

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 8 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2E_2B))$.

Definition 9 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 10 We define c_2Ebool_2EF to be $(ap (c_2Ebool_2E_21 2)) (\lambda V0t \in 2.V0t)$.

Definition 11 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap (ap c_2Emin_2E_3D_3D_3E V0t) c_2Ebool_2E_21 2))$.

Definition 12 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2)) (\lambda V2t \in 2.V2t)))$.

Definition 13 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\text{if } (\exists x \in A.p (ap P x)) \text{ then } (the (\lambda x.x \in A \wedge P x) \text{ of type } \iota \Rightarrow \iota)$.

Definition 14 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap V0P (ap (c_2Emin_2E_40 A P))))$.

Definition 15 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.V1n$.

Let $ty_2EternaryComparisons_2Eordering : \iota$ be given. Assume the following.

$$nonempty\ ty_2EternaryComparisons_2Eordering \quad (7)$$

Let $c_2EternaryComparisons_2Eordering2num : \iota$ be given. Assume the following.

$$c_2EternaryComparisons_2Eordering2num \in (ty_2Enum_2Enum^{ty_2EternaryComparisons_2Eordering}) \quad (8)$$

Let $c_2EternaryComparisons_2Enum2ordering : \iota$ be given. Assume the following.

$$c_2EternaryComparisons_2Enum2ordering \in (ty_2EternaryComparisons_2Eordering^{ty_2Enum_2Enum}) \quad (9)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (10)$$

Assume the following.

$$\begin{aligned} & ((\forall V0a \in ty_2EternaryComparisons_2Eordering.((ap c_2EternaryComparisons_2Enum2ordering \\ & \quad (ap c_2EternaryComparisons_2Eordering2num V0a)) = V0a)) \wedge (\forall V1r \in \\ & \quad ty_2Enum_2Enum.((p (ap (\lambda V2n \in ty_2Enum_2Enum.(ap (ap c_2Eprim_rec_2E_3C \\ & \quad V2n) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\ & \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))))) V1r)) \Leftrightarrow \\ & \quad ((ap c_2EternaryComparisons_2Eordering2num (ap c_2EternaryComparisons_2Enum2ordering \\ & \quad V1r)) = V1r)))) \quad (11) \end{aligned}$$

Theorem 1

$$\begin{aligned} & (\forall V0a \in \text{ty_2EternaryComparisons_2Eordering} . (\forall V1a_27 \in \\ & \text{ty_2EternaryComparisons_2Eordering} . (((\text{ap } c_2EternaryComparisons_2Eordering2num \\ & V0a) = (\text{ap } c_2EternaryComparisons_2Eordering2num V1a_27)) \Leftrightarrow (\\ & V0a = V1a_27)))) \end{aligned}$$