

thm_2Ewellorder_2Eorderlt__trichotomy (TM- NvZ8zNqkpHZ5BDHFTgc8Ny5baBi1eTv7E)

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Definition 1 We define `c_2Emin_2E_40` to be $\lambda A. \lambda P \in 2^A. \text{if } (\exists x \in A. p \text{ (ap } P \ x)) \text{ then (the } (\lambda x. x \in A \wedge p \ x) \text{ of type } \iota \Rightarrow \iota.$

Definition 2 We define `c_2Emin_2E_3D` to be $\lambda A. \lambda x \in A. \lambda y \in A. \text{inj_o } (x = y) \text{ of type } \iota \Rightarrow \iota.$

Definition 3 We define `c_2Ebool_2ET` to be $(\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 4 We define `c_2Ebool_2E_21` to be $\lambda A. \lambda 27a : \iota. (\lambda V0P \in (2^{A-27a}). (\text{ap } (\text{ap } (\text{c_2Emin_2E_3D } (2^{A-27a}))))$

Definition 5 We define `c_2Ecombin_2Eo` to be $\lambda A. \lambda 27a : \iota. \lambda A. \lambda 27b : \iota. \lambda A. \lambda 27c : \iota. \lambda V0f \in (A. 27b^{A-27c}). \lambda V1g$

Definition 6 We define `c_2Emarker_2EAbbrev` to be $\lambda V0x \in 2.V0x.$

Definition 7 We define `c_2Emin_2E_3D_3D_3E` to be $\lambda P \in 2. \lambda Q \in 2. \text{inj_o } (p \Rightarrow q) \text{ of type } \iota.$

Definition 8 We define `c_2Ebool_2E_5C_2F` to be $(\lambda V0t1 \in 2. (\lambda V1t2 \in 2. (\text{ap } (\text{c_2Ebool_2E_21 } 2) (\lambda V2t \in 2.V2t))$

Definition 9 We define `c_2Ebool_2EF` to be $(\text{ap } (\text{c_2Ebool_2E_21 } 2) (\lambda V0t \in 2.V0t)).$

Let `ty_2Epair_2Eprod` : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. \text{nonempty } A0 \Rightarrow \forall A1. \text{nonempty } A1 \Rightarrow \text{nonempty } (\text{ty_2Epair_2Eprod } A0 \ A1) \quad (1)$$

Let `c_2Epred_set_2EGSPEC` : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. \lambda 27a. \text{nonempty } A. \lambda 27a \Rightarrow \forall A. \lambda 27b. \text{nonempty } A. \lambda 27b \Rightarrow \text{c_2Epred_set_2EGSPEC } A. \lambda 27a \ A. \lambda 27b \in ((2^{A-27a})^{(\text{ty_2Epair_2Eprod } A. \lambda 27a \ 2)^{A-27b}}) \quad (2)$$

Let `ty_2Ewellorder_2Ewellorder` : $\iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. \text{nonempty } A0 \Rightarrow \text{nonempty } (\text{ty_2Ewellorder_2Ewellorder } A0) \quad (3)$$

Let `c_2Ewellorder_2Ewellorder__REP` : $\iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A. \lambda 27a. \text{nonempty } A. \lambda 27a \Rightarrow \text{c_2Ewellorder_2Ewellorder__REP } A. \lambda 27a \in ((2^{(\text{ty_2Epair_2Eprod } A. \lambda 27a \ A. \lambda 27a)})^{(\text{ty_2Ewellorder_2Ewellorder } A. \lambda 27a)}) \quad (4)$$

Definition 24 We define $c_2Ewellorder_2Eorderiso$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0w1 \in (ty_2Ewellorder_2E$

Definition 25 We define $c_2Ewellorder_2Eorderlt$ to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0w1 \in (ty_2Ewellorder_2E$

Definition 26 We define $c_2Epred_set_2ESUBSET$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). \lambda V1t \in (2^{A-27a}). (ap$

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty\ ty_2Eone_2Eone \quad (9)$$

Definition 27 We define c_2Eone_2Eone to be $(ap\ (c_2Emin_2E_40\ ty_2Eone_2Eone)\ (\lambda V0x \in ty_2Eone_2E$

Let $ty_2Esum_2Esum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow \forall A1. nonempty\ A1 \Rightarrow nonempty\ (ty_2Esum_2Esum\ A0\ A1) \quad (10)$$

Let $c_2Esum_2EABS_sum : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow \forall A_27b. nonempty\ A_27b \Rightarrow c_2Esum_2EABS_sum\ A_27a\ A_27b \in ((ty_2Esum_2Esum\ A_27a\ A_27b)^{((2^{A-27b})^{A-27a})^2}) \quad (11)$$

Definition 28 We define c_2Esum_2EINR to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27b. (ap\ (c_2Esum_2EABS$

Let $ty_2Eoption_2Eoption : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0. nonempty\ A0 \Rightarrow nonempty\ (ty_2Eoption_2Eoption\ A0) \quad (12)$$

