

l103_fomodel4 (TM- FydN3hweRdTg5tUuNTNNSgcNVmfLVQkJH)

October 27, 2020

Let $v6_struct_0 : \iota \Rightarrow o$ be given. Let $v11_fomodel1 : \iota \Rightarrow o$ be given. Let $l1_fomodel1 : \iota \Rightarrow o$ be given. Let $v10_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_fomodel1 : \iota \Rightarrow \iota$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k9_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_setfam_1 : \iota \Rightarrow \iota$ be given. Let $k1_fomodel4 : \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k22_fomodel4 : \iota \Rightarrow \iota$ be given. Let $k25_fomodel4 : \iota \Rightarrow \iota$ be given. Let $k9_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k27_fomodel4 : \iota \Rightarrow \iota$ be given. Let $k24_fomodel4 : \iota \Rightarrow \iota$ be given. Let $k26_fomodel4 : \iota \Rightarrow \iota$ be given. Let $k28_fomodel4 : \iota \Rightarrow \iota$ be given. Let $v10_fomodel4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v2_fomodel3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4_fomodel3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k35_fomodel1 : \iota \Rightarrow \iota$ be given. Let $k6_fomodel4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_tarski : \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v7_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v5_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v8_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k11_fomodel0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v9_fomodel1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\forall X0. \forall X1. (m1_subset_1 X0 (k1_zfmisc_1 X1)) \Leftrightarrow (r1_tarski X0 X1) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. k2_tarski X0 X1 = k2_xboole_0 (k1_tarski X0) (k1_tarski X1) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((\neg v1_xboole_0 X1) \wedge (m1_funct_2 X2 X0 X1)) \Rightarrow (\forall X3. (m2_funct_2 X3 X0 X1 X2) \Leftrightarrow (m1_subset_1 X3 X2)) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 X0)) \Rightarrow (k9_subset_1 X0 X1 X2 = k3_xboole_0 X1 X2) \quad (4)$$

Assume the following.

