

thm_2Ewords_2EWORD__ADD__LEFT__LO2
 (TMZJKRoKnQyXDS-
 BuM1Rnq8TmNZ54LbLE4cB)

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Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty\ ty_2Enum_2Enum \quad (1)$$

Definition 1 We define c_2Emin_2E3D to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 2 We define c_2Ebool_2E2T to be $(ap (ap (c_2Emin_2E3D (2^2)) (\lambda V0x \in 2.V0x)) (\lambda V1x \in 2.V1x))$

Definition 3 We define c_2Ebool_2E21 to be $\lambda A.\lambda 27a : \iota.(\lambda V0P \in (2^{A-27a}).(ap (ap (c_2Emin_2E3D (2^{A-27a}))$

Definition 4 We define c_2Ebool_2E2F to be $(ap (c_2Ebool_2E21 2) (\lambda V0t \in 2.V0t))$.

Definition 5 We define $c_2Emin_2E3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \Rightarrow q)$ of type ι .

Definition 6 We define $c_2Ebool_2EBOUNDED$ to be $(\lambda V0v \in 2.c_2Ebool_2E2T)$.

Definition 7 We define $c_2Ecombin_2EK$ to be $\lambda A.\lambda 27a : \iota.\lambda A.\lambda 27b : \iota.(\lambda V0x \in A.\lambda V1y \in A.\lambda V2z \in A.27a.27b.V0x)$

Definition 8 We define $c_2Ecombin_2ES$ to be $\lambda A.\lambda 27a : \iota.\lambda A.\lambda 27b : \iota.\lambda A.\lambda 27c : \iota.(\lambda V0f \in ((A.\lambda 27c^{A-27b})^{A-27a})$

Definition 9 We define $c_2Ecombin_2EI$ to be $\lambda A.\lambda 27a : \iota.(ap (ap (c_2Ecombin_2ES A.\lambda 27a (A.\lambda 27a^{A-27a}) A.\lambda 27a$

Let $ty_2EfcP_2Efinite_image : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2EfcP_2Efinite_image\ A0) \quad (2)$$

Let $ty_2Ebool_2Eitself : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_2Ebool_2Eitself\ A0) \quad (3)$$

Let $c_2Ebool_2Ethe_value : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A.\lambda 27a.nonempty\ A.\lambda 27a \Rightarrow c_2Ebool_2Ethe_value\ A.\lambda 27a \in (ty_2Ebool_2Eitself\ A.\lambda 27a) \quad (4)$$

Let $c_2Efc_2Edimindex : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Efc_2Edimindex\ A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself\ A_27a)}) \quad (5)$$

Definition 10 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap\ (ap\ c_2Emin_2E_3D_3D_3E\ V0t)\ c_2Ebool_2E_7E))$

Definition 11 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ (\lambda V2t \in 2.(ap\ (c_2Ebool_2E_21\ 2)\ V2t)\ V2t)\ V1t2)\ V0t1))$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (omega^{ty_2Enum_2Enum}) \quad (6)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (omega^{omega}) \quad (7)$$

Let $c_2Enum_2EABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EABS_num \in (ty_2Enum_2Enum^{omega}) \quad (8)$$

Definition 12 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap\ c_2Enum_2EABS_num\ m)$

Definition 13 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\mathbf{if}\ (\exists x \in A.p\ (ap\ P\ x))\ \mathbf{then}\ (the\ (\lambda x.x \in A \wedge P\ x))\ \mathbf{of\ type}\ \iota \Rightarrow \iota$.

Definition 14 We define $c_2Ebool_2E_3F$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ V0P\ (ap\ (c_2Emin_2E_40\ A_27a)\ V0P)))$

Definition 15 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap\ (c_2Eprim_rec_2E_3C\ V0m)\ V1n)$

Definition 16 We define $c_2Ebool_2E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ (ap\ c_2Ebool_2E_2F_5C\ A_27a)\ V0P)))$

Definition 17 We define $c_2Efc_2Efinite_index$ to be $\lambda A_27a : \iota.(ap\ (c_2Emin_2E_40\ A_27a)\ (ty_2Enum_2Enum\ A_27a))$

