



**Definition 9** We define  $c\_2Emin\_2E\_40$  to be  $\lambda A.\lambda P \in 2^A$ . **if**  $(\exists x \in A.p (ap P x))$  **then** (the  $(\lambda x.x \in A \wedge p$  of type  $\iota \Rightarrow \iota$ ).

**Definition 10** We define  $c\_2Eordinal\_2Eordinal\_REP$  to be  $\lambda A.27a : \iota.\lambda V0a \in (ty\_2Eordinal\_2Eordinal A$   
Let  $ty\_2Epair\_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty\_2Epair\_2Eprod A0 A1) \quad (6)$$

Let  $c\_2Ewellorder\_2Ewellorder\_REP : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow c\_2Ewellorder\_2Ewellorder\_REP A.27a \in ((2^{(ty\_2Epair\_2Eprod A.27a A.27a)})^{(ty\_2Ewellorder\_2Ewellorder A.27a)}) \quad (7)$$

**Definition 11** We define  $c\_2Ebool\_2E\_2F\_5C$  to be  $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c\_2Ebool\_2E\_21 2) (\lambda V2t \in$

Let  $c\_2Epair\_2EABS\_prod : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow \forall A.27b.nonempty A.27b \Rightarrow c\_2Epair\_2EABS\_prod A.27a A.27b \in ((ty\_2Epair\_2Eprod A.27a A.27b)^{(2^{A.27b})^{A.27a}}) \quad (8)$$

**Definition 12** We define  $c\_2Epair\_2E\_2C$  to be  $\lambda A.27a : \iota.\lambda A.27b : \iota.\lambda V0x \in A.27a.\lambda V1y \in A.27b.(ap (c\_2$

**Definition 13** We define  $c\_2Ebool\_2EIN$  to be  $\lambda A.27a : \iota.(\lambda V0x \in A.27a.(\lambda V1f \in (2^{A.27a}).(ap V1f V0x))$

Let  $c\_2Epair\_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow \forall A.27b.nonempty A.27b \Rightarrow c\_2Epair\_2ESND A.27a A.27b \in (A.27b^{(ty\_2Epair\_2Eprod A.27a A.27b)}) \quad (9)$$

Let  $c\_2Epair\_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow \forall A.27b.nonempty A.27b \Rightarrow c\_2Epair\_2EFST A.27a A.27b \in (A.27a^{(ty\_2Epair\_2Eprod A.27a A.27b)}) \quad (10)$$

**Definition 14** We define  $c\_2Epair\_2EUNCURRY$  to be  $\lambda A.27a : \iota.\lambda A.27b : \iota.\lambda A.27c : \iota.\lambda V0f \in ((A.27c^{A.27$

Let  $c\_2Epred\_set\_2EGSPEC : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow \forall A.27b.nonempty A.27b \Rightarrow c\_2Epred\_set\_2EGSPEC A.27a A.27b \in ((2^{A.27a})^{(ty\_2Epair\_2Eprod A.27a 2)^{A.27b}}) \quad (11)$$

**Definition 15** We define  $c\_2Eset\_relation\_2Estrict$  to be  $\lambda A.27a : \iota.\lambda V0r \in (2^{(ty\_2Epair\_2Eprod A.27a A.27a)})$

**Definition 16** We define  $c\_2Ewellorder\_2Eiseg$  to be  $\lambda A.27a : \iota.\lambda V0w \in (ty\_2Ewellorder\_2Ewellorder A.2$

**Definition 17** We define  $c\_Eset\_relation\_Erestrict$  to be  $\lambda A\_27a : \iota. \lambda V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)})$

Let  $c\_Ewellorder\_Ewellorder\_ABS : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall A\_27a. nonempty\ A\_27a \Rightarrow c\_Ewellorder\_Ewellorder\_ABS \\ & A\_27a \in ((ty\_2Ewellorder\_Ewellorder\ A\_27a)^{(2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27a)})}) \end{aligned} \quad (12)$$

**Definition 18** We define  $c\_Ewellorder\_Ewobound$  to be  $\lambda A\_27a : \iota. \lambda V0x \in A\_27a. \lambda V1w \in (ty\_2Ewellorder\ A\_27a)$

