

thm_2EternaryComparisons_2Eordering2num_11 (TMb4uj73NCM4pXnVcGB8irmkykZ68JLrZqa1)

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Definition 1 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \ P \Rightarrow p \ Q)$ of type ι .

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (1)$$

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty \ ty_2Enum_2Enum \quad (2)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (3)$$

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define c_2Enum_2E0 to be ($ap \ c_2Enum_2EABS_num \ c_2Enum_2EZERO_REP$).

Definition 4 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (4)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (5)$$

Definition 5 We define c_2Ebool_2ET to be ($ap \ (ap \ (c_2Emin_2E_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x)$)

Definition 6 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap \ (ap \ (c_2Emin_2E_3D \ (2^{A_27a})) \ (\lambda V1x \in 2.V1x)))$

Definition 7 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap \ c_2Enum_2EABS_num \ (m \ c_2Enum_2EREP_num))$

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (6)$$

Definition 8 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earithmetic_2EBIT1\ n)\ V)$

Definition 9 We define $c_2Earthmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Definition 10 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V0t\ t \in 2.V0t))$.

Definition 11 We define $c_2Eb0o_2E_7E$ to be $(\lambda V0t \in 2.(ap\ (ap\ c_2Emin_2E_3D_3D_3E\ V0t)\ c_2Eb0o_2E_7E))$

Definition 12 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in$

Definition 13 We define $c_2 \in \text{Min}(\mathcal{E})$ to be $\lambda A.\lambda P \in 2^A$, if $(\exists x \in A.p(ap P x))$ then $(\lambda x.x \in A \wedge$

Definition 14 We define $c_2 \in \mathbb{F}_{2^m}$ to be $\lambda A. 27a : \iota$ ($\lambda V0P \in (2^{A-27a})$) ($\lambda P. V0P$) ($\lambda P. (c_2 \oplus \min(2^A, 40))P$)

Definition 15. We define \mathcal{C} -2Eprim-rec-3C to be $\lambda V0m \in tu\text{-}2Enum\text{-}2Enum\ \lambda V1n \in tu\text{-}2Enum\text{-}2Enum$

Let $t \in 2E$ and $\alpha : \text{Comparison}(2E)$ be given. Assume the following.

following.

Let c \in *EternaryComparisons* \cap *Enum2ordering*. Assume the following:

Let $\mathcal{E} = \text{EternityComparisons}[\mathcal{L}, \text{nam}, \text{ordering}]$. It be given. Assume the following.

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$$((\forall V0t1 \in Z. (\forall V1t2 \in Z. (((p \vee 0t1) \Rightarrow (p \vee 1t2)) \Rightarrow (((p \vee 1t2) \Rightarrow (p \vee 0t1)) \Rightarrow (((p \vee 0t1) \Leftrightarrow (p \vee 1t2))))))) \quad (10)$$

Assume the following.

$$\begin{aligned}
& ((\forall V0a \in ty_2EternaryComparisons_2Eordering.((ap c_2EternaryComparisons_2Enum2ordering \\
& \quad (ap c_2EternaryComparisons_2Eordering2num V0a)) = V0a)) \wedge (\forall V1r \in \\
& \quad ty_2Enum_2Enum.((p (ap (\lambda V2n \in ty_2Enum_2Enum.(ap (ap c_2Eprim_rec_2E_3C \\
& \quad V2n) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 \\
& \quad (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) V1r))) \Leftrightarrow \\
& ((ap c_2EternaryComparisons_2Eordering2num (ap c_2EternaryComparisons_2Enum2ordering \\
& \quad V1r)) = V1r)))
\end{aligned} \tag{11}$$

Theorem 1

$$(\forall V0a \in ty_2EternaryComparisons_2Eordering. (\forall V1a_27 \in ty_2EternaryComparisons_2Eordering. (((ap\ c_2EternaryComparisons_2Eordering2num\ V0a) = (ap\ c_2EternaryComparisons_2Eordering2num\ V1a_27)) \Leftrightarrow (V0a = V1a_27))))$$