

thm_2Ewords_2EWORD__ADD_EQ_SUB
(TMGPS2EisGreHt5EhtJ9Zcj3hRHFvXyLdU5)

October 26, 2020

Definition 1 We define $c_2Emin_2E_3D$ to be $\lambda A. \lambda x \in A. \lambda y \in A. inj_o (x = y)$ of type $\iota \rightarrow \iota$.

Definition 2 We define c_Ebool_ET to be $(ap \ (ap \ (c_Emin_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x))$

Definition 3 We define $c_2Ebool_2E_21$ to be $\lambda A._27a : \iota.(\lambda V0P \in (2^A_{-27}a).(\ap (\ap (c_2Emin_2E_3D (2^A_{-27}a) V0P) A) P))$

Definition 4 We define c_2Ebool_2EF to be $(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p\ P \Rightarrow p\ Q)$ of type ι .

Definition 6 We define $c_{\text{Ebool_2E_2F_5C}}$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c_{\text{Ebool_2E_21}})2)(\lambda V2t \in 2.$

Definition 7 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap(c_2Ebool_2E_21 2))(\lambda V2t \in 2.$

Definition 8 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap\ (ap\ c_2Emin_2E_3D_3D_3E\ V0t)\ c_2Ebool_2EF))$

Let $ty_2Efc_{2E}finite_image : \iota \rightarrow \iota$ be given. Assume the following.

$\forall A0.\text{nonempty } A0 \Rightarrow \text{nonempty } (\text{ty_2E } fcp_2E \text{ finite_image } A0)$

$\mathcal{E}bool$ $\mathcal{E}itself : \iota \Rightarrow \iota$ be given. Assume the following

$\forall A0 \text{ nonempty } A0 \Rightarrow \text{nonempty}(\text{tu } 2E\text{bool } 2E\text{itsel})$

Ques 2) Ethical values can be given. Assume the following:

$\forall A, 27_A \text{ nonempty} \wedge A, 27_A \rightarrow_A 2Ebacl, 2Ethba \wedge \exists b : A, 27_A$

Figure 2 *Figure 2* can be given. Among the following

Let $c_2Efcp_2Edimindex : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2Efcp_2Edimindex A_27a \in (\text{ty_2Enum_2Enum}^{(\text{ty_2Ebool_2Eitself } A_27a)}) \quad (5)$$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{(\text{ty_2Enum_2Enum})}) \quad (6)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{(\text{ty_2Enum_2Enum})}) \quad (7)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (\text{ty_2Enum_2Enum}^{\omega}) \quad (8)$$

Definition 9 We define c_2Enum_2ESUC to be $\lambda V0m \in \text{ty_2Enum_2Enum}.(\text{ap } c_2Enum_2EABS_num (V0m))$

Definition 10 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\text{if } (\exists x \in A.p (\text{ap } P x)) \text{ then } (\text{the } (\lambda x.x \in A \wedge p)) \text{ of type } \iota \Rightarrow \iota$.

Definition 11 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(\text{ap } V0P (\text{ap } (c_2Emin_2E_40 (A_27a))))$

Definition 12 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in \text{ty_2Enum_2Enum}.(\lambda V1n \in \text{ty_2Enum_2Enum}.(V1n = m))$

Definition 13 We define $c_2Ebool_2E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(\text{ap } (\text{ap } c_2Ebool_2E_2F_5C (A_27a))))$

Definition 14 We define $c_2Efcp_2Efinit_index$ to be $\lambda A_27a : \iota.(\text{ap } (c_2Emin_2E_40 (A_27a^{(\text{ty_2Enum_2Enum})})))$

Let $\text{ty_2Efcp_2Ecart} : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.\text{nonempty } A0 \Rightarrow \forall A1.\text{nonempty } A1 \Rightarrow \text{nonempty } (\text{ty_2Efcp_2Ecart } A0 A1) \quad (9)$$

Let $c_2Efcp_2Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow \forall A_27b.\text{nonempty } A_27b \Rightarrow c_2Efcp_2Edest_cart A_27a A_27b \in ((A_27a^{(\text{ty_2Efcp_2Efinit_image } A_27b)})^{(\text{ty_2Efcp_2Ecart } A_27a A_27b)}) \quad (10)$$

Definition 15 We define $c_2Efcp_2Efcp_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (\text{ty_2Efcp_2Ecart } A_27a A_27b).(\text{ap } c_2Efcp_2Edest_cart (A_27a A_27b) (V0x))$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (11)$$

Definition 16 We define c_2Enum_2E0 to be $(\text{ap } c_2Enum_2EABS_num c_2Enum_2EZERO_REP)$.

