

# thm\_2Estring\_2ETOCHAR\_def (TMRMuUqMY- hFDMQqB69keaFcbA3dhxMYSBR5)

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Let  $ty\_2Elist\_2Elist : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty\_2Elist\_2Elist\ A0) \quad (1)$$

Let  $c\_2Elist\_2ECONS : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty\ A.27a \Rightarrow c\_2Elist\_2ECONS\ A.27a \in (((ty\_2Elist\_2Elist\ A.27a)^{(ty\_2Elist\_2Elist\ A.27a)})^{A.27a}) \quad (2)$$

Let  $c\_2Elist\_2ENIL : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty\ A.27a \Rightarrow c\_2Elist\_2ENIL\ A.27a \in (ty\_2Elist\_2Elist\ A.27a) \quad (3)$$

**Definition 1** We define  $c\_2Emin\_2E\_3D\_3D\_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o\ (P \Rightarrow Q)$  of type  $\iota$ .

**Definition 2** We define  $c\_2Emin\_2E\_3D$  to be  $\lambda A.\lambda x \in A.\lambda y \in A.inj\_o\ (x = y)$  of type  $\iota \Rightarrow \iota$ .

**Definition 3** We define  $c\_2Ebool\_2ET$  to be  $(ap\ (ap\ (c\_2Emin\_2E\_3D\ (2^2))\ (\lambda V0x \in 2.V0x))\ (\lambda V1x \in 2.V1x))$

**Definition 4** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.27a : \iota.(\lambda V0P \in (2^{A.27a}).(ap\ (ap\ (c\_2Emin\_2E\_3D\ (2^{A.27a}))\ (\lambda V1x \in 2.V1x))\ (\lambda V2x \in 2.V2x)))$

**Definition 5** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c\_2Ebool\_2E\_21\ 2)\ (\lambda V2t \in 2.V2t)))$

**Definition 6** We define  $c\_2Ebool\_2EF$  to be  $(ap\ (c\_2Ebool\_2E\_21\ 2)\ (\lambda V0t \in 2.V0t))$ .

**Definition 7** We define  $c\_2Erelation\_2EEMPTY\_REL$  to be  $\lambda A.27a : \iota.\lambda V0x \in A.27a.\lambda V1y \in A.27a.c\_2Ebool\_2E\_21$

Let  $c\_2Ebool\_2EARB : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty\ A.27a \Rightarrow c\_2Ebool\_2EARB\ A.27a \in A.27a \quad (4)$$

**Definition 8** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A.if\ (\exists x \in A.p\ (ap\ P\ x))\ then\ (the\ (\lambda x.x \in A \wedge P\ x))$  of type  $\iota \Rightarrow \iota$ .



Assume the following.

$$\forall A_{27a}.nonempty\ A_{27a} \Rightarrow (p\ (ap\ (c\_2Erelation\_2EWF\ A_{27a})\ (c\_2Erelation\_2EEMPTY\_REL\ A_{27a}))) \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall A_{27a}.nonempty\ A_{27a} \Rightarrow \forall A_{27b}.nonempty\ A_{27b} \Rightarrow ( \\ & \quad \forall V0M \in ((A_{27b}^{A_{27a}})^{(A_{27b}^{A_{27a}})}), (\forall V1R \in ((2^{A_{27a}})^{A_{27a}}). \\ & \quad (\forall V2f \in (A_{27b}^{A_{27a}}). ((V2f = (ap\ (ap\ (c\_2Erelation\_2EWFREC \\ & \quad A_{27a}\ A_{27b})\ V1R)\ V0M)) \Rightarrow ((p\ (ap\ (c\_2Erelation\_2EWF\ A_{27a})\ V1R)) \Rightarrow \\ & \quad (\forall V3x \in A_{27a}. ((ap\ V2f\ V3x) = (ap\ (ap\ V0M\ (ap\ (ap\ (ap\ (c\_2Erelation\_2ERESTRICT \\ & \quad A_{27a}\ A_{27b})\ V2f)\ V1R)\ V3x))\ V3x))))))))) \end{aligned} \quad (10)$$

**Theorem 1**

$$(\forall V0c \in ty\_2Estring\_2Echar. ((ap\ c\_2Estring\_2ETOCHAR\ (ap\ (ap\ (c\_2Elist\_2ECONS\ ty\_2Estring\_2Echar)\ V0c)\ (c\_2Elist\_2ENIL\ ty\_2Estring\_2Echar))) = V0c))$$