  be given. Assume the following.

$$c\_2Enum\_2ESUC\_REP \in (\omega^{\omega}) \quad (5)$$

**Definition 11** We define  $c\_2Enum\_2ESUC$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.(ap\ c\_2Enum\_2EABS\_num$

Let  $c\_2Earithmetic\_2E\_2B : \iota$  be given. Assume the following.

$$c\_2Earithmetic\_2E\_2B \in ((ty\_2Enum\_2Enum)^{ty\_2Enum\_2Enum})^{ty\_2Enum\_2Enum} \quad (6)$$

**Definition 12** We define  $c\_2Earithmetic\_2EBIT1$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic$

**Definition 13** We define  $c\_2Earithmetic\_2EBIT2$  to be  $\lambda V0n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Earithmetic$

**Definition 14** We define  $c\_2Earithmetic\_2ENUMERAL$  to be  $\lambda V0x \in ty\_2Enum\_2Enum.V0x$ .

**Definition 15** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c\_2Ebool\_2E\_21\ 2)\ (\lambda V2t \in$

**Definition 16** We define  $c\_2Eprim\_rec\_2E\_3C$  to be  $\lambda V0m \in ty\_2Enum\_2Enum.\lambda V1n \in ty\_2Enum\_2Enum$

Let  $ty\_2Estring\_2Echar : \iota$  be given. Assume the following.

$$nonempty\ ty\_2Estring\_2Echar \quad (7)$$

Let  $c\_2Estring\_2EORD : \iota$  be given. Assume the following.

$$c\_2Estring\_2EORD \in (ty\_2Enum\_2Enum)^{ty\_2Estring\_2Echar} \quad (8)$$

Let  $c\_2Estring\_2ECHR : \iota$  be given. Assume the following.

$$c\_2Estring\_2ECHR \in (ty\_2Estring\_2Echar)^{ty\_2Enum\_2Enum} \quad (9)$$

Assume the following.

$$True \quad (10)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2.(((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow \neg(p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow \neg( \\ & p\ V0t)))))) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & ((\forall V0a \in ty\_2Estring\_2Echar.((ap\ c\_2Estring\_2ECHR\ (ap \\ & c\_2Estring\_2EORD\ V0a) = V0a)) \wedge (\forall V1r \in ty\_2Enum\_2Enum. \\ & ((p\ (ap\ (\lambda V2n \in ty\_2Enum\_2Enum.(ap\ (ap\ c\_2Eprim\_rec\_2E\_3C \\ & V2n)\ (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT2 \\ & (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1 \\ & (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1 \\ & (ap\ c\_2Earithmetic\_2EBIT1\ c\_2Earithmetic\_2EZERO)))))))))) \\ & V1r)) \Leftrightarrow ((ap\ c\_2Estring\_2EORD\ (ap\ c\_2Estring\_2ECHR\ V1r) = V1r)))) \end{aligned} \quad (12)$$

**Theorem 1**

$(\forall V0a \in ty\_2Estring\_2Echar. (\exists V1r \in ty\_2Enum\_2Enum.$   
 $((V0a = (ap\ c\_2Estring\_2ECHR\ V1r)) \wedge (p\ (ap\ (ap\ c\_2Eprim\_rec\_2E\_3C$   
 $V1r)\ (ap\ c\_2Earithmetic\_2ENUMERAL\ (ap\ c\_2Earithmetic\_2EBIT2$   
 $(ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1$   
 $(ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1\ (ap\ c\_2Earithmetic\_2EBIT1$   
 $(ap\ c\_2Earithmetic\_2EBIT1\ c\_2Earithmetic\_2EZERO))))))))))))))$