$$\forall X0.k9_setfam_1 X0 = k1_zfmisc_1 X0 \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1_xboole_0 X0) \wedge ((m1_subset_1 X1 X0) \wedge (m1_subset_1 X2 X0))) \Rightarrow (k7_domain_1 X0 X1 X2 = k2_tarski X1 X2) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0) \wedge (m1_subset_1 X1 X0)) \Rightarrow (k6_domain_1 X0 X1 = k1_tarski X1) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1_subset_1 X1 (k1_zfmisc_1 X0)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 X0))) \Rightarrow (k4_subset_1 X0 X1 X2 = k2_xboole_0 X1 X2) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v6_struct_0 X1) \wedge ((v11_fomodel1 X1) \wedge \\ & (l1_fomodel1 X1))) \Rightarrow (\forall X2.((v7_fomodel1 X2 X1) \wedge (m1_subset_1 \\ & X2 (k1_fomodel1 X1))) \Rightarrow (\forall X3.(m1_subset_1 X3 (k1_zfmisc_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1)))) \Rightarrow (((k9_subset_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 \\ & X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k6_domain_1 (k9_funct_2 \\ & (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) \\ & (k24_fomodel4 X1)) X3 = k6_domain_1 (k9_funct_2 (k9_setfam_1 (\\ & k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k24_fomodel4 \\ & X1)) \wedge ((k9_subset_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k6_domain_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k26_fomodel4 \\ & X1)) X3 = k6_domain_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k26_fomodel4 X1)) \wedge ((k9_subset_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) X3 (k6_domain_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k28_fomodel4 X1)) = k6_domain_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) (k28_fomodel4 X1)) \wedge (v10_fomodel4 X0 X1 X3))) \Rightarrow (v2_fomodel3 \\ & (k4_fomodel3 X1 X2 X0) X1 (k35_fomodel1 X1) X2 (k6_fomodel4 X1 X3 \\ & X0)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((\neg v6_struct_0 X1) \wedge ((v11_fomodel1 X1) \wedge \\
& (l1_fomodel1 X1))) \Rightarrow (\forall X2. (m1_subset_1 X2 (k1_zfmisc_1 \\
& (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\
& X1)))))) \Rightarrow (\forall X3. ((v5_fomodel1 X3 X1) \wedge (m1_subset_1 X3 (k1_fomodel1 \\
& X1))) \Rightarrow (((r1_tarski (k6_domain_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 \\
& X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k27_fomodel4 X1)) X2) \wedge (\\
& (v10_fomodel4 X0 X1 X2) \wedge (v8_fomodel1 X3 X1))) \Rightarrow (v2_fomodel3 (k4_fomodel3 \\
& X1 X3 X0) X1 (k35_fomodel1 X1) X3 (k6_fomodel4 X1 X2 X0)))))) \\
& (10)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((\neg v6_struct_0 X1) \wedge ((v11_fomodel1 X1) \wedge \\
& (l1_fomodel1 X1))) \Rightarrow (\forall X2. ((v4_fomodel1 X2 X1) \wedge (m1_subset_1 \\
& X2 (k1_fomodel1 X1))) \Rightarrow (\forall X3. (m1_subset_1 X3 (k1_zfmisc_1 \\
& (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\
& X1)))))) \Rightarrow (((r1_tarski (k7_domain_1 (k9_funct_2 (k9_setfam_1 \\
& (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k22_fomodel4 \\
& X1) (k25_fomodel4 X1)) X3) \wedge ((r1_tarski (k7_domain_1 (k9_funct_2 \\
& (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) \\
& (k24_fomodel4 X1) (k26_fomodel4 X1)) X3) \wedge (v10_fomodel4 X0 X1 X3))) \Rightarrow \\
& (v2_fomodel3 (k4_fomodel3 X1 X2 X0) X1 (k35_fomodel1 X1) X2 (k6_fomodel4 \\
& X1 X3 X0)))))) \\
& (11)
\end{aligned}$$

Assume the following.

$$\forall X0. \forall X1. \neg v1_xboole_0 (k2_tarski X0 X1) \quad (12)$$

Assume the following.

$$\forall X0. \neg v1_xboole_0 (k1_zfmisc_1 X0) \quad (13)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. (m1_funct_2 X2 X0 X1) \Rightarrow (\neg v1_xboole_0 X2) \quad (14)$$

Assume the following.

$$\forall X0. \forall X1. (\neg v1_xboole_0 X1) \Rightarrow (m1_funct_2 (k9_funct_2 X0 X1) X0 X1) \quad (15)$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. ((m1_subset_1 X1 (k1_zfmisc_1 \\
& X0)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 X0))) \Rightarrow (m1_subset_1 (k4_subset_1 \\
& X0 X1 X2) (k1_zfmisc_1 X0)) \\
& (16)
\end{aligned}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v6_struct_0 X0) \wedge ((v11_fomodel1 X0) \wedge (l1_fomodel1 \\ X0))) \Rightarrow (m2_funct_2 (k26_fomodel4 X0) (k9_setfam_1 (k1_fomodel4 \\ X0)) (k9_setfam_1 (k1_fomodel4 X0)) (k9_funct_2 (k9_setfam_1 \\ (k1_fomodel4 X0)) (k9_setfam_1 (k1_fomodel4 X0)))) \end{aligned} \quad (17)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v6_struct_0 X0) \wedge ((v11_fomodel1 X0) \wedge (l1_fomodel1 \\ X0))) \Rightarrow (m2_funct_2 (k24_fomodel4 X0) (k9_setfam_1 (k1_fomodel4 \\ X0)) (k9_setfam_1 (k1_fomodel4 X0)) (k9_funct_2 (k9_setfam_1 \\ (k1_fomodel4 X0)) (k9_setfam_1 (k1_fomodel4 X0)))) \end{aligned} \quad (18)$$