Let $ty_2Efc_2Ecart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_2Efc_2Ecart\ A0\ A1) \quad (9)$$

Let $c_2Efc_2Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_2Efc_2Edest_cart\ A_27a\ A_27b \in ((A_27a^{(ty_2Efc_2Efinite_image\ A_27b)})^{(ty_2Efc_2Ecart\ A_27a\ A_27b)}) \quad (10)$$

Definition 18 We define $c_2Efc_2Efc_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (ty_2Efc_2Ecart\ A_27a\ A_27b)$

Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in omega \quad (11)$$

Definition 19 We define c_2Enum_2E0 to be $(ap\ c_2Enum_2EABS_num\ c_2Enum_2EZERO_REP)$.

Definition 20 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (12)$$

Definition 21 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2E_2B))$.

Definition 22 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_2Earithmetic_2EEXP : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EEXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (13)$$

Definition 23 We define c_2Ebool_2ECOND to be $\lambda A_27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A_27a.(\lambda V2t2 \in A_27a.(ap (ap c_2Ebool_2ECOND)))))$.

Definition 24 We define c_2Ebit_2ESBIT to be $\lambda V0b \in 2.\lambda V1n \in ty_2Enum_2Enum.(ap (ap (ap (c_2Ebool_2ESBIT))))$.

Let $c_2Esum_num_2ESUM : \iota$ be given. Assume the following.

$$c_2Esum_num_2ESUM \in ((ty_2Enum_2Enum^{(ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}}))^{ty_2Enum_2Enum} \quad (14)$$

Definition 25 We define $c_2Ewords_2Ew2n$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2EfcP_2Ecart\ 2\ A_27a).(ap (ap c_2Ewords_2Ew2n))$.

Let $c_2Earithmetic_2E_2D : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2D \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (15)$$

Definition 26 We define c_2Ebool_2ELET to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27a.(ap (ap c_2Ebool_2ELET))))$.

Let $c_2Ewords_2Edimword : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow c_2Ewords_2Edimword\ A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself\ A_27a)})^{ty_2Enum_2Enum} \quad (16)$$

Definition 27 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT2))$.

Let $c_2Earithmetic_2EDIV : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EDIV \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (17)$$

Definition 28 We define $c_2Ebit_2EDIV_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap (ap c_2Ebit_2EDIV_2EXP))$.

Let $c_2Earithmetic_2EMOD : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EMOD \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (18)$$

Definition 29 We define $c_2Ebit_2EMOD_2EXP$ to be $\lambda V0x \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum$

Definition 30 We define c_2Ebit_2EBITS to be $\lambda V0h \in ty_2Enum_2Enum.\lambda V1l \in ty_2Enum_2Enum.\lambda V$

Definition 31 We define c_2Ebit_2EBIT to be $\lambda V0b \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.(ap$

Definition 32 We define c_2Efcpc_2EFCP to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0g \in (A_27a^{ty_2Enum_2Enum}).(ap$

Definition 33 We define $c_2Ewords_2En2w$ to be $\lambda A_27a : \iota.\lambda V0n \in ty_2Enum_2Enum.(ap (c_2Efcpc_2EFC$

Definition 34 We define $c_2Ewords_2Eword_2comp$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efcpc_2Ecart 2 A_27a).$

Definition 35 We define $c_2Ewords_2Eword_2msb$ to be $\lambda A_27a : \iota.\lambda V0w \in (ty_2Efcpc_2Ecart 2 A_27a).(ap$

Definition 36 We define $c_2Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap (c_2Ebool_2E_21 2) (\lambda V2t \in$

Let $ty_2Epair_2Eprod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow \forall A1.nonempty A1 \Rightarrow nonempty (ty_2Epair_2Eprod A0 A1) \quad (19)$$

Let $c_2Epair_2EABS_prod : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2EABS_prod A_27a A_27b \in ((ty_2Epair_2Eprod A_27a A_27b)^{(2^{A_27b})^{A_27a}}) \quad (20)$$

Definition 37 We define $c_2Epair_2E_2C$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in A_27a.\lambda V1y \in A_27b.(ap (c_2$