**Definition 19** We define  $c\_Ebool\_2E3F$  to be  $\lambda A\_27a : \iota. (\lambda V0P \in (2^{A\_27a}). (ap\ V0P\ (ap\ (c\_2Emin\_2E40\ A\_27a))))$

**Definition 20** We define  $c\_Eset\_relation\_ERange$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)})$

**Definition 21** We define  $c\_Eset\_relation\_EDomain$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0r \in (2^{(ty\_2Epair\_2Eprod\ A\_27a\ A\_27b)})$

**Definition 22** We define  $c\_Epred\_set\_2EUNION$  to be  $\lambda A\_27a : \iota. \lambda V0s \in (2^{A\_27a}). \lambda V1t \in (2^{A\_27a}). (ap\ (c\_2Epred\_set\_2EUNION\ A\_27a\ s\ t))$

**Definition 23** We define  $c\_Ewellorder\_2EelsOf$  to be  $\lambda A\_27a : \iota. \lambda V0w \in (ty\_2Ewellorder\_Ewellorder\ A\_27a)$

**Definition 24** We define  $c\_Ewellorder\_2Eorderiso$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0w1 \in (ty\_2Ewellorder\_Ewellorder\ A\_27a)$

**Definition 25** We define  $c\_Ewellorder\_2Eorderlt$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0w1 \in (ty\_2Ewellorder\_Ewellorder\ A\_27a)$

**Definition 26** We define  $c\_2Eordinal\_2Eordlt$  to be  $\lambda A\_27a : \iota. \lambda V0T1 \in (ty\_2Eordinal\_2Eordinal\ A\_27a)$

**Definition 27** We define  $c\_2Eordinal\_2Eoleast$  to be  $\lambda A\_27a : \iota. \lambda V0P \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)})$

**Definition 28** We define  $c\_2Eordinal\_2EordSUC$  to be  $\lambda A\_27a : \iota. \lambda V0a \in (ty\_2Eordinal\_2Eordinal\ A\_27a)$

**Definition 29** We define  $c\_2Eveblen\_2Eunbounded$  to be  $\lambda A\_27a : \iota. \lambda V0A \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)})$

**Definition 30** We define  $c\_2Eordinal\_2Epreds$  to be  $\lambda A\_27a : \iota. \lambda V0w \in (ty\_2Eordinal\_2Eordinal\ A\_27a)$

**Definition 31** We define  $c\_2Epred\_set\_2EIMAGE$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (A\_27b^{A\_27a}). \lambda V1s \in (2^{A\_27b})$

**Definition 32** We define  $c\_2Epred\_set\_2EBIGUNION$  to be  $\lambda A\_27a : \iota. \lambda V0P \in (2^{(2^{A\_27a})})$

**Definition 33** We define  $c\_2Eordinal\_2Esup$  to be  $\lambda A\_27a : \iota. \lambda V0ordset \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)})$

**Definition 34** We define  $c\_2Eveblen\_2Eclosed$  to be  $\lambda A\_27a : \iota. \lambda V0A \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)})$

**Definition 35** We define  $c\_2Eveblen\_2Eclub$  to be  $\lambda A\_27a : \iota. \lambda V0A \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)})$

**Definition 36** We define  $c\_2Epred\_set\_2EUNIV$  to be  $\lambda A\_27a : \iota. (\lambda V0x \in A\_27a. c\_2Ebool\_2EET)$

**Definition 37** We define  $c\_2Epred\_set\_2EINJ$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in (A\_27b^{A\_27a}). \lambda V1s \in (2^{A\_27b})$

**Definition 38** We define  $c\_2Ecardinal\_2Ecardleq$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0s1 \in (2^{A\_27a}). \lambda V1s2 \in (2^{A\_27b})$

**Definition 39** We define  $c\_2Eveblen\_2Econtinuous$  to be  $\lambda A\_27a : \iota. \lambda A\_27b : \iota. \lambda V0f \in ((ty\_2Eordinal\_2Eordinal\ A\_27a)^{A\_27b})$

**Definition 40** We define  $c\_2Eveblen\_2Estrict\_mono$  to be  $\lambda A\_27a : \iota.\lambda A\_27b : \iota.\lambda V0f \in ((ty\_2Eordinal\_2E$

Assume the following.

$$True \quad (13)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (14)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p V0t))) \quad (15)$$

Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow (\forall V0t \in 2.((\forall V1x \in A\_27a.(p V0t)) \Leftrightarrow (p V0t))) \quad (16)$$

Assume the following.

$$(\forall V0t \in 2.(((True \wedge (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \wedge True) \Leftrightarrow (p V0t)) \wedge (((False \wedge (p V0t)) \Leftrightarrow False) \wedge (((p V0t) \wedge False) \Leftrightarrow False) \wedge (((p V0t) \wedge (p V0t)) \Leftrightarrow (p V0t)))))) \quad (17)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge ((p V0t) \Rightarrow False) \Leftrightarrow (\neg (p V0t)))))) \quad (18)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t))) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True))) \quad (19)$$

Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow (\forall V0x \in A\_27a.((V0x = V0x) \Leftrightarrow True)) \quad (20)$$

Assume the following.

$$\forall A\_27a.nonempty A\_27a \Rightarrow (\forall V0x \in A\_27a.(\forall V1y \in A\_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (21)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (22)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in (2^{A\_27a}). (\forall V1Q \in \\ & 2. ((\exists V2x \in A\_27a. ((p\ (ap\ V0P\ V2x)) \wedge (p\ V1Q))) \Leftrightarrow ((\exists V3x \in \\ & A\_27a. (p\ (ap\ V0P\ V3x)) \wedge (p\ V1Q)))))) \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in (2^{A\_27a}). (\forall V1Q \in \\ & 2. ((\forall V2x \in A\_27a. ((p\ (ap\ V0P\ V2x)) \Rightarrow (p\ V1Q))) \Leftrightarrow ((\exists V3x \in \\ & A\_27a. (p\ (ap\ V0P\ V3x)) \Rightarrow (p\ V1Q)))))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((p\ V0A) \Rightarrow (p\ V1B)) \Leftrightarrow ((\neg(p\ V0A)) \vee \\ & (p\ V1B)))))) \end{aligned} \quad (25)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow \\ & ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (26)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2. (\forall V1x\_27 \in 2. (\forall V2y \in 2. (\forall V3y\_27 \in \\ & 2. (((p\ V0x) \Leftrightarrow (p\ V1x\_27)) \wedge ((p\ V1x\_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y\_27)))))) \Rightarrow \\ & (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x\_27) \Rightarrow (p\ V3y\_27)))))) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0P \in (2^{A\_27a}). (\forall V1a \in \\ & A\_27a. ((\exists V2x \in A\_27a. ((V2x = V1a) \wedge (p\ (ap\ V0P\ V2x)))) \Leftrightarrow (p\ ( \\ & ap\ V0P\ V1a)))))) \end{aligned} \quad (28)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0f \in (2^{A\_27a}). (\forall V1v \in \\ & A\_27a. ((\forall V2x \in A\_27a. ((V2x = V1v) \Rightarrow (p\ (ap\ V0f\ V2x)))) \Leftrightarrow (p\ ( \\ & ap\ V0f\ V1v)))))) \end{aligned} \quad (29)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow \forall A\_27c. \\ & nonempty\ A\_27c \Rightarrow (\forall V0f \in (A\_27c^{A\_27a}). (\forall V1s \in (2^{A\_27a}). \\ & (\forall V2t \in (2^{A\_27b}). ((p\ (ap\ (ap\ (c\_2Ecardinal\_2Ecardleq\ A\_27a \\ & A\_27b)\ V1s)\ V2t)) \Rightarrow (p\ (ap\ (ap\ (c\_2Ecardinal\_2Ecardleq\ A\_27c\ A\_27b) \\ & (ap\ (ap\ (c\_2Epred\_set\_2EIMAGE\ A\_27a\ A\_27c)\ V0f)\ V1s))\ V2t)))))) \end{aligned} \quad (30)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0w \in (ty\_2Eordinal\_2Eordinal \\ & A\_27a). (\neg(p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V0w)\ V0w)))) \end{aligned} \quad (31)$$

Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in (ty\_2Eordinal\_2Eordinal \\ A\_27a).(\forall V1y \in (ty\_2Eordinal\_2Eordinal\ A\_27a).(\forall V2z \in \\ (ty\_2Eordinal\_2Eordinal\ A\_27a).(((\neg(p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt \\ A\_27a)\ V1y)\ V0x))) \wedge (p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V1y) \\ V2z)))) \Rightarrow (p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V0x)\ V2z)))))) \end{aligned} \quad (32)$$

Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0Q \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)}). \\ (\forall V1P \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)}).(((\exists V2a \in \\ (ty\_2Eordinal\_2Eordinal\ A\_27a).(p\ (ap\ V1P\ V2a))) \wedge (\forall V3a \in \\ (ty\_2Eordinal\_2Eordinal\ A\_27a).(((\forall V4b \in (ty\_2Eordinal\_2Eordinal \\ A\_27a).((p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V4b)\ V3a)) \Rightarrow (\neg \\ p\ (ap\ V1P\ V4b)))))) \wedge (p\ (ap\ V1P\ V3a))) \Rightarrow (p\ (ap\ V0Q\ V3a)))) \Rightarrow (p\ (ap\ V0Q \\ (ap\ (c\_2Eordinal\_2Eoleast\ A\_27a)\ V1P)))))) \end{aligned} \quad (33)$$

Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0a \in (ty\_2Eordinal\_2Eordinal \\ A\_27a).(p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V0a)\ (ap\ (c\_2Eordinal\_2EordSUC \\ A\_27a)\ V0a)))) \end{aligned} \quad (34)$$

Assume the following.

$$\begin{aligned} \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0s1 \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)}). \\ (\forall V1s2 \in (2^{(ty\_2Eordinal\_2Eordinal\ A\_27a)}).(((p\ (ap\ ( \\ ap\ (c\_2Ecardinal\_2Ecardleq\ (ty\_2Eordinal\_2Eordinal\ A\_27a)\ ( \\ ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum\ A\_27a))\ V0s1)\ (c\_2Epred\_set\_2EUNIV \\ (ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum\ A\_27a)))) \wedge ((p\ (ap\ (c\_2Ecardinal\_2Ecardleq \\ (ty\_2Eordinal\_2Eordinal\ A\_27a)\ (ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum \\ A\_27a))\ V1s2)\ (c\_2Epred\_set\_2EUNIV\ (ty\_2Esum\_2Esum\ ty\_2Enum\_2Enum \\ A\_27a)))) \wedge ((\forall V2a \in (ty\_2Eordinal\_2Eordinal\ A\_27a).(( \\ p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Eordinal\_2Eordinal\ A\_27a))\ V2a) \\ V0s1)) \Rightarrow (\exists V3b \in (ty\_2Eordinal\_2Eordinal\ A\_27a).((p\ (ap \\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Eordinal\_2Eordinal\ A\_27a))\ V3b)\ V1s2)) \wedge \\ (\neg(p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V3b)\ V2a)))))) \wedge (\forall V4b \in \\ (ty\_2Eordinal\_2Eordinal\ A\_27a).((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Eordinal\_2Eordinal \\ A\_27a))\ V4b)\ V1s2)) \Rightarrow (\exists V5a \in (ty\_2Eordinal\_2Eordinal\ A\_27a). \\ ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ (ty\_2Eordinal\_2Eordinal\ A\_27a))\ V5a) \\ V0s1)) \wedge (\neg(p\ (ap\ (ap\ (c\_2Eordinal\_2Eordlt\ A\_27a)\ V5a)\ V4b)))))))))) \Rightarrow \\ ((ap\ (c\_2Eordinal\_2Esup\ A\_27a)\ V0s1) = (ap\ (c\_2Eordinal\_2Esup \\ A\_27a)\ V1s2)))) \end{aligned} \quad (35)$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0x \in A\_27a. (\forall V1y \in A\_27b. (\forall V2a \in A\_27a. (\forall V3b \in \\ & \quad A\_27b. (((ap\ (ap\ (c\_2Epair\_2E\_2C\ A\_27a\ A\_27b)\ V0x)\ V1y) = (ap\ (ap \\ & \quad (c\_2Epair\_2E\_2C\ A\_27a\ A\_27b)\ V2a)\ V3b)) \Leftrightarrow ((V0x = V2a) \wedge (V1y = V3b)))))) \\ & \end{aligned} \tag{36}$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0f \in ((ty\_2Epair\_2Eprod\ A\_27a\ 2)^{A\_27b}). (\forall V1v \in \\ & \quad A\_27a. ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V1v)\ (ap\ (c\_2Epred\_set\_2EGSPEC \\ & \quad A\_27a\ A\_27b)\ V0f))) \Leftrightarrow (\exists V2x \in A\_27b. ((ap\ (ap\ (c\_2Epair\_2E\_2C \\ & \quad A\_27a\ 2)\ V1v)\ c\_2Ebool\_2ET) = (ap\ V0f\ V2x)))))) \\ & \end{aligned} \tag{37}$$

