

thm_2Ewords_2Edimword_2 (TMH- baM3ztxKTT1jV75fwt5WHcrgTuFYTLNd)

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Definition 1 We define $c_2Emin_2E_3D_3D_3E$ to be $\lambda P \in 2.\lambda Q \in 2.inj_o (p \ P \Rightarrow p \ Q)$ of type ι .

Let $ty_2Enum_2Enum : \iota$ be given. Assume the following.

$$nonempty \ ty_2Enum_2Enum \quad (1)$$

Definition 2 We define $c_2Emin_2E_3D$ to be $\lambda A.\lambda x \in A.\lambda y \in A.inj_o (x = y)$ of type $\iota \Rightarrow \iota$.

Definition 3 We define c_2Ebool_2ET to be $(ap \ (ap \ (c_2Emin_2E_3D \ (2^2)) \ (\lambda V0x \in 2.V0x)) \ (\lambda V1x \in 2.V1x))$

Definition 4 We define $c_2Ebool_2E_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap \ (ap \ (c_2Emin_2E_3D \ (2^{A_27a})) \ (\lambda V1x \in 2.V1x)) \ (\lambda V2x \in 2.V2x)))$

Definition 5 We define c_2Ebool_2EF to be $(ap \ (c_2Ebool_2E_21 \ 2) \ (\lambda V0t \in 2.V0t))$.

Definition 6 We define $c_2Ebool_2E_7E$ to be $(\lambda V0t \in 2.(ap \ (ap \ c_2Emin_2E_3D_3D_3E \ V0t) \ c_2Ebool_2EF))$

Definition 7 We define $c_2Ebool_2E_2F_5C$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap \ (c_2Ebool_2E_21 \ 2) \ (\lambda V2t \in 2.V2t))))$

Let $c_2Enum_2EREP_num : \iota$ be given. Assume the following.

$$c_2Enum_2EREP_num \in (\omega^{ty_2Enum_2Enum}) \quad (2)$$

Let $c_2Enum_2ESUC_REP : \iota$ be given. Assume the following.

$$c_2Enum_2ESUC_REP \in (\omega^{\omega}) \quad (3)$$

Let $c_2Enum_2EAABS_num : \iota$ be given. Assume the following.

$$c_2Enum_2EAABS_num \in (ty_2Enum_2Enum^{\omega}) \quad (4)$$

Definition 8 We define c_2Enum_2ESUC to be $\lambda V0m \in ty_2Enum_2Enum.(ap \ c_2Enum_2EAABS_num \ m)$

Definition 9 We define $c_2Emin_2E_40$ to be $\lambda A.\lambda P \in 2^A.\text{if } (\exists x \in A.p \ (ap \ P \ x)) \ \text{then } (\text{the } (\lambda x.x \in A \wedge p \ x)) \ \text{else } (\lambda x.x \in A \wedge \neg p \ x)$ of type $\iota \Rightarrow \iota$.

Definition 10 We define $c_2Eb0_2E_3F$ to be $\lambda A_{27a} : \iota.(\lambda V0P \in (2^{A_27a}).(ap_{V0P}_{(ap_{(c_2Emin_2E_40$

Definition 11 We define $c_2Eprim_rec_2E_3C$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.$

Definition 12 We define $c_2Earthmetic_2E_3E$ to be $\lambda V0m \in ty_2Enum_2Enum. \lambda V1n \in ty_2Enum_2Enum.$

Definition 13 We define $c_Ebool_2E_5C_2F$ to be $(\lambda V0t1 \in 2.(\lambda V1t2 \in 2.(ap\ (c_Ebool_2E_21\ 2)\ (\lambda V2t \in$

Definition 14 We define $c_2Earthmetic_2E_3E_3D$ to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.$

Definition 15 We define c_2 Earthmetic_2E_3C_3D to be $\lambda V0m \in ty_2Enum_2Enum.\lambda V1n \in ty_2Enum_2Enum.$

Let $c_2\text{Earithmetic_2EXP} : \iota$ be given. Assume the following.

$c_2Earithmetic_2EEEXP \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^*$

Let c_2 be given. Assume the following.

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Let $c_2Enum_2EZERO_REP : \iota$ be given. Assume the following.

$$c_2Enum_2EZERO_REP \in \omega \quad (7)$$

Definition 16 We define c_2Enum_2E0 to be (ap $c_2Enum_2EABS_num c_2Enum_2EZERO_REP$).

