

# l138\_toprealb

(TMTuQsa9PycrPcv77aePqRi4BMZG6VDfXsB)

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Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k1\_fcont\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k8\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $k32\_sin\_cos : \iota$  be given. Let  $k5\_toprealb : \iota \Rightarrow \iota$  be given. Let  $c45\_toprealb : \iota$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_pre\_topc : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_topalg\_2 : \iota$  be given. Let  $k2\_rcomp\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $c5\_toprealb : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xcmplx\_0 : \iota \Rightarrow o$  be given. Let  $k3\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $k10\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k31\_sin\_cos : \iota$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_toprealb : \iota \Rightarrow \iota$  be given. Let  $v1\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 (k1\_zfmisc\_1 X1)) \Leftrightarrow (r1\_tarski X0 X1) \quad (1)$$

Assume the following.

$$\forall X0. (v1\_xcmplx\_0 X0) \Rightarrow (k3\_xcmplx\_0 np\_1 X0 = X0) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \Rightarrow ((r1\_tarski (k10\_xtuple\_0 X1) X0) \Rightarrow ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 (k9\_xtuple\_0 X1) X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k9\_xtuple\_0 X1) X0))))))) \quad (3)$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0 \ np\_2) \wedge (m2\_subset\_1 \ np\_2 \ k1\_numbers \ k5\_numbers)) \wedge \\ & ((m1\_subset\_1 \ np\_2 \ k5\_numbers) \wedge (m1\_subset\_1 \ np\_2 \ k1\_numbers)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0 \ np\_1) \wedge (m2\_subset\_1 \ np\_1 \ k1\_numbers \ k5\_numbers)) \wedge \\ & ((m1\_subset\_1 \ np\_1 \ k5\_numbers) \wedge (m1\_subset\_1 \ np\_1 \ k1\_numbers)) \end{aligned} \quad (5)$$

Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 \ X0 \ k1\_numbers) \wedge (v1\_xreal\_0 \ X1)) \Rightarrow (k8\_real\_1 \ X0 \ X1 = k3\_xcmplx\_0 \ X0 \ X1) \quad (6)$$

Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 \ X0 \ k1\_numbers) \wedge (v1\_xreal\_0 \ X1)) \Rightarrow (k7\_real\_1 \ X0 \ X1 = k2\_xcmplx\_0 \ X0 \ X1) \quad (7)$$

Assume the following.

$$k32\_sin\_cos = k31\_sin\_cos \quad (8)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 \ X1) \wedge (v5\_relat\_1 \ X1 \ X0)) \Rightarrow (k2\_relset\_1 \ X0 \ X1 = k10\_xtuple\_0 \ X1) \quad (9)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 \ X1) \wedge (v4\_relat\_1 \ X1 \ X0)) \Rightarrow (k1\_relset\_1 \ X0 \ X1 = k9\_xtuple\_0 \ X1) \quad (10)$$

Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 \ X0 \ k1\_numbers) \wedge (v1\_xreal\_0 \ X1)) \Rightarrow (k10\_real\_1 \ X0 \ X1 = k7\_xcmplx\_0 \ X0 \ X1) \quad (11)$$

Assume the following.

$$\begin{aligned} & r1\_tarski \ (k2\_relset\_1 \ k1\_numbers \ (k2\_partfun1 \ k1\_numbers \ k1\_numbers \\ & \ (k1\_fcont\_1 \ (k10\_real\_1 \ np\_1 \ (k8\_real\_1 \ np\_2 \ k32\_sin\_cos)) \\ & \ np\_1) \ (k5\_toprealb \ c45\_toprealb))) \ (k2\_rcomp\_1 \ (k10\_real\_1 \\ & \ np\_1 \ np\_2) \ (k7\_real\_1 \ (k10\_real\_1 \ np\_1 \ np\_2) \ c5\_toprealb)) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} & k1\_relset\_1 \ k1\_numbers \ (k2\_partfun1 \ k1\_numbers \ k1\_numbers \ (k1\_fcont\_1 \\ & \ (k10\_real\_1 \ np\_1 \ (k8\_real\_1 \ np\_2 \ k32\_sin\_cos)) \ np\_1) \ (k5\_toprealb \\ & \ c45\_toprealb)) = k5\_toprealb \ c45\_toprealb \end{aligned} \quad (13)$$

Assume the following.

$$u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k2\_rcomp\_1 (k10\_real\_1 np\_1 np\_2) (k7\_real\_1 (k10\_real\_1 np\_1 np\_2) c5\_toprealb)))) = k5\_toprealb (k2\_rcomp\_1 (k10\_real\_1 np\_1 np\_2) (k7\_real\_1 (k10\_real\_1 np\_1 np\_2) c5\_toprealb)) \quad (14)$$

Assume the following.

