

Definition 18 We define $c_Ebit_EDIV_EXP$ to be $\lambda V0x \in ty_Enum_Enum.\lambda V1n \in ty_Enum_Enum$.
Let $c_Earithmetic_E_D : \iota$ be given. Assume the following.

$$c_Earithmetic_E_D \in ((ty_Enum_Enum^{ty_Enum_Enum})^{ty_Enum_Enum}) \quad (13)$$

Let $c_Earithmetic_EMOD : \iota$ be given. Assume the following.

$$c_Earithmetic_EMOD \in ((ty_Enum_Enum^{ty_Enum_Enum})^{ty_Enum_Enum}) \quad (14)$$

Definition 19 We define $c_Ebit_EMOD_EXP$ to be $\lambda V0x \in ty_Enum_Enum.\lambda V1n \in ty_Enum_Enum$.

Definition 20 We define c_Ebit_EBITS to be $\lambda V0h \in ty_Enum_Enum.\lambda V1l \in ty_Enum_Enum.\lambda V$

Definition 21 We define c_Ebit_EBIT to be $\lambda V0b \in ty_Enum_Enum.\lambda V1n \in ty_Enum_Enum.(ap$

Let $ty_Efc_Efinite_image : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow nonempty\ (ty_Efc_Efinite_image\ A0) \quad (15)$$

Definition 22 We define $c_Ebool_E_3F_21$ to be $\lambda A_27a : \iota.(\lambda V0P \in (2^{A_27a}).(ap\ (ap\ c_Ebool_E_2F_5C$

Definition 23 We define $c_Efc_Efinite_index$ to be $\lambda A_27a : \iota.(ap\ (c_Emin_E_40\ (A_27a^{ty_Enum_Enum}$

Let $ty_Efc_Ecart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A0.nonempty\ A0 \Rightarrow \forall A1.nonempty\ A1 \Rightarrow nonempty\ (ty_Efc_Ecart\ A0\ A1) \quad (16)$$

Let $c_Efc_Edest_cart : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow c_Efc_Edest_cart\ A_27a\ A_27b \in ((A_27a^{(ty_Efc_Efinite_image\ A_27b)})^{(ty_Efc_Ecart\ A_27a\ A_27b)}) \quad (17)$$

Definition 24 We define $c_Efc_Efc_index$ to be $\lambda A_27a : \iota.\lambda A_27b : \iota.\lambda V0x \in (ty_Efc_Ecart\ A_27a\ A_27b)$

Definition 25 We define c_Efc_EFCP to be $\lambda A_27a : \iota.\lambda A_27b : \iota.(\lambda V0g \in (A_27a^{ty_Enum_Enum}).(ap$

Definition 26 We define c_Ewords_En2w to be $\lambda A_27a : \iota.\lambda V0n \in ty_Enum_Enum.(ap\ (c_Efc_EFC$

Definition 27 We define $c_Ewords_Eword_nand$ to be $\lambda A_27a : \iota.\lambda V0v \in (ty_Efc_Ecart\ 2\ A_27a).\lambda V$

Assume the following.

$$\begin{aligned} & (\forall V0x \in ty_Enum_Enum.(\forall V1n \in ty_Enum_Enum.(\\ & \quad \forall V2op \in ((2^2)^2).(\forall V3a \in ty_Enum_Enum.(\forall V4b \in \\ & \quad ty_Enum_Enum.((p\ (ap\ (ap\ c_Eprim_rec_E_3C\ V0x)\ V1n)) \Rightarrow ((\\ & \quad p\ (ap\ (ap\ c_Ebit_EBIT\ V0x)\ (ap\ (ap\ (ap\ (ap\ c_Ebit_EBITWISE\ V1n) \\ & \quad V2op)\ V3a)\ V4b))) \Leftrightarrow (p\ (ap\ (ap\ V2op\ (ap\ (ap\ c_Ebit_EBIT\ V0x)\ V3a)) \\ & \quad (ap\ (ap\ c_Ebit_EBIT\ V0x)\ V4b)))))))))) \end{aligned} \quad (18)$$

Assume the following.

$$True \quad (19)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0t \in 2. ((\forall V1x \in A_27a.(p\ V0t) \Leftrightarrow (p\ V0t)))) \quad (20)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \Rightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Rightarrow True) \Leftrightarrow \\ & True) \wedge (((False \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge (((p\ V0t) \Rightarrow (p\ V0t)) \Leftrightarrow True) \wedge ((\\ & (p\ V0t) \Rightarrow False) \Leftrightarrow (\neg(p\ V0t)))))) \end{aligned} \quad (21)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. ((V0x = V0x) \Leftrightarrow True)) \quad (22)$$

Assume the following.

$$\forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0x \in A_27a. (\forall V1y \in A_27a. ((V0x = V1y) \Leftrightarrow (V1y = V0x)))) \quad (23)$$

Assume the following.