Definition 17 We define $c_2Enumeral_2EiiSUC$ to be $\lambda V0n\in ty_2Enum_2Enum.(ap\ c_2Enum_2ESUC\ (ap$

Let $c_2E\text{arithmetic}_2E\text{EVEN} : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EEVEN \in (2^{ty_2Enum_2Enum}) \quad (8)$$

Let $c_2\text{Enumeral}_2Eonecount : \iota$ be given. Assume the following.

$$c_2Enumeral_2Eonecount \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum})^{ty_2Enum_2Enum} \quad (9)$$

Let $c_2\text{Enumeral}_2Eexactlog : \iota$ be given. Assume the following.

$$c_2Enumeral_2Eexactlog \in (ty_2Enum_2Enum^{ty_2Enum_2Enum}) \quad (10)$$

Definition 18 We define c_2Ebool_2ECOND to be $\lambda A._27a : \iota.(\lambda V0t \in 2.(\lambda V1t1 \in A._27a.(\lambda V2t2 \in A._27a.($

Definition 19 We define $c_2Eprim_rec_2EPRE$ to be $\lambda V0m \in ty_2Enum_2Enum.(ap (ap (ap (ap (c_2EBool_2E$

Definition 20 We define $c_2Earithmetic_2EZERO$ to be c_2Enum_2E0 .

Let $c_2Earithmetic_2E_2B : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2B \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (11)$$

Definition 21 We define $c_2Earithmetic_2EBIT2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EBIT1 n))$

Definition 22 We define $c_2Earithmetic_2ENUMERAL$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Let $c_2Earithmetic_2EDIV : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EDIV \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (12)$$

Definition 23 We define $c_2Earithmetic_2EDIV2$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EDIV n))$

Let $c_2Enumeral_2Etexp_help : \iota$ be given. Assume the following.

$$c_2Enumeral_2Etexp_help \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (13)$$

Let $c_2Earithmetic_2EODD : \iota$ be given. Assume the following.

$$c_2Earithmetic_2EODD \in (2^{ty_2Enum_2Enum}) \quad (14)$$

Definition 24 We define c_2Ebool_2ELET to be $\lambda A_27a : \iota. \lambda A_27b : \iota. (\lambda V0f \in (A_27b^{A_27a}).(\lambda V1x \in A_27b.f(x)))$

Definition 25 We define $c_2Enumeral_2EiDUB$ to be $\lambda V0x \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EODD x))$

Definition 26 We define $c_2Enumeral_2EiZ$ to be $\lambda V0x \in ty_2Enum_2Enum.V0x$.

Definition 27 We define $c_2Earithmetic_2EBIT1$ to be $\lambda V0n \in ty_2Enum_2Enum.(ap (ap c_2Earithmetic_2EODD n))$

Let $c_2Earithmetic_2E_2A : \iota$ be given. Assume the following.

$$c_2Earithmetic_2E_2A \in ((ty_2Enum_2Enum^{ty_2Enum_2Enum})^{ty_2Enum_2Enum}) \quad (15)$$

Definition 28 We define $c_2Enumeral_2Einternal_mult$ to be $c_2Earithmetic_2E_2A$.

Let $ty_2Ebool_2Eitself : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty A0 \Rightarrow nonempty (ty_2Ebool_2Eitself A0) \quad (16)$$

Let $c_2Ewords_2Edimword : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Ewords_2Edimword A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself A_27a)}) \quad (17)$$

Let $c_2Ebool_2Ethet_value : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Ebool_2Ethet_value A_27a \in (ty_2Ebool_2Eitself A_27a) \quad (18)$$

Let $ty_2Eone_2Eone : \iota$ be given. Assume the following.

$$nonempty ty_2Eone_2Eone \quad (19)$$

Let $ty_2Efcp_2Ebit0 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_0.nonempty A_0 \Rightarrow nonempty (ty_2Efcp_2Ebit0 A_0) \quad (20)$$

Let $c_2Ewords_2EINT_MIN : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow c_2Ewords_2EINT_MIN A_27a \in (ty_2Enum_2Enum^{(ty_2Ebool_2Eitself A_27a)}) \quad (21)$$

Assume the following.

$$(\forall V0t1 \in 2. (\forall V1t2 \in 2. (((p V0t1) \Rightarrow (p V1t2)) \Rightarrow (((p V1t2) \Rightarrow (p V0t1)) \Rightarrow ((p V0t1) \Leftrightarrow (p V1t2)))))) \quad (22)$$

Assume the following.

$$(\forall V0t \in 2. (False \Rightarrow (p V0t))) \quad (23)$$

Assume the following.

$$\forall A_27a.nonempty A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (24)$$

Assume the following.

$$\begin{aligned} \forall A_27a.nonempty A_27a \Rightarrow & (\forall V0t1 \in A_27a. (\forall V1t2 \in \\ & A_27a. (((ap (ap (ap (c_2Ebool_2ECOND A_27a) c_2Ebool_2ET) V0t1) \\ & V1t2) = V0t1) \wedge ((ap (ap (ap (c_2Ebool_2ECOND A_27a) c_2Ebool_2EF) \\ & V0t1) V1t2) = V1t2)))))) \end{aligned} \quad (25)$$

Assume the following.