Assume the following.

$$\forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0x \in A\_27a. (p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V0x)\ (c\_2Epred\_set\_2EUNIV\ A\_27a)))) \tag{38}$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0y \in A\_27b. (\forall V1s \in (2^{A\_27a}). (\forall V2f \in (A\_27b^{A\_27a}). \\ & \quad ((p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27b)\ V0y)\ (ap\ (ap\ (c\_2Epred\_set\_2EIMAGE \\ & \quad A\_27a\ A\_27b)\ V2f)\ V1s))) \Leftrightarrow (\exists V3x \in A\_27a. ((V0y = (ap\ V2f\ V3x)) \wedge \\ & \quad (p\ (ap\ (ap\ (c\_2Ebool\_2EIN\ A\_27a)\ V3x)\ V1s)))))) \\ & \end{aligned} \tag{39}$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow \forall A\_27b.nonempty\ A\_27b \Rightarrow ( \\ & \quad \forall V0f \in (A\_27b^{ty\_2Eenum\_2Eenum}). (p\ (ap\ (ap\ (c\_2Ecardinal\_2Ecardleq \\ & \quad A\_27b\ (ty\_2Esum\_2Esum\ ty\_2Eenum\_2Eenum\ A\_27a))\ (ap\ (c\_2Epred\_set\_2EGSPEC \\ & \quad A\_27b\ ty\_2Eenum\_2Eenum)\ (\lambda V1n \in ty\_2Eenum\_2Eenum. (ap\ (ap\ (c\_2Epair\_2E\_2C \\ & \quad A\_27b\ 2)\ (ap\ V0f\ V1n))\ c\_2Ebool\_2ET))))\ (c\_2Epred\_set\_2EUNIV \\ & \quad (ty\_2Esum\_2Esum\ ty\_2Eenum\_2Eenum\ A\_27a)))) \\ & \end{aligned} \tag{40}$$

Assume the following.

$$\begin{aligned} & \forall A\_27a.nonempty\ A\_27a \Rightarrow (\forall V0f \in ((ty\_2Eordinal\_2Eordinal \\ & \quad A\_27a)^{(ty\_2Eordinal\_2Eordinal\ A\_27a)}). (\forall V1x \in (ty\_2Eordinal\_2Eordinal \\ & \quad A\_27a). (((p\ (ap\ (c\_2Eveblen\_2Estrict\_mono\ A\_27a\ A\_27a)\ V0f)) \wedge \\ & \quad (p\ (ap\ (c\_2Eveblen\_2Econtinuous\ A\_27a\ A\_27a)\ V0f))) \Rightarrow (\neg (p\ (ap\ ( \\ & \quad (c\_2Eordinal\_2Eordlt\ A\_27a)\ (ap\ V0f\ V1x))\ V1x)))))) \\ & \end{aligned} \tag{41}$$

**Theorem 1**

$$\forall A_{27a}. \text{nonempty } A_{27a} \Rightarrow (\forall V0f \in ((ty\_2Eordinal\_2Eordinal \\ A_{27a})^{(ty\_2Eordinal\_2Eordinal \ A_{27a})}). (((p \ (ap \ (c\_2Eveblen\_2Estrict\_mono \\ A_{27a} \ A_{27a}) \ V0f)) \wedge (p \ (ap \ (c\_2Eveblen\_2Econtinuous \ A_{27a} \ A_{27a}) \\ V0f))) \Rightarrow (p \ (ap \ (c\_2Eveblen\_2Eclub \ A_{27a}) \ (ap \ (ap \ (c\_2Epred\_set\_2EIMAGE \\ (ty\_2Eordinal\_2Eordinal \ A_{27a}) \ (ty\_2Eordinal\_2Eordinal \ A_{27a})) \\ V0f) \ (c\_2Epred\_set\_2EUNIV \ (ty\_2Eordinal\_2Eordinal \ A_{27a}))))))$$