Definition 38 We define $c_2Ewords_2Enzcv$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Efcpc_2Ecart 2 A_27a).\lambda V1b \in ($

Let $c_2Epair_2ESND : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2ESND A_27a A_27b \in (A_27b^{(ty_2Epair_2Eprod A_27a A_27b)}) \quad (21)$$

Let $c_2Epair_2EFST : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow c_2Epair_2EFST A_27a A_27b \in (A_27a^{(ty_2Epair_2Eprod A_27a A_27b)}) \quad (22)$$

Definition 39 We define $c_2Epair_2EUNCURRY$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda A_27c : \iota.\lambda V0f \in ((A_27c^{A_27$

Definition 40 We define $c_2Ewords_2Eword_2ls$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Efcpc_2Ecart 2 A_27a).\lambda V1b$

Definition 41 We define $c_2Ewords_2Eword_2add$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_2Efcpc_2Ecart 2 A_27a).\lambda V$

Definition 42 We define $c_2Ewords_2Eword_2lo$ to be $\lambda A_27a : \iota.\lambda V0a \in (ty_2Efcpc_2Ecart 2 A_27a).\lambda V1b$

Assume the following.

$$(\forall V0c \in ty_2Enum_2Enum.((ap (ap c_2Earithmetric_2E_2D V0c) V0c) = c_2Enum_2E0)) \quad (23)$$

Assume the following.

$$True \quad (24)$$

Assume the following.

$$(\forall V0t1 \in 2.(\forall V1t2 \in 2.(((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (25)$$

Assume the following.

$$(\forall V0t \in 2.(False \Rightarrow (p V0t))) \quad (26)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow \forall A_27b.nonempty A_27b \Rightarrow (\forall V0f \in (A_27b^{A_27a}).(\forall V1x \in A_27a.((ap (ap (c_2Ebool_2ELET A_27a A_27b) V0f) V1x) = (ap V0f V1x)))) \quad (27)$$

Assume the following.

$$(\forall V0t \in 2.(((True \vee (p V0t)) \Leftrightarrow True) \wedge (((p V0t) \vee True) \Leftrightarrow True) \wedge (((False \vee (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee False) \Leftrightarrow (p V0t)) \wedge (((p V0t) \vee (p V0t)) \Leftrightarrow (p V0t)))))) \quad (28)$$

Assume the following.

$$((\forall V0t \in 2.((\neg(\neg(p V0t))) \Leftrightarrow (p V0t)) \wedge (((\neg True) \Leftrightarrow False) \wedge ((\neg False) \Leftrightarrow True)))) \quad (29)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.((V0x = V0x) \Leftrightarrow True)) \quad (30)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a.(\forall V1y \in A_27a.((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (31)$$

Assume the following.

$$(\forall V0t \in 2.(((True \Leftrightarrow (p V0t)) \Leftrightarrow (p V0t)) \wedge (((p V0t) \Leftrightarrow True) \Leftrightarrow (p V0t)) \wedge (((False \Leftrightarrow (p V0t)) \Leftrightarrow (\neg(p V0t))) \wedge (((p V0t) \Leftrightarrow False) \Leftrightarrow (\neg(p V0t)))))) \quad (32)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t1 \in A_27a. (\forall V1t2 \in \\ A_27a. (((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a)\ c_2Ebool_2ET)\ V0t1) \\ V1t2) = V0t1) \wedge ((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a)\ c_2Ebool_2EF \\ V0t1)\ V1t2) = V1t2)))))) \end{aligned} \quad (33)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow \\ ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \quad (34)$$

Assume the following.