$((\forall V0n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B c_2Enum_2E0) V0n) = V0n)) \wedge ((\forall V1n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B V1n) c_2Enum_2E0) = V1n)) \wedge ((\forall V2n \in ty_2Enum_2Enum.(\forall V3m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2B ap c_2Earithmetic_2ENUMERAL V2n)) (ap c_2Earithmetic_2ENUMERAL V3m)) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Enum_2EiZ (ap (ap c_2Earithmetic_2E_2B V2n) V3m))))))) \wedge ((\forall V4n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A c_2Enum_2E0) V4n) = c_2Enum_2E0)) \wedge ((\forall V5n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A V5n) c_2Enum_2E0) = c_2Enum_2E0)) \wedge ((\forall V6n \in ty_2Enum_2Enum.((\forall V7m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2A (ap c_2Earithmetic_2ENUMERAL V6n)) (ap c_2Earithmetic_2ENUMERAL V7m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2A V6n) V7m))))))) \wedge ((\forall V8n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D c_2Enum_2E0) V8n) = c_2Enum_2E0)) \wedge ((\forall V9n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D V9n) c_2Enum_2E0) = V9n)) \wedge ((\forall V10n \in ty_2Enum_2Enum.(\forall V11m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2E_2D (ap c_2Earithmetic_2ENUMERAL V10n)) (ap c_2Earithmetic_2ENUMERAL V11m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2E_2D V10n) V11m))))))) \wedge ((\forall V12n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEEXP c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 V12n))) = c_2Enum_2E0)) \wedge ((\forall V13n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEEXP c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT2 V13n))) = c_2Enum_2E0)) \wedge ((\forall V14n \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEEXP V14n) c_2Enum_2E0) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO))))))) \wedge ((\forall V15n \in ty_2Enum_2Enum.(\forall V16m \in ty_2Enum_2Enum.((ap (ap c_2Earithmetic_2EEEXP (ap c_2Earithmetic_2ENUMERAL V15n)) (ap c_2Earithmetic_2ENUMERAL V16m)) = (ap c_2Earithmetic_2ENUMERAL (ap (ap c_2Earithmetic_2EEEXP V15n) V16m))))))) \wedge (((ap c_2Enum_2ESUC c_2Enum_2E0) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT1 c_2Earithmetic_2EZERO)))) \wedge ((\forall V17n \in ty_2Enum_2Enum.((ap c_2Enum_2ESUC (ap c_2Earithmetic_2ENUMERAL V17n)) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Enum_2ESUC V17n))))))) \wedge (((ap c_2Eprim_rec_2EPRE c_2Enum_2E0) = c_2Enum_2E0) \wedge ((\forall V18n \in ty_2Enum_2Enum.((ap c_2Eprim_rec_2EPRE (ap c_2Earithmetic_2ENUMERAL V18n)) = (ap c_2Earithmetic_2ENUMERAL (ap c_2Eprim_rec_2EPRE V18n))))))) \wedge ((\forall V19n \in ty_2Enum_2Enum.(((ap c_2Earithmetic_2ENUMERAL V19n) = c_2Enum_2E0) \Leftrightarrow (V19n = c_2Earithmetic_2EZERO))) \wedge ((\forall V20n \in ty_2Enum_2Enum.((c_2Enum_2E0 = (ap c_2Earithmetic_2ENUMERAL V20n)) \Leftrightarrow (V20n = c_2Earithmetic_2EZERO))) \wedge ((\forall V21n \in ty_2Enum_2Enum.((\forall V22m \in ty_2Enum_2Enum.(((ap c_2Earithmetic_2ENUMERAL V21n) = (ap c_2Earithmetic_2ENUMERAL V22m)) \Leftrightarrow (V21n = V22m))))))) \wedge ((\forall V23n \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL V23n)) \Leftrightarrow False))) \wedge ((\forall V24n \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL V24n)) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) V24n))))))) \wedge ((\forall V25n \in ty_2Enum_2Enum.((\forall V26m \in ty_2Enum_2Enum.((p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL V25n)) (ap c_2Earithmetic_2ENUMERAL V26m)) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) (ap c_2Earithmetic_2ENUMERAL V25n) V26m))))))) \wedge ((\forall V27n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E c_2Enum_2E0) V27n)) \Leftrightarrow False))) \wedge ((\forall V28n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E (ap c_2Earithmetic_2ENUMERAL V28n)) c_2Enum_2E0) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Earithmetic_2EZERO) V28n))))))) \wedge ((\forall V29n \in ty_2Enum_2Enum.((\forall V30m \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3E c_2Enum_2E0) V29n)) (ap c_2Earithmetic_2ENUMERAL V30m)) \Leftrightarrow (p (ap (ap c_2Eprim_rec_2E_3C c_2Enum_2E0) V29n))))))) \wedge ((\forall V31n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3D c_2Enum_2E0) V31n)) \Leftrightarrow True))) \wedge ((\forall V32n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3C c_2Enum_2E0) V32n)) \Leftrightarrow False))) \wedge ((\forall V33n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3D c_2Enum_2E0) V33n)) \Leftrightarrow True))) \wedge ((\forall V34n \in ty_2Enum_2Enum.((p (ap (ap c_2Earithmetic_2E_3D c_2Enum_2E0) V34n)) \Leftrightarrow False)))$

