

Definition 6 We define $c_2Etoto_2ETotOrd$ to be $\lambda A_27a : \iota.\lambda V0c \in ((ty_2EternaryComparisons_2Eorde$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0c \in (ty_2Etoto_2Etoto\ A_27a).(p\ (ap\ (c_2Etoto_2ETotOrd\ A_27a)\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)))) \quad (7)$$

Theorem 1

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0c \in (ty_2Etoto_2Etoto\ A_27a).((\forall V1x \in A_27a.(\forall V2y \in A_27a.(((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V1x)\ V2y) = c_2EternaryComparisons_2EEQUAL) \Leftrightarrow \\ & (V1x = V2y)))) \wedge ((\forall V3x \in A_27a.(\forall V4y \in A_27a.(((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V3x)\ V4y) = c_2EternaryComparisons_2EGREATER) \Leftrightarrow \\ & ((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V4y)\ V3x) = c_2EternaryComparisons_2ELESS)))) \wedge \\ & (\forall V5x \in A_27a.(\forall V6y \in A_27a.(\forall V7z \in A_27a.(((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V5x)\ V6y) = c_2EternaryComparisons_2ELESS) \wedge \\ & ((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V6y)\ V7z) = c_2EternaryComparisons_2ELESS)) \Rightarrow \\ & ((ap\ (ap\ (ap\ (c_2Etoto_2Eapto\ A_27a)\ V0c)\ V5x)\ V7z) = c_2EternaryComparisons_2ELESS)))))) \end{aligned}$$