Let $c_2Eoption_2Eoption_ABS : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a. nonempty\ A_27a \Rightarrow c_2Eoption_2Eoption_ABS\ A_27a \in ((ty_2Eoption_2Eoption\ A_27a)^{(ty_2Esum_2Esum\ A_27a\ ty_2Eone_2Eone)}) \quad (13)$$

Definition 29 We define $c_2Eoption_2ENONE$ to be $\lambda A_27a : \iota. (ap\ (c_2Eoption_2Eoption_ABS\ A_27a)\ (c$

Definition 30 We define c_2Esum_2EINL to be $\lambda A_27a : \iota. \lambda A_27b : \iota. \lambda V0e \in A_27a. (ap\ (c_2Esum_2EABS$

Definition 31 We define $c_2Eoption_2ESOME$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. (ap\ (c_2Eoption_2Eoption$

Definition 32 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota. (\lambda V0t \in 2. (\lambda V1t1 \in A_27a. (\lambda V2t2 \in A_27a. ($

Definition 33 We define $c_2Eoption_2ESome$ to be $\lambda A_27a : \iota. \lambda V0P \in (2^{A-27a}). (ap\ (ap\ (ap\ (c_2Ebool_2ECOND$

Definition 34 We define $c_2Ewellorder_2Ewleast$ to be $\lambda A_27a : \iota. \lambda V0w \in (ty_2Ewellorder_2Ewellorder\ A$

Definition 35 We define $c_2Epred_set_2EEMPTY$ to be $\lambda A_27a : \iota. (\lambda V0x \in A_27a. c_2Ebool_2ECOND$

Definition 36 We define $c_2Epred_set_2EINSERT$ to be $\lambda A_27a : \iota. \lambda V0x \in A_27a. \lambda V1s \in (2^{A-27a}). (ap\ (c$

Definition 37 We define $c_2Epred_set_2EDIFF$ to be $\lambda A_27a : \iota. \lambda V0s \in (2^{A-27a}). \lambda V1t \in (2^{A-27a}). (ap\ (c$

Definition 38 We define $c_2Epred_set_2EDELETE$ to be $\lambda A_27a : \iota.\lambda V0s \in (2^{A_27a}).\lambda V1x \in A_27a.(ap (a$
 Let $c_2Eoption_2ETHE : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Eoption_2ETHE A_27a \in (A_27a^{(ty_2Eoption_2Eoption A_27a)}) \quad (14)$$

Definition 39 We define $c_2Epred_set_2EIMAGE$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V1s \in$

Definition 40 We define c_2Ebool_2ELET to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27$

Let $c_2Ebool_2EARB : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Ebool_2EARB A_27a \in A_27a \quad (15)$$

Definition 41 We define $c_2Erelation_2ERESTRICT$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0f \in (A_27b^{A_27a}).\lambda V1$

Definition 42 We define $c_2Erelation_2ETC$ to be $\lambda A_27a : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1a \in A_27a.\lambda V2b$

Definition 43 We define $c_2Erelation_2Eapprox$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1M$

Definition 44 We define $c_2Erelation_2Ethe_fun$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1M$

Definition 45 We define $c_2Erelation_2EWFREC$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0R \in ((2^{A_27a})^{A_27a}).\lambda V1M$

Definition 46 We define $c_2Ewellorder_2Ewo2wo$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0w1 \in (ty_2Ewellorder_2E$

Assume the following.

$$True \quad (16)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (17)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p V0t))) \quad (18)$$

Assume the following.

$$(\forall V0t \in 2.((p V0t) \vee \neg(p V0t))) \quad (19)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0t \in 2.((\exists V1x \in A_27a.(p V0t)) \Leftrightarrow (p V0t))) \quad (20)$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2.(((True \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \wedge True) \Leftrightarrow \\
& (p \ V0t)) \wedge (((False \wedge (p \ V0t)) \Leftrightarrow False) \wedge (((p \ V0t) \wedge False) \Leftrightarrow False) \wedge \\
& (((p \ V0t) \wedge (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \quad (21)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2.(((True \vee (p \ V0t)) \Leftrightarrow True) \wedge (((p \ V0t) \vee True) \Leftrightarrow True) \wedge \\
& (((False \vee (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \vee False) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \vee \\
& (p \ V0t)) \Leftrightarrow (p \ V0t)))))) \quad (22)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2.(((True \Rightarrow (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \Rightarrow True) \Leftrightarrow \\
& True) \wedge (((False \Rightarrow (p \ V0t)) \Leftrightarrow True) \wedge (((p \ V0t) \Rightarrow (p \ V0t)) \Leftrightarrow True) \wedge ((\\
& (p \ V0t) \Rightarrow False) \Leftrightarrow (\neg(p \ V0t)))))) \quad (23)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& ((\forall V0t \in 2.((\neg(\neg(p \ V0t))) \Leftrightarrow (p \ V0t)) \wedge (((\neg True) \Leftrightarrow False) \wedge \\
& ((\neg False) \Leftrightarrow True))) \quad (24)
\end{aligned}$$