Assume the following.

$$\forall X0. \forall X1. m1_subset_1 (k11_fomodel0 X0 X1) (k1_zfmisc_1 X0) \quad (19)$$

Assume the following.

$$\forall X0. \forall X1. k11_fomodel0 X0 X1 = k3_xboole_0 X0 X1 \quad (20)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. (m1_subset_1 X2 (k1_zfmisc_1 \\ X0)) \Rightarrow (k9_subset_1 X0 X1 X2 = k9_subset_1 X0 X2 X1) \end{aligned} \quad (21)$$

Assume the following.

$$\forall X0. \forall X1. k3_xboole_0 X0 X1 = k3_xboole_0 X1 X0 \quad (22)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v6_struct_0 X0) \wedge ((v11_fomodel1 X0) \wedge (l1_fomodel1 \\ X0))) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_fomodel1 X0)) \Rightarrow ((v8_fomodel1 \\ X1 X0) \Rightarrow (v9_fomodel1 X1 X0))) \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v6_struct_0 X0) \wedge ((v11_fomodel1 X0) \wedge (l1_fomodel1 \\ X0))) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_fomodel1 X0)) \Rightarrow (((\neg v5_fomodel1 \\ X1 X0) \wedge (v9_fomodel1 X1 X0)) \Rightarrow ((v4_fomodel1 X1 X0) \wedge (v9_fomodel1 \\ X1 X0)))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v6_struct_0 X0) \wedge ((v11_fomodel1 X0) \wedge (l1_fomodel1 \\ X0))) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_fomodel1 X0)) \Rightarrow (((\neg v7_fomodel1 \\ X1 X0) \wedge (v10_fomodel1 X1 X0)) \Rightarrow ((v8_fomodel1 X1 X0) \wedge (v10_fomodel1 \\ X1 X0)))) \end{aligned} \quad (25)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 \\ X0)) \Rightarrow (v1_xboole_0 X1)) \end{aligned} \quad (26)$$

Theorem 1

$$\begin{aligned} & \forall X0.\forall X1.((\neg v6_struct_0 X1) \wedge ((v11_fomodel1 X1) \wedge \\ & (l1_fomodel1 X1))) \Rightarrow (\forall X2.((v10_fomodel1 X2 X1) \wedge (m1_subset_1 \\ & X2 (k1_fomodel1 X1))) \Rightarrow (\forall X3.(m1_subset_1 X3 (k1_zfmisc_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1)))) \Rightarrow (((r1_tarski (k7_domain_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k22_fomodel4 \\ & X1) (k25_fomodel4 X1)) X3) \wedge ((k9_subset_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) X3 (k6_domain_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) (k27_fomodel4 X1)) = k6_domain_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k27_fomodel4 \\ & X1)) \wedge ((k9_subset_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k6_domain_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k24_fomodel4 \\ & X1)) X3 = k6_domain_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k24_fomodel4 X1)) \wedge ((k9_subset_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) (k6_domain_1 (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) \\ & (k9_setfam_1 (k1_fomodel4 X1))) (k26_fomodel4 X1)) X3 = k6_domain_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) (k26_fomodel4 X1)) \wedge ((k9_subset_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) X3 (k6_domain_1 \\ & (k9_funct_2 (k9_setfam_1 (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 \\ & X1))) (k28_fomodel4 X1)) = k6_domain_1 (k9_funct_2 (k9_setfam_1 \\ & (k1_fomodel4 X1)) (k9_setfam_1 (k1_fomodel4 X1))) (k28_fomodel4 \\ & X1)) \wedge (v10_fomodel4 X0 X1 X3)))))) \Rightarrow (v2_fomodel3 (k4_fomodel3 \\ & X1 X2 X0) X1 (k35_fomodel1 X1) X2 (k6_fomodel4 X1 X3 X0)))) \end{aligned}$$