Definition 17 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum_2Enum})^{ty_2Enum_2Enum}) \\ (12)$$

Definition 18 We define $c_2Earthmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earthmetic\ n\ 0)\ V)$

Definition 19 We define `c_2Earthmetic_2ENUMERAL` to be $\lambda V0x \in ty_2Enum_2Enum. V0x$.

Let c_2 be given. Assume the following.

$$c_2Earithmetic_2EE EXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \\ (13)$$

Definition 21 We define c_2EBit_2ESBIT to be $\lambda V0b \in 2.\lambda V1n \in ty_2Enum_2Enum.(ap\ (ap\ (ap\ (ap\ (c_2Ebo$

Let $c_2Esum_num_2ESUM : \iota$ be given. Assume the following.

$$c_2Esum_num_2ESUM \in ((ty_2Enum_2Enum^{(ty_2Enum_2Enum^{ty_2Enum_2Enum^{ty_2Enum_2Enum}})})^{ty_2Enum_2Enum}) \quad (14)$$

Definition 22 We define c_2 as the word $\lambda A. \exists x. \forall w \in (ty.Efcp_2Ecart\ 2\ A). (ap\ (ap\ c\ (x,w))\ (A\ w))$

Let $c_2Ewords_2Edimword : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.\text{nonempty } A_27a \Rightarrow c_2Ewords_2Edimword A_27a \in (\text{ty_2Enum_2Enum}^{(\text{ty_2Ebool_2Eitself } A_27a)})$$

(15)

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum ty_2Enum_2Enum_2Enum) ty_2Enum_2Enum) \\ (16)$$

Definition 23 We define $c_2Earthmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap\ (ap\ c_2Earthmetic\ n\ 0)\ V)$

Let $c_2Earithmetic_2EDIV : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EDIV \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (17)$$

Definition 24 We define $c_2Ebit_2EDIV_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum.$

Let $c.2Earithmetic_2EMOD : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EMOD \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (18)$$

Definition 25 We define $c_2Ebit_2EMOD_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2E$

Definition 26 We define c_2Ebit_2EBITS to be $\lambda V0h \in ty_2Enum$

Definition 27 We define c_2Ebit_2EBIT to be $\lambda V0b \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum. (ap$

Definition 28 We define c_2Efcp_2EFCP to be $\lambda A_27a : \iota. \lambda A_27b : \iota. (\lambda V0g \in (A_27a^{ty_2Enum_2Enum}). (ap$

Definition 29 We define $c_2Ewords_2En2w$ to be $\lambda A_27a : \iota. \lambda V0n \in ty_2Enum_2Enum. (ap (c_2Efcp_2EFC$

Definition 30 We define $c_2Ewords_2Eword_2comp$ to be $\lambda A_27a : \iota. \lambda V0w \in (ty_2Efcp_2Ecart 2 A_27a).$

Definition 31 We define $c_2Ewords_2Eword_add$ to be $\lambda A_27a : \iota. \lambda V0v \in (ty_2Efcp_2Ecart 2 A_27a). \lambda V1$

Definition 32 We define $c_2Ewords_2Eword_sub$ to be $\lambda A_27a : \iota. \lambda V0v \in (ty_2Efcp_2Ecart 2 A_27a). \lambda V1$

Assume the following.

$$True \quad (19)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V1t2) \Leftrightarrow (p V0t1)))))) \quad (20)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Rightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Rightarrow True) \Leftrightarrow True) \wedge (((False \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \Rightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (21)$$

Assume the following.

$$((\forall V0t \in 2. ((\neg(\neg(p V0t)) \Leftrightarrow (p V0t)) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True)))) \quad (22)$$