Assume the following.

$$\forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0x \in A_27a.(V0x = V0x)) \quad (25)$$

Assume the following.

$$\forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (26)$$

Assume the following.

$$\forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (27)$$

Assume the following.

$$\begin{aligned}
& (\forall V0t \in 2.(((True \Leftrightarrow (p \ V0t)) \Leftrightarrow (p \ V0t)) \wedge (((p \ V0t) \Leftrightarrow True) \Leftrightarrow \\
& (p \ V0t)) \wedge (((False \Leftrightarrow (p \ V0t)) \Leftrightarrow (\neg(p \ V0t))) \wedge (((p \ V0t) \Leftrightarrow False) \Leftrightarrow (\neg(\\
& p \ V0t)))))) \quad (28)
\end{aligned}$$

Assume the following.

$$\forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).((\neg(\forall V1x \in A_27a.(p \ (ap \ V0P \ V1x)))) \Leftrightarrow (\exists V2x \in A_27a.(\neg(p \ (ap \ V0P \ V2x)))))) \quad (29)$$

Assume the following.

$$\forall A_27a.nonempty \ A_27a \Rightarrow (\forall V0P \in (2^{A_27a}).((\neg(\exists V1x \in A_27a.(p \ (ap \ V0P \ V1x)))) \Leftrightarrow (\forall V2x \in A_27a.(\neg(p \ (ap \ V0P \ V2x)))))) \quad (30)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in (2^{A-27a}). ((p V0P) \wedge (\forall V2x \in A.27a. (p (ap V1Q V2x)))))) \Leftrightarrow (\forall V3x \in A.27a. ((p V0P) \wedge (p (ap V1Q V3x)))))) \quad (31)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in (2^{A-27a}). (\forall V1Q \in 2. ((\exists V2x \in A.27a. ((p (ap V0P V2x)) \wedge (p V1Q)))))) \Leftrightarrow ((\exists V3x \in A.27a. (p (ap V0P V3x))) \wedge (p V1Q)))) \quad (32)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in (2^{A-27a}). ((\exists V2x \in A.27a. ((p V0P) \wedge (p (ap V1Q V2x)))))) \Leftrightarrow ((p V0P) \wedge (\exists V3x \in A.27a. (p (ap V1Q V3x)))))) \quad (33)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in (2^{A-27a}). ((\forall V2x \in A.27a. ((p V0P) \vee (p (ap V1Q V2x)))))) \Leftrightarrow ((p V0P) \vee (\forall V3x \in A.27a. (p (ap V1Q V3x)))))) \quad (34)$$

Assume the following.

$$\forall A.27a.nonempty A.27a \Rightarrow (\forall V0P \in (2^{A-27a}). (\forall V1Q \in 2. ((\forall V2x \in A.27a. ((p (ap V0P V2x)) \Rightarrow (p V1Q)))))) \Leftrightarrow ((\exists V3x \in A.27a. (p (ap V0P V3x))) \Rightarrow (p V1Q)))) \quad (35)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. ((\neg((p V0A) \Rightarrow (p V1B)))))) \Leftrightarrow ((p V0A) \wedge (\neg(p V1B)))) \quad (36)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p V0A) \wedge (p V1B)))) \Leftrightarrow ((\neg(p V0A)) \vee (\neg(p V1B)))))) \wedge (((\neg((p V0A) \vee (p V1B)))) \Leftrightarrow ((\neg(p V0A)) \wedge (\neg(p V1B)))))) \quad (37)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (\forall V2C \in 2. (((p V0A) \vee ((p V1B) \wedge (p V2C)))))) \Leftrightarrow (((p V0A) \vee (p V1B)) \wedge ((p V0A) \vee (p V2C)))))) \quad (38)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (\forall V2C \in 2. (((p V1B) \wedge ((p V2C) \vee (p V0A)))))) \Leftrightarrow (((p V1B) \vee (p V0A)) \wedge ((p V2C) \vee (p V0A)))))) \quad (39)$$

Assume the following.

$$(\forall V0A \in 2.(\forall V1B \in 2.(((p V0A) \Rightarrow (p V1B)) \Leftrightarrow ((\neg(p V0A)) \vee (p V1B)))))) \quad (40)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(\forall V2t3 \in 2.(((p V0t1) \Rightarrow ((p V1t2) \Rightarrow (p V2t3))) \Leftrightarrow (((p V0t1) \wedge (p V1t2)) \Rightarrow (p V2t3)))))) \quad (41)$$

Assume the following.