$$u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb c45\_toprealb)) = k5\_toprealb c45\_toprealb \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xreal\_0 X0)\wedge(v1\_xreal\_0 X1))\Rightarrow(v1\_xreal\_0 (k7\_xcmplx\_0 X0 X1)) \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xreal\_0 X0)\wedge(v1\_xreal\_0 X1))\Rightarrow(v1\_xreal\_0 (k2\_xcmplx\_0 X0 X1)) \quad (17)$$

Assume the following.

$$\forall X0.\forall X1.((m1\_subset\_1 X0 k1\_numbers)\wedge(v1\_xreal\_0 X1))\Rightarrow(m1\_subset\_1 (k8\_real\_1 X0 X1) k1\_numbers) \quad (18)$$

Assume the following.

$$\forall X0.((v1\_funct\_1 X0)\wedge(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k1\_numbers k1\_numbers))))\Rightarrow((v1\_funct\_1 (k6\_toprealb X0))\wedge(v1\_funct\_2 (k6\_toprealb X0) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k1\_relset\_1 k1\_numbers X0)))) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k2\_relset\_1 k1\_numbers X0)))))\wedge(m1\_subset\_1 (k6\_toprealb X0) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k1\_relset\_1 k1\_numbers X0)))) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k2\_relset\_1 k1\_numbers X0)))))))))) \quad (19)$$

Assume the following.

$$v1\_xreal\_0 k31\_sin\_cos \quad (20)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0 X0)\wedge(v1\_xxreal\_0 X1))\Rightarrow(m1\_subset\_1 (k2\_rcomp\_1 X0 X1) (k1\_zfmisc\_1 k1\_numbers)) \quad (21)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.((v1\_funct\_1 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))))\Rightarrow((v1\_funct\_1 (k2\_partfun1 X0 X1 X2 X3))\wedge(m1\_subset\_1 (k2\_partfun1 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))) \quad (22)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xreal\_0 X0)\wedge(v1\_xreal\_0 X1))\Rightarrow((v1\_funct\_1 \\ (k1\_fcont\_1 X0 X1))\wedge((v1\_funct\_2 (k1\_fcont\_1 X0 X1) k1\_numbers \\ k1\_numbers)\wedge(m1\_subset\_1 (k1\_fcont\_1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ k1\_numbers k1\_numbers)))))) \end{aligned} \quad (23)$$

Assume the following.

$$(v1\_xreal\_0 c5\_toprealb)\wedge(v2\_xreal\_0 c5\_toprealb) \quad (24)$$

Assume the following.

$$\begin{aligned} (\neg v1\_xboole\_0 c45\_toprealb)\wedge(m1\_subset\_1 c45\_toprealb (k1\_zfmisc\_1 \\ k1\_numbers)) \end{aligned} \quad (25)$$

Assume the following.

$$c5\_toprealb = np\_1 \quad (26)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_funct\_1 X0)\wedge(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ k1\_numbers k1\_numbers))))\Rightarrow(k6\_toprealb X0 = X0) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 (k1\_zfmisc\_1 k1\_numbers))\Rightarrow(k5\_toprealb \\ X0 = X0) \end{aligned} \quad (28)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(v1\_xreal\_0 X0) \quad (29)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(v1\_xcmplx\_0 X0) \quad (30)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 X0 X1)))\Rightarrow((v4\_relat\_1 X2 X0)\wedge(v5\_relat\_1 X2 X1)) \end{aligned} \quad (31)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k1\_numbers)\Rightarrow(v1\_xreal\_0 X0) \quad (32)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v1\_relat\_1 X2) \end{aligned} \quad (33)$$

**Theorem 1**

$(v1\_funct\_1 (k2\_partfun1 k1\_numbers k1\_numbers (k1\_fcont\_1 (k10\_real\_1 np\_1 (k8\_real\_1 np\_2 k32\_sin\_cos)) np\_1) (k5\_toprealb c45\_toprealb))) \wedge ((v1\_funct\_2 (k2\_partfun1 k1\_numbers k1\_numbers (k1\_fcont\_1 (k10\_real\_1 np\_1 (k8\_real\_1 np\_2 k32\_sin\_cos)) np\_1) (k5\_toprealb c45\_toprealb)) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb c45\_toprealb))) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k2\_rcomp\_1 (k10\_real\_1 np\_1 np\_2) (k7\_real\_1 (k10\_real\_1 np\_1 np\_2) c5\_toprealb)))))) \wedge (m1\_subset\_1 (k2\_partfun1 k1\_numbers k1\_numbers (k1\_fcont\_1 (k10\_real\_1 np\_1 (k8\_real\_1 np\_2 k32\_sin\_cos)) np\_1) (k5\_toprealb c45\_toprealb)) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb c45\_toprealb))) (u1\_struct\_0 (k1\_pre\_topc k2\_topalg\_2 (k5\_toprealb (k2\_rcomp\_1 (k10\_real\_1 np\_1 np\_2) (k7\_real\_1 (k10\_real\_1 np\_1 np\_2) c5\_toprealb))))))))))$