

thm\_2Etoto\_2ETO\_of\_less\_rel  
(TMYZ29nwkpU8gMub4nVh93jZ4WCMYTcRRZx)

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**Definition 1** We define  $c_2Emin_2E_3D_3D_3E$  to be  $\lambda P \in 2.\lambda Q \in 2.inj\_o (p\ P \Rightarrow p\ Q)$  of type  $\iota$ .

**Definition 2** We define  $c_2Emin\_2E_3D$  to be  $\lambda A. \lambda x \in A. \lambda y \in A. inj\_o (x = y)$  of type  $\iota \rightarrow \iota$ .

**Definition 3** We define  $c\_Ebool\_ET$  to be  $(ap \ (ap \ (c\_Emin\_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x))$

**Definition 4** We define  $c\_2Ebool\_2E\_21$  to be  $\lambda A.27a : \iota.(\lambda V0P \in (2^A\_{27a}).(ap\ (ap\ (c\_2Emin\_2E\_3D\ (2^A\_{27a}\_21)\ V)\ P)\ 0)$

**Definition 5** We define  $c\_Ebool\_E\_5C\_2F$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c\_Ebool\_E\_21 2))(\lambda V2t \in 2.$

**Definition 6** We define  $c\_2Ebool\_2EF$  to be  $(ap\ (c\_2Ebool\_2E_21\ 2)\ (\lambda V0t\in 2.V0t))$ .

**Definition 7** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c\_2Ebool\_2E\_21\ 2)\ (\lambda V2t \in 2.\dots)))$

**Definition 8** We define  $c\_2Erelation\_2Etransitive$  to be  $\lambda A\_27a : \iota. \lambda V0R \in ((2^{A\_27a})^{A\_27a}).(ap\ (c\_2Ebool\_2E$

**Definition 9** We define  $c\_2Ebool\_2E\_7E$  to be  $(\lambda V0t \in 2.(ap\ (ap\ c\_2Emin\_2E\_3D\_3D\_3E\ V0t)\ c\_2Ebool\_2EF))$

**Definition 10** We define  $c\text{-}2\mathsf{Erelation}\text{-}2\mathsf{Eirreflexive}$  to be  $\lambda A.\exists 2a:\iota.\lambda V0R\in((2^{A\text{-}27a})^{A\text{-}27a}).(\lambda p(c\text{-}2\mathsf{Ebool}\text{-}2\mathsf{Eirreflexive}))$

**Definition 11.** We define a 2Erelation 2Etrichotomous to be  $\lambda A. \exists \vec{a} : \iota. \lambda V0B \in ((2^{A-27a})^A)^{A-27a}$  (an  $\iota$ -2Efunction

**Definition 12.** We define a 2Frelation, 2FStrongOrder, to be  $\lambda A. \exists g : \iota. \lambda V0Z. ((^{(2A-27g)}V)^{A-27g})$  (ap, (ap)  $\in$  2F)

D. Section 12. Week 6 - 25. Let  $\alpha = \text{CES}(r, k)$ . Calculate  $\lambda^A$ ,  $\lambda^{27}$ ,  $\lambda^{NOB}$ ,  $\pi_A(\alpha^A, \alpha^{27})$ ,  $\pi_{27}(\alpha^A, \alpha^{27})$ ,  $\pi_{NOB}(\alpha^A, \alpha^{27})$ .

**Definition 1.4.** We define a  $2\Gamma$ -min- $2\Gamma$ -4B to be  $\lambda A.B \in 2\Gamma$  if  $(\exists n \in A.n.(an.B))$ , then (the  $\lambda n.n \in A.n$ )

**D. Statistics** 15. We have  $\text{SE}_{\bar{X}} = \text{SECOND}(\bar{X})^{1/2} / \sqrt{N} = 0.00154 \approx 0.00154$ ,  $(N\bar{X}_1) = 0.00154$ ,  $(N\bar{X}_2) = 0.00154$ ,  $(N\bar{X}_3) = 0.00154$ ,  $(N\bar{X}_4) = 0.00154$ ,  $(N\bar{X}_5) = 0.00154$ ,  $(N\bar{X}_6) = 0.00154$ ,  $(N\bar{X}_7) = 0.00154$ ,  $(N\bar{X}_8) = 0.00154$ ,  $(N\bar{X}_9) = 0.00154$ ,  $(N\bar{X}_{10}) = 0.00154$ .