$$(\forall V0x \in 2.(\forall V1x_{.27} \in 2.(\forall V2y \in 2.(\forall V3y_{.27} \in 2.(((p V0x) \Leftrightarrow (p V1x_{.27})) \wedge ((p V1x_{.27}) \Rightarrow ((p V2y) \Leftrightarrow (p V3y_{.27})))))) \Rightarrow (((p V0x) \Rightarrow (p V2y)) \Leftrightarrow ((p V1x_{.27}) \Rightarrow (p V3y_{.27})))))) \quad (42)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0a \in A_{.27a}.(\exists V1x \in A_{.27a}.(V1x = V0a))) \quad (43)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0P \in (2^{A_{.27a}}).(\forall V1a \in A_{.27a}.((\exists V2x \in A_{.27a}.((V2x = V1a) \wedge (p (ap V0P V2x)))) \Leftrightarrow (p (ap V0P V1a)))))) \quad (44)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0f \in (2^{A_{.27a}}).(\forall V1v \in A_{.27a}.((\forall V2x \in A_{.27a}.((V2x = V1v) \Rightarrow (p (ap V0f V2x)))) \Leftrightarrow (p (ap V0f V1v)))))) \quad (45)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow \forall A_{.27b}.nonempty A_{.27b} \Rightarrow \forall A_{.27c}.nonempty A_{.27c} \Rightarrow (\forall V0f \in (A_{.27b}^{A_{.27a}}).(\forall V1g \in (A_{.27a}^{A_{.27c}}).(\forall V2x \in A_{.27c}.((ap (ap (ap (c_{.2}Ecombin_{.2}Eo A_{.27c} A_{.27b} A_{.27a}) V0f) V1g) V2x) = (ap V0f (ap V1g V2x)))))) \quad (46)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0opt \in (ty_{.2}Eoption_{.2}Eoption A_{.27a}).((V0opt = (c_{.2}Eoption_{.2}ENONE A_{.27a})) \vee (\exists V1x \in A_{.27a}.(V0opt = (ap (c_{.2}Eoption_{.2}ESOME A_{.27a}) V1x)))))) \quad (47)$$

Assume the following.

$$\forall A_{.27a}.nonempty A_{.27a} \Rightarrow (\forall V0x \in A_{.27a}.(\forall V1y \in A_{.27a}.(((ap (c_{.2}Eoption_{.2}ESOME A_{.27a}) V0x) = (ap (c_{.2}Eoption_{.2}ESOME A_{.27a}) V1y)) \Leftrightarrow (V0x = V1y)))) \quad (48)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\neg((c_2Eoption_2ENONE\ A_27a) = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x)))) \quad (49)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\neg((ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x) = (c_2Eoption_2ENONE\ A_27a)))) \quad (50)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((ap\ (c_2Eoption_2ETHE\ A_27a)\ (ap\ (c_2Eoption_2ESOME\ A_27a)\ V0x)) = V0x)) \quad (51)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0opt \in (ty_2Eoption_2Eoption\ A_27a). ((\exists V1x \in A_27a. (V0opt = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V1x))) \vee (V0opt = (c_2Eoption_2ENONE\ A_27a)))) \quad (52)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27b. (\forall V2a \in A_27a. (\forall V3b \in A_27b. (((ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V0x)\ V1y) = (ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ A_27b)\ V2a)\ V3b)) \Leftrightarrow ((V0x = V2a) \wedge (V1y = V3b)))))) \quad (53)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0s \in (2^{A_27a}). (\forall V1t \in (2^{A_27a}). ((V0s = V1t) \Leftrightarrow (\forall V2x \in A_27a. ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V2x)\ V0s)) \Leftrightarrow (p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V2x)\ V1t)))))) \quad (54)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\forall V0f \in ((ty_2Epair_2Eprod\ A_27a\ 2)^{A_27b}). (\forall V1v \in A_27a. ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V1v)\ (ap\ (c_2Epred_set_2EGSPEC\ A_27a\ A_27b)\ V0f))) \Leftrightarrow (\exists V2x \in A_27b. ((ap\ (ap\ (c_2Epair_2E_2C\ A_27a\ 2)\ V1v)\ c_2Ebool_2ET) = (ap\ V0f\ V2x)))))) \quad (55)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0s \in (2^{A_27a}). (\forall V1x \in A_27a. (\forall V2y \in A_27a. ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V1x)\ (ap\ (ap\ (c_2Epred_set_2EDELETE\ A_27a)\ V0s)\ V2y))) \Leftrightarrow ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V1x)\ V0s)) \wedge (\neg(V1x = V2y)))))) \quad (56)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \quad \forall V0y \in A_27b. (\forall V1s \in (2^{A_27a}). (\forall V2f \in (A_27b^{A_27a}). \\ & ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27b)\ V0y)\ (ap\ (ap\ (c_2Epred_set_2EIMAGE \\ & \quad A_27a\ A_27b)\ V2f)\ V1s))) \Leftrightarrow (\exists V3x \in A_27a. ((V0y = (ap\ V2f\ V3x)) \wedge \\ & \quad (p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a)\ V3x)\ V1s)))))) \\ & \end{aligned} \tag{57}$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p\ V0t))) \Leftrightarrow (p\ V0t))) \tag{58}$$

Assume the following.