Assume the following.

Assume the following.

$$\begin{aligned}
 (\forall V0n \in ty_2Enum_2Enum. (((ap c_2Enumeral_2EiDUB (ap c_2Earithmetic_2EBIT1 \\
 V0n)) = (ap c_2Earithmetic_2EBIT2 (ap c_2Enumeral_2EiDUB V0n))) \wedge \\
 (((ap c_2Enumeral_2EiDUB (ap c_2Earithmetic_2EBIT2 V0n)) = (ap \\
 c_2Earithmetic_2EBIT2 (ap c_2Earithmetic_2EBIT1 V0n))) \wedge ((ap \\
 c_2Enumeral_2EiDUB c_2Earithmetic_2EZERO) = c_2Earithmetic_2EZERO)))) \\
 \end{aligned} \tag{28}$$

Assume the following.

$$\begin{aligned}
 (\forall V0n \in ty_2Enum_2Enum. ((p (ap c_2Earithmetic_2EEVEN c_2Earithmetic_2EZERO)) \wedge \\
 ((p (ap c_2Earithmetic_2EEVEN (ap c_2Earithmetic_2EBIT2 V0n))) \wedge \\
 ((\neg(p (ap c_2Earithmetic_2EEVEN (ap c_2Earithmetic_2EBIT1 V0n)))) \wedge \\
 ((\neg(p (ap c_2Earithmetic_2EODD c_2Earithmetic_2EZERO))) \wedge ((\\
 \neg(p (ap c_2Earithmetic_2EODD (ap c_2Earithmetic_2EBIT2 V0n))) \wedge \\
 (p (ap c_2Earithmetic_2EODD (ap c_2Earithmetic_2EBIT1 V0n)))))))) \\
 \end{aligned} \tag{29}$$

Assume the following.

$$\begin{aligned}
 ((\forall V0x \in ty_2Enum_2Enum. ((ap (ap c_2Enumeral_2Eonecount \\
 c_2Earithmetic_2EZERO) V0x) = V0x)) \wedge (\forall V1n \in ty_2Enum_2Enum. \\
 (\forall V2x \in ty_2Enum_2Enum. ((ap (ap c_2Enumeral_2Eonecount \\
 (ap c_2Earithmetic_2EBIT1 V1n)) V2x) = (ap (ap c_2Enumeral_2Eonecount \\
 V1n) (ap c_2Enum_2ESUC V2x)))))) \wedge (\forall V3n \in ty_2Enum_2Enum. \\
 (\forall V4x \in ty_2Enum_2Enum. ((ap (ap c_2Enumeral_2Eonecount \\
 (ap c_2Earithmetic_2EBIT2 V3n)) V4x) = c_2Earithmetic_2EZERO)))) \\
 \end{aligned} \tag{30}$$

Assume the following.