$$\begin{aligned} (\forall V0P \in 2. (\forall V1P_27 \in 2. (\forall V2Q \in 2. (\forall V3Q_27 \in \\ 2. (((p\ V2Q) \Rightarrow ((p\ V0P) \Leftrightarrow (p\ V1P_27))) \wedge ((p\ V1P_27) \Rightarrow ((p\ V2Q) \Leftrightarrow (p\ V3Q_27)))))) \Rightarrow \\ (((p\ V0P) \wedge (p\ V2Q)) \Leftrightarrow ((p\ V1P_27) \wedge (p\ V3Q_27)))))) \end{aligned} \quad (35)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0P \in 2. (\forall V1Q \in 2. \\ (\forall V2x \in A_27a. (\forall V3x_27 \in A_27a. (\forall V4y \in A_27a. \\ (\forall V5y_27 \in A_27a. (((p\ V0P) \Leftrightarrow (p\ V1Q)) \wedge ((p\ V1Q) \Rightarrow (V2x = V3x_27)) \wedge \\ ((\neg(p\ V1Q)) \Rightarrow (V4y = V5y_27)))))) \Rightarrow ((ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a) \\ V0P)\ V2x)\ V4y) = (ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ A_27a)\ V1Q)\ V3x_27 \\ V5y_27))))))))) \end{aligned} \quad (36)$$

Assume the following.

$$(\forall V0v \in 2. ((p\ (ap\ c_2Ebool_2EBOUNDED\ V0v)) \Leftrightarrow True)) \quad (37)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((ap\ (c_2Ecombin_2EI \\ A_27a)\ V0x) = V0x)) \quad (38)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow ((\forall V0w \in (ty_2Efc_2Ecart \\ 2\ A_27a). ((ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ V0w)\ (ap\ (c_2Ewords_2En2w \\ A_27a)\ c_2Enum_2E0)) = V0w)) \wedge (\forall V1w \in (ty_2Efc_2Ecart\ 2 \\ A_27a). ((ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ (ap\ (c_2Ewords_2En2w \\ A_27a)\ c_2Enum_2E0))\ V1w) = V1w))) \end{aligned} \quad (39)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0w \in (ty_2Efc_2Ecart \\ 2\ A_27a). (\forall V1v \in (ty_2Efc_2Ecart\ 2\ A_27a). (((ap\ (c_2Ewords_2Eword_2comp \\ A_27a)\ V1v) = V0w) \Leftrightarrow (V1v = (ap\ (c_2Ewords_2Eword_2comp\ A_27a)\ V0w)))))) \end{aligned} \quad (40)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0a \in (ty_2EfcP_2Ecart \\ & 2\ A_27a).(\forall V1b \in (ty_2EfcP_2Ecart\ 2\ A_27a).((p\ (ap\ (ap \\ & (c_2Ewords_2Eword_ls\ A_27a)\ V0a)\ V1b)) \Leftrightarrow ((p\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\ & A_27a)\ V0a)\ V1b)) \vee (V0a = V1b)))))) \end{aligned} \quad (41)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0a \in (ty_2EfcP_2Ecart \\ & 2\ A_27a).(p\ (ap\ (ap\ (c_2Ewords_2Eword_ls\ A_27a)\ V0a)\ V0a))) \end{aligned} \quad (42)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0b \in (ty_2EfcP_2Ecart \\ & 2\ A_27a).(\forall V1c \in (ty_2EfcP_2Ecart\ 2\ A_27a).(\forall V2a \in \\ & (ty_2EfcP_2Ecart\ 2\ A_27a).((p\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\ & A_27a)\ (ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ V2a)\ V0b))\ V1c)) \Leftrightarrow \\ & (p\ (ap\ (ap\ (ap\ (c_2Ebool_2ECOND\ 2)\ (ap\ (ap\ (c_2Ewords_2Eword_ls \\ & A_27a)\ V0b)\ V1c))\ (ap\ (ap\ (c_2Ebool_2ELET\ (ty_2EfcP_2Ecart\ 2\ A_27a) \\ & 2)\ (\lambda V3x \in (ty_2EfcP_2Ecart\ 2\ A_27a).(ap\ (ap\ c_2Ebool_2E_5C_2F \\ & (ap\ (ap\ (c_2Ewords_2Eword_lo\ A_27a)\ V2a)\ V3x))\ (ap\ (ap\ c_2Ebool_2E_2F_5C \\ & (ap\ c_2Ebool_2E_7E\ (ap\ (ap\ (c_2Emin_2E_3D\ (ty_2EfcP_2Ecart\ 2 \\ & A_27a))\ V0b)\ (ap\ (c_2Ewords_2En2w\ A_27a)\ c_2Enum_2E0))))))\ (ap\ (\\ & ap\ (c_2Ewords_2Eword_ls\ A_27a)\ (ap\ (ap\ (c_2Ewords_2Eword_add \\ & A_27a)\ (ap\ (c_2Ewords_2Eword_2comp\ A_27a)\ V1c))\ V3x))\ V2a)))))) \\ & (ap\ (c_2Ewords_2En2w\ A_27a)\ (ap\ (ap\ c_2Earithmetic_2E_2D\ (ap\ (\\ & c_2Ewords_2Ew2n\ A_27a)\ V1c))\ (ap\ (c_2Ewords_2Ew2n\ A_27a)\ V0b)))))) \\ & (ap\ (ap\ c_2Ebool_2E_2F_5C\ (ap\ (ap\ (c_2Ewords_2Eword_ls\ A_27a) \\ & (ap\ (c_2Ewords_2Eword_2comp\ A_27a)\ V0b))\ V2a))\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\ & A_27a)\ V2a)\ (ap\ (ap\ (c_2Ewords_2Eword_add\ A_27a)\ (ap\ (c_2Ewords_2Eword_2comp \\ & A_27a)\ V0b))\ V1c))))))))) \end{aligned} \quad (43)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0a \in (ty_2EfcP_2Ecart \\ & 2\ A_27a).(\forall V1b \in (ty_2EfcP_2Ecart\ 2\ A_27a).((p\ (ap\ (ap \\ & (c_2Ewords_2Eword_lo\ A_27a)\ (ap\ (c_2Ewords_2Eword_2comp\ A_27a) \\ & V0a))\ V1b)) \Leftrightarrow ((\neg(V1b = (ap\ (c_2Ewords_2En2w\ A_27a)\ c_2Enum_2E0))) \wedge \\ & ((V0a = (ap\ (c_2Ewords_2En2w\ A_27a)\ c_2Enum_2E0)) \vee (p\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\ & A_27a)\ (ap\ (c_2Ewords_2Eword_2comp\ A_27a)\ V1b))\ V0a)))))) \end{aligned} \quad (44)$$