$$(\forall V0A \in 2. ((p\ V0A) \Rightarrow ((\neg(p\ V0A)) \Rightarrow False))) \tag{59}$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & \quad ((p\ V0A) \Rightarrow False) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))) \\ & \end{aligned} \tag{60}$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(\neg(p\ V0A) \vee (p\ V1B))) \Rightarrow False) \Leftrightarrow \\ & \quad ((p\ V0A) \Rightarrow ((\neg(p\ V1B)) \Rightarrow False)))))) \\ & \end{aligned} \tag{61}$$

Assume the following.

$$(\forall V0A \in 2. (((\neg(p\ V0A)) \Rightarrow False) \Rightarrow (((p\ V0A) \Rightarrow False) \Rightarrow False))) \tag{62}$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p\ V0p) \Leftrightarrow (\\ & \quad (p\ V1q) \Leftrightarrow (p\ V2r))) \Leftrightarrow (((p\ V0p) \vee ((p\ V1q) \vee (p\ V2r))) \wedge (((p\ V0p) \vee ((\neg \\ & \quad p\ V2r)) \vee (\neg(p\ V1q)))) \wedge (((p\ V1q) \vee ((\neg(p\ V2r)) \vee (\neg(p\ V0p)))) \wedge ((p\ V2r) \vee \\ & \quad ((\neg(p\ V1q)) \vee (\neg(p\ V0p)))))))))) \\ & \end{aligned} \tag{63}$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p\ V0p) \Leftrightarrow (\\ & \quad (p\ V1q) \wedge (p\ V2r))) \Leftrightarrow (((p\ V0p) \vee ((\neg(p\ V1q)) \vee (\neg(p\ V2r)))) \wedge (((p\ V1q) \vee \\ & \quad (\neg(p\ V0p))) \wedge ((p\ V2r) \vee (\neg(p\ V0p)))))))))) \\ & \end{aligned} \tag{64}$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p\ V0p) \Leftrightarrow (\\ & \quad (p\ V1q) \vee (p\ V2r))) \Leftrightarrow (((p\ V0p) \vee (\neg(p\ V1q))) \wedge (((p\ V0p) \vee (\neg(p\ V2r))) \wedge \\ & \quad ((p\ V1q) \vee ((p\ V2r) \vee (\neg(p\ V0p)))))))))) \\ & \end{aligned} \tag{65}$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee \neg(p V2r))) \wedge (\neg(p V1q)) \vee ((p V2r) \vee \neg(p V0p)))))))) \quad (66)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((p V0p) \Leftrightarrow \neg(p V1q)) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (\neg(p V1q)) \vee \neg(p V0p)))))) \quad (67)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \Rightarrow (p V1q)) \Rightarrow (p V0p)))) \quad (68)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \Rightarrow (p V1q)) \Rightarrow \neg(p V1q)))) \quad (69)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \vee (p V1q)) \Rightarrow \neg(p V0p)))) \quad (70)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (\neg((p V0p) \vee (p V1q)) \Rightarrow \neg(p V1q)))) \quad (71)$$

Assume the following.