$$\begin{aligned}
 (((ap c_2Enumeral_2Eexactlog c_2Earithmetic_2EZERO) = c_2Earithmetic_2EZERO) \wedge \\
 ((\forall V0n \in ty_2Enum_2Enum. ((ap c_2Enumeral_2Eexactlog (\\
 ap c_2Earithmetic_2EBIT1 V0n)) = c_2Earithmetic_2EZERO)) \wedge (\forall V1n \in \\
 ty_2Enum_2Enum. ((ap c_2Enumeral_2Eexactlog (ap c_2Earithmetic_2EBIT2 \\
 V1n)) = (ap (ap (c_2Ebool_2LET ty_2Enum_2Enum ty_2Enum_2Enum) \\
 (\lambda V2x \in ty_2Enum_2Enum. (ap (ap (ap (c_2Ebool_2ECOND ty_2Enum_2Enum) \\
 (ap (ap (c_2Emin_2E_3D ty_2Enum_2Enum) V2x) c_2Earithmetic_2EZERO) \\
 c_2Earithmetic_2EZERO) (ap c_2Earithmetic_2EBIT1 V2x)))) (ap \\
 (ap c_2Enumeral_2Eonecount V1n) c_2Earithmetic_2EZERO))))))) \\
 \end{aligned} \tag{31}$$

Assume the following.

$$\begin{aligned}
& (\forall V0n \in ty_2Enum_2Enum. (\forall V1x \in ty_2Enum_2Enum. (\forall V2y \in ty_2Enum_2Enum. (((ap (ap c_2Earithmetic_2E_2A c_2Earithmetic_2EZERO) \\
V0n) = c_2Earithmetic_2EZERO) \wedge (((ap (ap c_2Earithmetic_2E_2A \\
V0n) c_2Earithmetic_2EZERO) = c_2Earithmetic_2EZERO) \wedge (((ap \\
(ap c_2Earithmetic_2E_2A (ap c_2Earithmetic_2EBIT1 V1x)) (ap \\
c_2Earithmetic_2EBIT1 V2y)) = (ap (ap c_2Enumeral_2Einternal_mult \\
(ap c_2Earithmetic_2EBIT1 V1x)) (ap c_2Earithmetic_2EBIT1 V2y))) \wedge \\
(((ap (ap c_2Earithmetic_2E_2A (ap c_2Earithmetic_2EBIT1 V1x)) \\
(ap c_2Earithmetic_2EBIT2 V2y)) = (ap (ap (c_2Ebool_2ELET ty_2Enum_2Enum \\
ty_2Enum_2Enum) (\lambda V3n \in ty_2Enum_2Enum. (ap (ap (c_2Ebool_2ECOND \\
ty_2Enum_2Enum) (ap c_2Earithmetic_2EODD V3n)) (ap (ap c_2Enumeral_2Eexp_help \\
(ap c_2Earithmetic_2EDIV2 V3n)) (ap c_2Eprim_rec_2EPRE (ap c_2Earithmetic_2EBIT1 \\
V1x)))) (ap (ap c_2Enumeral_2Einternal_mult (ap c_2Earithmetic_2EBIT1 \\
V1x)) (ap c_2Earithmetic_2EBIT2 V2y)))))) (ap c_2Enumeral_2Eexactlog \\
(ap c_2Earithmetic_2EBIT2 V2y)))) \wedge (((ap (ap c_2Earithmetic_2E_2A \\
(ap c_2Earithmetic_2EBIT2 V1x)) (ap c_2Earithmetic_2EBIT1 V2y)) = \\
(ap (ap (c_2Ebool_2ELET ty_2Enum_2Enum ty_2Enum_2Enum) (\lambda V4m \in \\
ty_2Enum_2Enum. (ap (ap (c_2Ebool_2ECOND ty_2Enum_2Enum) \\
(ap c_2Earithmetic_2EODD V4m)) (ap (ap c_2Enumeral_2Eexp_help \\
(ap c_2Earithmetic_2EDIV2 V4m)) (ap c_2Eprim_rec_2EPRE (ap c_2Earithmetic_2EBIT1 \\
V2y)))))) (ap (ap c_2Enumeral_2Einternal_mult (ap c_2Earithmetic_2EBIT2 \\
V1x)) (ap c_2Earithmetic_2EBIT1 V2y)))))) (ap c_2Enumeral_2Eexactlog \\
(ap c_2Earithmetic_2EBIT2 V1x)))) \wedge ((ap (ap c_2Earithmetic_2E_2A \\
(ap c_2Earithmetic_2EBIT2 V1x)) (ap c_2Earithmetic_2EBIT2 V2y)) = \\
(ap (ap (c_2Ebool_2ELET ty_2Enum_2Enum ty_2Enum_2Enum) (\lambda V5m \in \\
ty_2Enum_2Enum. (ap (ap (c_2Ebool_2ELET ty_2Enum_2Enum ty_2Enum_2Enum) \\
(\lambda V6n \in ty_2Enum_2Enum. (ap (ap (ap (c_2Ebool_2ECOND ty_2Enum_2Enum) \\
(ap c_2Earithmetic_2EODD V5m)) (ap (ap c_2Enumeral_2Eexp_help \\
(ap c_2Earithmetic_2EDIV2 V5m)) (ap c_2Eprim_rec_2EPRE (ap c_2Earithmetic_2EBIT2 \\
V2y)))))) (ap (ap (ap (c_2Ebool_2ECOND ty_2Enum_2Enum) (ap c_2Earithmetic_2EODD \\
V6n)) (ap (ap c_2Enumeral_2Eexp_help (ap c_2Earithmetic_2EDIV2 \\
V6n)) (ap c_2Eprim_rec_2EPRE (ap c_2Earithmetic_2EBIT2 V1x)))) \\
(ap (ap c_2Enumeral_2Einternal_mult (ap c_2Earithmetic_2EBIT2 \\
V1x)) (ap c_2Earithmetic_2EBIT2 V2y)))))) (ap c_2Enumeral_2Eexactlog \\
(ap c_2Earithmetic_2EBIT2 V2y)))))) (ap c_2Enumeral_2Eexactlog \\
(ap c_2Earithmetic_2EBIT2 V1x)))))))))))))) \\
(32)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
 & (\forall V0n \in ty_2Enum_2Enum. (\forall V1m \in ty_2Enum_2Enum. \\
 & ((ap (ap c_2Eenumeral_2Einternal_mult c_2Earithmetic_2EZERO) \\
 & V0n) = c_2Earithmetic_2EZERO) \wedge (((ap (ap c_2Eenumeral_2Einternal_mult \\
 & V0n) c_2Earithmetic_2EZERO) = c_2Earithmetic_2EZERO) \wedge (((ap \\
 & (ap c_2Eenumeral_2Einternal_mult (ap c_2Earithmetic_2EBIT1 \\
 & V0n)) V1m) = (ap c_2Eenumeral_2EiZ (ap (ap c_2Earithmetic_2E_2B \\
 & (ap c_2Eenumeral_2EiDUB (ap (ap c_2Eenumeral_2Einternal_mult \\
 & V0n) V1m))) V1m))) \wedge ((ap (ap c_2Eenumeral_2Einternal_mult (ap \\
 & c_2Earithmetic_2EBIT2 V0n)) V1m) = (ap c_2Eenumeral_2EiDUB (ap \\
 & c_2Eenumeral_2EiZ (ap (ap c_2Earithmetic_2E_2B (ap (ap c_2Eenumeral_2Einternal_mult \\
 & V0n) V1m)))))))))) \\
 & \end{aligned} \tag{33}$$