Assume the following.

$$(\forall V0t \in 2. (((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t))))))) \quad (23)$$

Assume the following.

$$(\forall V0t \in 2. ((\neg(\neg(p V0t)) \Leftrightarrow (p V0t)))) \quad (24)$$

Assume the following.

$$(\forall V0A \in 2. ((p V0A) \Rightarrow ((\neg(p V0A)) \Rightarrow False))) \quad (25)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((\neg(p V0A) \vee (p V1B)) \Rightarrow False) \Leftrightarrow (((p V0A) \Rightarrow False) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))))) \quad (26)$$

Assume the following.

$$(\forall V0A \in 2. (\forall V1B \in 2. (((\neg((\neg(p V0A)) \vee (p V1B))) \Rightarrow False) \Leftrightarrow ((p V0A) \Rightarrow ((\neg(p V1B)) \Rightarrow False)))) \quad (27)$$

Assume the following.

$$(\forall V0A \in 2. (((\neg(p V0A)) \Rightarrow False) \Rightarrow (((p V0A) \Rightarrow False) \Rightarrow False))) \quad (28)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Leftrightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee ((p V1q) \vee (p V2r))) \wedge (((p V0p) \vee ((\neg(p V2r)) \vee (\neg(p V1q)))) \wedge (((p V1q) \vee ((\neg(p V2r)) \vee (\neg(p V0p)))) \wedge ((p V2r) \vee ((\neg(p V1q)) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (29)$$

Assume the following.

$$\begin{aligned} & (\forall V0p \in 2. (\forall V1q \in 2. (\forall V2r \in 2. (((p V0p) \Leftrightarrow (p V1q) \Rightarrow (p V2r))) \Leftrightarrow (((p V0p) \vee (p V1q)) \wedge (((p V0p) \vee (\neg(p V2r))) \wedge (((p V1q) \vee ((\neg(p V2r)) \vee (\neg(p V0p)))) \vee ((p V2r) \vee ((\neg(p V1q)) \vee (\neg(p V0p))))))))))) \end{aligned} \quad (30)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (p V0p)))) \quad (31)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((\neg((p V0p) \Rightarrow (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (32)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V0p)))) \quad (33)$$

Assume the following.

$$(\forall V0p \in 2. (\forall V1q \in 2. (((\neg((p V0p) \vee (p V1q))) \Rightarrow (\neg(p V1q)))) \quad (34)$$

Assume the following.

$$(\forall V0p \in 2. (((\neg(\neg(p V0p))) \Rightarrow (p V0p))) \quad (35)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0v \in (ty_2Efcpc_2Ecart \\ & 2 A_27a). (\forall V1w \in (ty_2Efcpc_2Ecart 2 A_27a). ((ap (ap (c_2Ewords_2Eword_sub \\ & A_27a) (ap (ap (c_2Ewords_2Eword_add A_27a) V0v) V1w) V0v) V1w) = V0v))) \end{aligned} \quad (36)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.\text{nonempty } A_27a \Rightarrow (\forall V0v \in (ty_2Efcpc_2Ecart \\ & 2 A_27a). (\forall V1w \in (ty_2Efcpc_2Ecart 2 A_27a). ((ap (ap (c_2Ewords_2Eword_add \\ & A_27a) (ap (ap (c_2Ewords_2Eword_sub A_27a) V0v) V1w) V0v) V1w) = V0v))) \end{aligned} \quad (37)$$

Theorem 1

$$\begin{aligned} \forall A_27a.\text{nonempty } A_27a \Rightarrow & (\forall V0v \in (ty_2Efc_2Ecart \\ & 2 A_27a).(\forall V1w \in (ty_2Efc_2Ecart 2 A_27a).(\forall V2x \in \\ & (ty_2Efc_2Ecart 2 A_27a).(((ap (ap (c_2Ewords_2Eword_add \\ & A_27a) V0v) V1w) = V2x) \Leftrightarrow (V0v = (ap (ap (c_2Ewords_2Eword_sub A_27a) \\ & V2x) V1w))))))) \end{aligned}$$