$$(\forall V0p \in 2. (\neg(\neg(p V0p)) \Rightarrow (p V0p))) \quad (72)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty A.27a \Rightarrow (\forall V0x \in A.27a. (\forall V1y \in \\ A.27a. (\forall V2w \in (ty_2Ewellorder_2Ewellorder A.27a). ((p \\ (ap (ap (c_2Ebool_2EIN (ty_2Epair_2Eprod A.27a A.27a)) (ap (ap \\ (c_2Epair_2E_2C A.27a A.27a) V0x) V1y)) (ap (c_2Eset_relation_2Estrict \\ A.27a) (ap (c_2Ewellorder_2Ewellorder_REP A.27a) V2w)))) \Rightarrow (\\ (p (ap (ap (c_2Ebool_2EIN A.27a) V0x) (ap (c_2Ewellorder_2EelsOf \\ A.27a) V2w))) \wedge (p (ap (ap (c_2Ebool_2EIN A.27a) V1y) (ap (c_2Ewellorder_2EelsOf \\ A.27a) V2w))))))))) \end{aligned} \quad (73)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty A.27a \Rightarrow (\forall V0w \in (ty_2Ewellorder_2Ewellorder \\ A.27a). (\forall V1x \in A.27a. (\forall V2y \in A.27a. (((p (ap (ap (c_2Ebool_2EIN \\ A.27a) V1x) (ap (c_2Ewellorder_2EelsOf A.27a) V0w))) \wedge (p (ap (ap \\ (c_2Ebool_2EIN A.27a) V2y) (ap (c_2Ewellorder_2EelsOf A.27a) \\ V0w)))) \Rightarrow ((p (ap (ap (c_2Ebool_2EIN (ty_2Epair_2Eprod A.27a A.27a)) \\ (ap (ap (c_2Epair_2E_2C A.27a A.27a) V1x) V2y)) (ap (c_2Eset_relation_2Estrict \\ A.27a) (ap (c_2Ewellorder_2Ewellorder_REP A.27a) V0w)))) \vee (\\ (V1x = V2y) \vee (p (ap (ap (c_2Ebool_2EIN (ty_2Epair_2Eprod A.27a A.27a)) \\ (ap (ap (c_2Epair_2E_2C A.27a A.27a) V2y) V1x)) (ap (c_2Eset_relation_2Estrict \\ A.27a) (ap (c_2Ewellorder_2Ewellorder_REP A.27a) V0w)))))))))) \end{aligned} \quad (74)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0x \in A.27a. (\forall V1w \in \\ (ty_2Ewellorder_2Ewellorder\ A.27a). ((p\ (ap\ (ap\ (c.2Ebool_2EIN \\ (ty_2Epair_2Eprod\ A.27a\ A.27a))\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a \\ A.27a)\ V0x)\ V0x))\ (ap\ (c.2Eset_relation_2Estrict\ A.27a)\ (ap\ (\\ c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V1w)))) \Leftrightarrow False))) \end{aligned} \quad (75)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0x \in A.27a. (\forall V1y \in \\ A.27a. (\forall V2w \in (ty_2Ewellorder_2Ewellorder\ A.27a). (\forall V3z \in \\ A.27a. ((p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a\ A.27a)) \\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V0x)\ V1y))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V2w)))) \wedge (\\ p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a\ A.27a))\ (ap\ (ap \\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V1y)\ V3z))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V2w)))))) \Rightarrow \\ (p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a\ A.27a))\ (ap\ (\\ ap\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V0x)\ V3z))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V2w)))))) \end{aligned} \quad (76)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0x \in A.27a. (\forall V1y \in \\ A.27a. (\forall V2z \in A.27a. (\forall V3w \in (ty_2Ewellorder_2Ewellorder \\ A.27a). ((p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a\ A.27a)) \\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V0x)\ V1y))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ (ap\ (ap\ (c.2Ewellorder_2Ewobound \\ A.27a)\ V2z)\ V3w)))))) \Leftrightarrow ((p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod \\ A.27a\ A.27a))\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V0x)\ V2z))\ (ap \\ (c.2Eset_relation_2Estrict\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP \\ A.27a)\ V3w)))) \wedge ((p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a \\ A.27a))\ (ap\ (ap\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V1y)\ V2z))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V3w)))) \wedge (\\ p\ (ap\ (ap\ (c.2Ebool_2EIN\ (ty_2Epair_2Eprod\ A.27a\ A.27a))\ (ap\ (ap \\ (c.2Epair_2E_2C\ A.27a\ A.27a)\ V0x)\ V1y))\ (ap\ (c.2Eset_relation_2Estrict \\ A.27a)\ (ap\ (c.2Ewellorder_2Ewellorder_REP\ A.27a)\ V3w)))))) \end{aligned} \quad (77)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0x \in A.27a. (\forall V1w \in \\ (ty_2Ewellorder_2Ewellorder\ A.27a). ((ap\ (c_2Ewellorder_2EelsOf \\ A.27a)\ (ap\ (ap\ (c_2Ewellorder_2Ewobound\ A.27a)\ V0x)\ V1w))) = (ap \\ (c_2Epred_set_2EGSPEC\ A.27a\ A.27a)\ (\lambda V2y \in A.27a. (ap\ (ap\ (\\ c_2Epair_2E_2C\ A.27a\ 2)\ V2y)\ (ap\ (ap\ (c_2Ebool_2EIN\ (ty_2Epair_2Eprod \\ A.27a\ A.27a))\ (ap\ (ap\ (c_2Epair_2E_2C\ A.27a\ A.27a)\ V2y)\ V0x)))\ (ap \\ (c_2Eset_relation_2Estrict\ A.27a)\ (ap\ (c_2Ewellorder_2Ewellorder_REP \\ A.27a)\ V1w))))))))) \end{aligned} \quad (78)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow (\\ \forall V0w1 \in (ty_2Ewellorder_2Ewellorder\ A.27a). (\forall V1w2 \in \\ (ty_2Ewellorder_2Ewellorder\ A.27b). ((p\ (ap\ (ap\ (c_2Ewellorder_2Eorderiso \\ A.27a\ A.27b)\ V0w1)\ V1w2)) \Rightarrow (p\ (ap\ (ap\ (c_2Ewellorder_2Eorderiso \\ A.27b\ A.27a)\ V1w2)\ V0w1)))))) \end{aligned} \quad (79)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0w \in (ty_2Ewellorder_2Ewellorder \\ A.27a). (\forall V1s \in (2^{A.27a}). (\forall V2x \in A.27a. (((ap\ (ap \\ (c_2Ewellorder_2Ewleast\ A.27a)\ V0w)\ V1s) = (ap\ (c_2Eoption_2ESOME \\ A.27a)\ V2x)) \Rightarrow ((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A.27a)\ V2x)\ (ap\ (c_2Ewellorder_2EelsOf \\ A.27a)\ V0w))) \wedge ((\neg(p\ (ap\ (ap\ (c_2Ebool_2EIN\ A.27a)\ V2x)\ V1s)))) \wedge \\ (\forall V3y \in A.27a. (((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A.27a)\ V3y)\ (ap \\ (c_2Ewellorder_2EelsOf\ A.27a)\ V0w))) \wedge ((\neg(p\ (ap\ (ap\ (c_2Ebool_2EIN \\ A.27a)\ V3y)\ V1s)))) \wedge (\neg(V2x = V3y)))) \Rightarrow (p\ (ap\ (ap\ (c_2Ebool_2EIN\ (\\ ty_2Epair_2Eprod\ A.27a\ A.27a))\ (ap\ (ap\ (c_2Epair_2E_2C\ A.27a\ A.27a) \\ V2x)\ V3y))\ (ap\ (c_2Eset_relation_2Estrict\ A.27a)\ (ap\ (c_2Ewellorder_2Ewellorder_REP \\ A.27a)\ V0w))))))))) \end{aligned} \quad (80)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow (\forall V0w \in (ty_2Ewellorder_2Ewellorder \\ A.27a). (\forall V1s \in (2^{A.27a}). (((ap\ (ap\ (c_2Ewellorder_2Ewleast \\ A.27a)\ V0w)\ V1s) = (c_2Eoption_2ENONE\ A.27a)) \Rightarrow (p\ (ap\ (ap\ (c_2Epred_set_2ESUBSET \\ A.27a)\ (ap\ (c_2Ewellorder_2EelsOf\ A.27a)\ V0w))\ V1s)))))) \end{aligned} \quad (81)$$