Assume the following.

$$\begin{aligned}
 & \forall A_27a.\text{nonempty } A_27a \Rightarrow ((ap (c_2Ewords_2Edimword A_27a) \\
 & (c_2Ebool_2Ethe_value A_27a)) = (ap (ap c_2Earithmetic_2E_2A \\
 & (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT2 c_2Earithmetic_2EZERO))) \\
 & (ap (c_2Ewords_2EINT_MIN A_27a) (c_2Ebool_2Ethe_value A_27a)))) \\
 & \end{aligned} \tag{34}$$

Assume the following.

$$\begin{aligned}
 & ((ap (c_2Ewords_2EINT_MIN (ty_2Efcp_2Ebit0 ty_2Eone_2Eone)) \\
 & (c_2Ebool_2Ethe_value (ty_2Efcp_2Ebit0 ty_2Eone_2Eone))) = \\
 & (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT2 c_2Earithmetic_2EZERO))) \\
 & \end{aligned} \tag{35}$$

Theorem 1

$$\begin{aligned}
 & ((ap (c_2Ewords_2Edimword (ty_2Efcp_2Ebit0 ty_2Eone_2Eone)) \\
 & (c_2Ebool_2Ethe_value (ty_2Efcp_2Ebit0 ty_2Eone_2Eone))) = \\
 & (ap c_2Earithmetic_2ENUMERAL (ap c_2Earithmetic_2EBIT2 (ap c_2Earithmetic_2EBIT1 \\
 & c_2Earithmetic_2EZERO)))) \\
 & \end{aligned}$$