$$\begin{aligned} & (\forall V0t \in 2. (((True \Leftrightarrow (p\ V0t)) \Leftrightarrow (p\ V0t)) \wedge (((p\ V0t) \Leftrightarrow True) \Leftrightarrow \\ & (p\ V0t)) \wedge (((False \Leftrightarrow (p\ V0t)) \Leftrightarrow (\neg(p\ V0t))) \wedge (((p\ V0t) \Leftrightarrow False) \Leftrightarrow (\neg(\\ & p\ V0t)))))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned} & (\forall V0A \in 2. (\forall V1B \in 2. (((\neg((p\ V0A) \wedge (p\ V1B))) \Leftrightarrow ((\neg(\\ & p\ V0A) \vee (\neg(p\ V1B)))) \wedge ((\neg((p\ V0A) \vee (p\ V1B))) \Leftrightarrow ((\neg(p\ V0A) \wedge (\neg(p\ V1B))))))))) \end{aligned} \quad (25)$$

Assume the following.

$$\begin{aligned} & (\forall V0t1 \in 2. (\forall V1t2 \in 2. (\forall V2t3 \in 2. (((p\ V0t1) \Rightarrow \\ & ((p\ V1t2) \Rightarrow (p\ V2t3))) \Leftrightarrow (((p\ V0t1) \wedge (p\ V1t2)) \Rightarrow (p\ V2t3)))))) \end{aligned} \quad (26)$$

Assume the following.

$$\begin{aligned} & (\forall V0x \in 2. (\forall V1x_27 \in 2. (\forall V2y \in 2. (\forall V3y_27 \in \\ & 2. (((p\ V0x) \Leftrightarrow (p\ V1x_27)) \wedge ((p\ V1x_27) \Rightarrow ((p\ V2y) \Leftrightarrow (p\ V3y_27)))) \Rightarrow \\ & (((p\ V0x) \Rightarrow (p\ V2y)) \Leftrightarrow ((p\ V1x_27) \Rightarrow (p\ V3y_27)))))) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} & \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\ & \forall V0x \in (ty_2EfcP_2Ecart\ A_27a\ A_27b). (\forall V1y \in (ty_2EfcP_2Ecart \\ & A_27a\ A_27b). ((V0x = V1y) \Leftrightarrow (\forall V2i \in ty_2Enum_2Enum. ((p\ (ap \\ & (ap\ c_2Eprim_rec_2E_3C\ V2i)\ (ap\ (c_2EfcP_2Edimindex\ A_27b)\ (\\ & c_2Ebool_2Ethe_value\ A_27b)))) \Rightarrow ((ap\ (ap\ (c_2EfcP_2EfcP_index \\ & A_27a\ A_27b)\ V0x)\ V2i) = (ap\ (ap\ (c_2EfcP_2EfcP_index\ A_27a\ A_27b) \\ & V1y)\ V2i)))))) \end{aligned} \quad (28)$$

Assume the following.

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow \forall A_27b.nonempty\ A_27b \Rightarrow (\\
& \quad \forall V0g \in (A_27a^{ty_2Enum_2Enum}).(\forall V1i \in ty_2Enum_2Enum. \\
& \quad ((p\ (ap\ (ap\ c_2Eprim_rec_2E_3C\ V1i)\ (ap\ (c_2Efc_2Edimindex\ A_27b) \\
& \quad (c_2Ebool_2Ethe_value\ A_27b)))) \Rightarrow ((ap\ (ap\ (c_2Efc_2Efc_index \\
& \quad A_27a\ A_27b)\ (ap\ (c_2Efc_2EFCP\ A_27a\ A_27b)\ V0g))\ V1i) = (ap\ V0g \\
& \quad V1i))))))
\end{aligned} \tag{29}$$

Theorem 1

$$\begin{aligned}
& \forall A_27a.nonempty\ A_27a \Rightarrow (\forall V0n \in ty_2Enum_2Enum.(\\
& \quad \forall V1m \in ty_2Enum_2Enum.((ap\ (ap\ (c_2Ewords_2Eword_nand \\
& \quad A_27a)\ (ap\ (c_2Ewords_2En2w\ A_27a)\ V0n))\ (ap\ (c_2Ewords_2En2w \\
& \quad A_27a)\ V1m)) = (ap\ (c_2Ewords_2En2w\ A_27a)\ (ap\ (ap\ (ap\ (ap\ c_2Ebit_2EBITWISE \\
& \quad (ap\ (c_2Efc_2Edimindex\ A_27a)\ (c_2Ebool_2Ethe_value\ A_27a)))) \\
& \quad (\lambda V2x \in 2.(\lambda V3y \in 2.(ap\ c_2Ebool_2E_7E\ (ap\ (ap\ c_2Ebool_2E_2F_5C \\
& \quad V2x)\ V3y))))))\ V0n)\ V1m))))))
\end{aligned}$$