Assume the following.

$$\begin{aligned} \forall A.27a.nonempty\ A.27a \Rightarrow \forall A.27b.nonempty\ A.27b \Rightarrow (\\ \forall V0w1 \in (ty_2Ewellorder_2Ewellorder\ A.27a). (\forall V1w2 \in \\ (ty_2Ewellorder_2Ewellorder\ A.27b). (\forall V2x \in A.27a. (\forall V3y \in \\ A.27b. (((ap\ (ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A.27a\ A.27b)\ V0w1) \\ V1w2)\ V2x) = (ap\ (c_2Eoption_2ESOME\ A.27b)\ V3y)) \Rightarrow (p\ (ap\ (ap\ (c_2Ebool_2EIN \\ A.27b)\ V3y)\ (ap\ (c_2Ewellorder_2EelsOf\ A.27b)\ V1w2))))))))) \end{aligned} \quad (82)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0x1 \in A_27a. (\forall V1w1 \in (ty_2Ewellorder_2Ewellorder \\
& \quad A_27a). (\forall V2x2 \in A_27a. (\forall V3w2 \in (ty_2Ewellorder_2Ewellorder \\
& \quad A_27b). (\forall V4y \in A_27b. (((p\ (ap\ (ap\ (c_2Ebool_2EIN\ A_27a) \\
& \quad V0x1)\ (ap\ (c_2Ewellorder_2EelsOf\ A_27a)\ V1w1))) \wedge ((p\ (ap\ (ap\ (c_2Ebool_2EIN \\
& \quad A_27a)\ V2x2)\ (ap\ (c_2Ewellorder_2EelsOf\ A_27a)\ V1w1))) \wedge ((ap \\
& \quad (ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A_27a\ A_27b)\ V1w1)\ V3w2)\ V0x1) = \\
& \quad (ap\ (c_2Eoption_2ESOME\ A_27b)\ V4y)) \wedge ((ap\ (ap\ (ap\ (c_2Ewellorder_2Ewo2wo \\
& \quad A_27a\ A_27b)\ V1w1)\ V3w2)\ V2x2) = (ap\ (c_2Eoption_2ESOME\ A_27b)\ V4y)))))) \Rightarrow \\
& \quad (V0x1 = V2x2))))))
\end{aligned} \tag{83}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0w1 \in (ty_2Ewellorder_2Ewellorder\ A_27b). (\forall V1w2 \in \\
& \quad (ty_2Ewellorder_2Ewellorder\ A_27a). (\forall V2x0 \in A_27b. (\forall V3y0 \in \\
& \quad A_27a. (\forall V4x \in A_27b. (\forall V5y \in A_27a. (((ap\ (ap\ (ap\ (\\
& \quad c_2Ewellorder_2Ewo2wo\ A_27b\ A_27a)\ V0w1)\ V1w2)\ V2x0) = (ap\ (c_2Eoption_2ESOME \\
& \quad A_27a)\ V3y0)) \wedge ((ap\ (ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A_27b\ A_27a) \\
& \quad V0w1)\ V1w2)\ V4x) = (ap\ (c_2Eoption_2ESOME\ A_27a)\ V5y)) \wedge (p\ (ap\ (ap \\
& \quad (c_2Ebool_2EIN\ (ty_2Epair_2Eprod\ A_27b\ A_27b))\ (ap\ (ap\ (c_2Epair_2E_2C \\
& \quad A_27b\ A_27b)\ V2x0)\ V4x))\ (ap\ (c_2Eset_relation_2Estrict\ A_27b) \\
& \quad (ap\ (c_2Ewellorder_2Ewellorder_REP\ A_27b)\ V0w1)))))) \Rightarrow (p\ (ap \\
& \quad (ap\ (c_2Ebool_2EIN\ (ty_2Epair_2Eprod\ A_27a\ A_27a))\ (ap\ (ap\ (c_2Epair_2E_2C \\
& \quad A_27a\ A_27a)\ V3y0)\ V5y))\ (ap\ (c_2Eset_relation_2Estrict\ A_27a) \\
& \quad (ap\ (c_2Ewellorder_2Ewellorder_REP\ A_27a)\ V1w2))))))
\end{aligned} \tag{84}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0x \in A_27a. (\forall V1w1 \in (ty_2Ewellorder_2Ewellorder \\
& \quad A_27a). (\forall V2w2 \in (ty_2Ewellorder_2Ewellorder\ A_27b). (\\
& \quad \forall V3y \in A_27b. (\forall V4y0 \in A_27b. (((p\ (ap\ (ap\ (c_2Ebool_2EIN \\
& \quad A_27a)\ V0x)\ (ap\ (c_2Ewellorder_2EelsOf\ A_27a)\ V1w1))) \wedge ((ap\ (\\
& \quad ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A_27a\ A_27b)\ V1w1)\ V2w2)\ V0x) = (ap \\
& \quad (c_2Eoption_2ESOME\ A_27b)\ V3y)) \wedge (p\ (ap\ (ap\ (c_2Ebool_2EIN\ (ty_2Epair_2Eprod \\
& \quad A_27b\ A_27b))\ (ap\ (ap\ (c_2Epair_2E_2C\ A_27b\ A_27b)\ V4y0)\ V3y))\ (\\
& \quad ap\ (c_2Eset_relation_2Estrict\ A_27b)\ (ap\ (c_2Ewellorder_2Ewellorder_REP \\
& \quad A_27b)\ V2w2)))))) \Rightarrow (\exists V5x0 \in A_27a. ((p\ (ap\ (ap\ (c_2Ebool_2EIN \\
& \quad A_27a)\ V5x0)\ (ap\ (c_2Ewellorder_2EelsOf\ A_27a)\ V1w1))) \wedge ((ap\ (\\
& \quad ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A_27a\ A_27b)\ V1w1)\ V2w2)\ V5x0) = (\\
& \quad ap\ (c_2Eoption_2ESOME\ A_27b)\ V4y0))))))
\end{aligned} \tag{85}$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0w1 \in (ty_2Ewellorder_2Ewellorder\ A_27b). (\forall V1w2 \in \\
& (ty_2Ewellorder_2Ewellorder\ A_27a). (\forall V2x \in A_27b. (((\\
& ap\ (ap\ (ap\ (c_2Ewellorder_2Ewo2wo\ A_27b\ A_27a)\ V0w1)\ V1w2)\ V2x) = \\
& (c_2Eoption_2ENONE\ A_27a)) \Rightarrow ((ap\ (c_2Ewellorder_2EelsOf\ A_27a) \\
& V1w2) = (ap\ (ap\ (c_2Epred_set_2EIMAGE\ (ty_2Eoption_2Eoption \\
& A_27a)\ A_27a)\ (c_2Eoption_2ETHE\ A_27a))\ (ap\ (ap\ (c_2Epred_set_2EDELETE \\
& (ty_2Eoption_2Eoption\ A_27a))\ (ap\ (ap\ (c_2Epred_set_2EIMAGE \\
& A_27b\ (ty_2Eoption_2Eoption\ A_27a))\ (ap\ (ap\ (c_2Ewellorder_2Ewo2wo \\
& A_27b\ A_27a)\ V0w1)\ V1w2))\ (ap\ (ap\ (c_2Ewellorder_2Eiseg\ A_27b) \\
& V0w1)\ V2x))))\ (c_2Eoption_2ENONE\ A_27a))))))
\end{aligned} \tag{86}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \forall V0w1 \in (ty_2Ewellorder_2Ewellorder\ A_27a). (\forall V1w2 \in \\
& (ty_2Ewellorder_2Ewellorder\ A_27b). ((p\ (ap\ (ap\ (c_2Ewellorder_2Eorderlt \\
& A_27a\ A_27b)\ V0w1)\ V1w2)) \vee ((p\ (ap\ (ap\ (c_2Ewellorder_2Eorderiso \\
& A_27a\ A_27b)\ V0w1)\ V1w2)) \vee (p\ (ap\ (ap\ (c_2Ewellorder_2Eorderlt \\
& A_27b\ A_27a)\ V1w2)\ V0w1))))))
\end{aligned}$$