

l14\_homothet (TM-  
bUKYjgjf8nKEMQS7wTxqAVREME7GZuKL8)

October 27, 2020

Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_diraf : \iota \Rightarrow o$  be given. Let  $v2\_diraf : \iota \Rightarrow o$  be given. Let  $l1\_analoaf : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_aff\_2 : \iota \Rightarrow o$  be given. Let  $r2\_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\ & (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & \quad X0)) \Rightarrow ((r1\_aff\_1 X0 X1 X2 X3) \Rightarrow ((r1\_aff\_1 X0 X1 X3 X2) \wedge ((r1\_aff\_1 \\ & \quad X0 X2 X1 X3) \wedge ((r1\_aff\_1 X0 X2 X3 X1) \wedge ((r1\_aff\_1 X0 X3 X1 X2) \wedge (r1\_aff\_1 \\ & \quad X0 X3 X2 X1)))))))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\ & (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & \quad X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\ & \quad (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\ & \quad (u1\_struct\_0 X0)) \Rightarrow (((r1\_aff\_1 X0 X1 X2 X4) \wedge ((r1\_aff\_1 X0 X1 X3 X5) \wedge \\ & \quad ((r1\_aff\_1 X0 X1 X3 X6) \wedge ((r2\_analoaf X0 X2 X3 X4 X5) \wedge (r2\_analoaf \\ & \quad X0 X2 X3 X4 X6)))))) \Rightarrow ((r1\_aff\_1 X0 X1 X2 X3) \vee (X5 = X6)))))))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& \quad (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& \quad (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow \\
& \quad ((r1\_aff\_1 X0 X1 X2 X3) \Rightarrow ((X1 = X2) \vee ((X1 = X3) \vee (((\neg(\neg r1\_aff\_1 X0 X1 \\
& X2 X4) \wedge (r1\_aff\_1 X0 X1 X4 X5) \wedge (r2\_analoaf X0 X2 X4 X3 X5))) \wedge (\neg(r1\_aff\_1 \\
& \quad X0 X1 X2 X4) \wedge (\exists X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \wedge (\exists X7. \\
& \quad (m1\_subset\_1 X7 (u1\_struct\_0 X0)) \wedge (\neg r1\_aff\_1 X0 X1 X2 X6) \wedge ((r1\_aff\_1 \\
& X0 X1 X6 X7) \wedge ((r2\_analoaf X0 X2 X6 X3 X7) \wedge ((r2\_analoaf X0 X6 X4 X7 X5) \wedge \\
& \quad (r1\_aff\_1 X0 X1 X2 X5)))))) \vee ((X1 \neq X3) \wedge ((X1 \neq X2) \wedge ((r1\_aff\_1 \\
& X0 X1 X3 X2) \wedge ((\neg r1\_aff\_1 X0 X1 X3 X5) \wedge ((r1\_aff\_1 X0 X1 X5 X4) \wedge (r2\_analoaf \\
& X0 X3 X5 X2 X4))) \vee ((r1\_aff\_1 X0 X1 X3 X5) \wedge (\exists X6.(m1\_subset\_1 \\
& \quad X6 (u1\_struct\_0 X0)) \wedge (\exists X7.(m1\_subset\_1 X7 (u1\_struct\_0 \\
& X0)) \wedge (\neg r1\_aff\_1 X0 X1 X3 X6) \wedge ((r1\_aff\_1 X0 X1 X6 X7) \wedge ((r2\_analoaf \\
& X0 X3 X6 X2 X7) \wedge ((r2\_analoaf X0 X6 X5 X7 X4) \wedge (r1\_aff\_1 X0 X1 X3 X4))))))))))))) \\
& \hspace{15em} (3)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& \quad (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& \quad (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow \\
& \quad (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow (((r1\_aff\_1 X0 \\
& X1 X2 X3) \wedge ((v4\_aff\_2 X0) \wedge (r1\_aff\_1 X0 X1 X2 X4))) \Rightarrow ((X1 = X2) \vee ((\forall X7. \\
& \quad (m1\_subset\_1 X7 (u1\_struct\_0 X0)) \Rightarrow (\forall X8.(m1\_subset\_1 X8 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\neg(\neg r1\_aff\_1 X0 X1 X2 X7) \wedge ((r1\_aff\_1 X0 X1 X7 \\
& X8) \wedge ((r2\_analoaf X0 X2 X7 X3 X8) \wedge ((r2\_analoaf X0 X7 X4 X8 X5) \wedge (r1\_aff\_1 \\
& X0 X1 X2 X5)))))) \vee ((\forall X7.(m1\_subset\_1 X7 (u1\_struct\_0 X0)) \Rightarrow \\
& \quad (\forall X8.(m1\_subset\_1 X8 (u1\_struct\_0 X0)) \Rightarrow (\neg(\neg r1\_aff\_1 X0 \\
& X1 X2 X7) \wedge ((r1\_aff\_1 X0 X1 X7 X8) \wedge ((r2\_analoaf X0 X2 X7 X3 X8) \wedge ((r2\_analoaf \\
& X0 X7 X4 X8 X6) \wedge (r1\_aff\_1 X0 X1 X2 X6)))))) \vee (X5 = X6))))))))) \\
& \hspace{15em} (4)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow (((r1\_aff\_1 X0 \\
& X1 X2 X3) \wedge (v4\_aff\_2 X0)) \Rightarrow ((X1 = X2) \vee ((X1 = X3) \vee (((\neg(\neg r1\_aff\_1 X0 \\
& X1 X2 X4) \wedge ((r1\_aff\_1 X0 X1 X4 X5) \wedge (r2\_analoaf X0 X2 X4 X3 X5)))) \wedge (\neg \\
& (r1\_aff\_1 X0 X1 X2 X4) \wedge (\exists X7.(m1\_subset\_1 X7 (u1\_struct\_0 \\
& X0)) \wedge (\exists X8.(m1\_subset\_1 X8 (u1\_struct\_0 X0)) \wedge ((\neg r1\_aff\_1 \\
& X0 X1 X2 X7) \wedge ((r1\_aff\_1 X0 X1 X7 X8) \wedge ((r2\_analoaf X0 X2 X7 X3 X8) \wedge ( \\
& (r2\_analoaf X0 X7 X4 X8 X5) \wedge (r1\_aff\_1 X0 X1 X2 X5)))))))))) \vee (((\neg( \\
& \neg r1\_aff\_1 X0 X1 X2 X6) \wedge ((r1\_aff\_1 X0 X1 X6 X5) \wedge (r2\_analoaf X0 X2 X6 \\
& X3 X5))) \wedge (\neg(r1\_aff\_1 X0 X1 X2 X6) \wedge (\exists X7.(m1\_subset\_1 X7 ( \\
& u1\_struct\_0 X0)) \wedge (\exists X8.(m1\_subset\_1 X8 (u1\_struct\_0 X0)) \wedge \\
& ((\neg r1\_aff\_1 X0 X1 X2 X7) \wedge ((r1\_aff\_1 X0 X1 X7 X8) \wedge ((r2\_analoaf X0 \\
& X2 X7 X3 X8) \wedge ((r2\_analoaf X0 X7 X6 X8 X5) \wedge (r1\_aff\_1 X0 X1 X2 X5)))))))))) \vee \\
& (X4 = X6))))))))))
\end{aligned}$$