Let  $ty\_2EternaryComparisons\_2Ordering : \iota$  be given. Assume the following.

$$nonempty\ ty\_2EternaryComparisons\_2Ordering \quad (1)$$

Let  $c\_2EternaryComparisons\_2EGREATER : \iota$  be given. Assume the following.

$$c\_2EternaryComparisons\_2EGREATER \in ty\_2EternaryComparisons\_2Ordering \quad (2)$$

Let  $c\_2EternaryComparisons\_2ELESS : \iota$  be given. Assume the following.

$$c\_2EternaryComparisons\_2ELESS \in ty\_2EternaryComparisons\_2Ordering \quad (3)$$

Let  $c\_2EternaryComparisons\_2EQUAL : \iota$  be given. Assume the following.

$$c\_2EternaryComparisons\_2EQUAL \in ty\_2EternaryComparisons\_2Ordering \quad (4)$$

**Definition 16** We define  $c\_2Etoto\_2ETO\_of\_LinearOrder$  to be  $\lambda A\_27a : \iota. \lambda V0r \in ((2^{A\_27a})^{A\_27a}). \lambda V1x \in$

Assume the following.

$$True \quad (5)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2))))) \quad (6)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \quad (7)$$

Assume the following.

$$(\forall V0t \in 2. ((p V0t) \vee (\neg(p V0t)))) \quad (8)$$

Assume the following.

$$((\forall V0t \in 2. ((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (9)$$

Assume the following.

$$\forall A\_27a. nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (10)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall A\_27a.\text{nonempty } A\_27a \Rightarrow & (\forall V0t1 \in A\_27a.(\forall V1t2 \in \\ A\_27a.(((ap (ap (ap (c\_2Ebool\_2ECOND A\_27a) c\_2Ebool\_2ET) V0t1) \\ V1t2) = V0t1) \wedge ((ap (ap (ap (c\_2Ebool\_2ECOND A\_27a) c\_2Ebool\_2EF) \\ V0t1) V1t2) = V1t2)))))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} (((\neg(c\_2EternaryComparisons\_2ELESS = c\_2EternaryComparisons\_2EQUAL)) \wedge \\ ((\neg(c\_2EternaryComparisons\_2ELESS = c\_2EternaryComparisons\_2EGREATER)) \wedge \\ (\neg(c\_2EternaryComparisons\_2EQUAL = c\_2EternaryComparisons\_2EGREATER)))) \wedge \\ ((\neg(c\_2EternaryComparisons\_2EQUAL = c\_2EternaryComparisons\_2ELESS)) \wedge \\ ((\neg(c\_2EternaryComparisons\_2EGREATER = c\_2EternaryComparisons\_2ELESS)) \wedge \\ (\neg(c\_2EternaryComparisons\_2EGREATER = c\_2EternaryComparisons\_2EQUAL)))))) \end{aligned} \quad (13)$$

### Theorem 1

$$\begin{aligned} \forall A\_27a.\text{nonempty } A\_27a \Rightarrow & (\forall V0r \in ((2^{A\_27a})^{A\_27a}). \\ ((p (ap (c\_2Erelation\_2EStrongLinearOrder A\_27a) V0r)) \Rightarrow (\forall V1x \in \\ A\_27a.(\forall V2y \in A\_27a.(((ap (ap (c\_2Etoto\_2ETO\_of\_LinearOrder \\ A\_27a) V0r) V1x) V2y) = c\_2EternaryComparisons\_2ELESS) \Leftrightarrow (p (ap \\ (ap V0r V1x) V2y))))))) \end{aligned}$$