Assume the following.

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow \forall A_{.27b}.nonempty\ A_{.27b} \Rightarrow (\\
& (\forall V0n \in (ty_2EfcP_2Ecart\ 2\ A_{.27a}).((p\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\
& A_{.27a})\ (ap\ (c_2Ewords_2En2w\ A_{.27a})\ c_2Enum_2E0))\ V0n)) \Leftrightarrow (\neg(V0n = \\
& (ap\ (c_2Ewords_2En2w\ A_{.27a})\ c_2Enum_2E0)))))) \wedge (\forall V1n \in (\\
& ty_2EfcP_2Ecart\ 2\ A_{.27b}).(\neg(p\ (ap\ (ap\ (c_2Ewords_2Eword_lo \\
& A_{.27b})\ V1n)\ (ap\ (c_2Ewords_2En2w\ A_{.27b})\ c_2Enum_2E0))))))
\end{aligned} \tag{45}$$

Theorem 1

$$\begin{aligned}
& \forall A_{.27a}.nonempty\ A_{.27a} \Rightarrow (\forall V0c \in (ty_2EfcP_2Ecart \\
& 2\ A_{.27a}).(\forall V1a \in (ty_2EfcP_2Ecart\ 2\ A_{.27a}).((p\ (ap\ (ap \\
& (c_2Ewords_2Eword_lo\ A_{.27a})\ (ap\ (ap\ (c_2Ewords_2Eword_add \\
& A_{.27a})\ V0c)\ V1a))\ V1a)) \Leftrightarrow ((\neg(V1a = (ap\ (c_2Ewords_2En2w\ A_{.27a})\ c_2Enum_2E0))) \wedge \\
& (((\neg(V0c = (ap\ (c_2Ewords_2En2w\ A_{.27a})\ c_2Enum_2E0))) \wedge (p\ (ap\ (\\
& ap\ (c_2Ewords_2Eword_lo\ A_{.27a})\ (ap\ (c_2Ewords_2Eword_2comp \\
& A_{.27a})\ V0c))\ V1a))) \vee (V1a = (ap\ (c_2Ewords_2Eword_2comp\ A_{.27a}) \\
& V0c))))))
\end{aligned}$$