

l17_endalg (TMP- nCDnKV42tG1c7noX7sfKKWrvG6aWmH4)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v11_struct_0 : \iota \Rightarrow o$ be given. Let $l1_msualg_1 : \iota \Rightarrow o$ be given. Let $v4_msualg_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $l3_msualg_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $k6_endalg : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_msualg_3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u3_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_algstr_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v4_relat_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m2_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k8_pboole : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k4_autalg_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_autalg_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v2_relat_1 : \iota \Rightarrow o$ be given. Let $k3_msualg_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $l1_struct_0 : \iota \Rightarrow o$ be given. Let $l2_msualg_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $l5_struct_0 : \iota \Rightarrow o$ be given. Let $l4_algstr_0 : \iota \Rightarrow o$ be given. Let $l3_struct_0 : \iota \Rightarrow o$ be given. Let $l3_algstr_0 : \iota \Rightarrow o$ be given. Let $v22_algstr_0 : \iota \Rightarrow o$ be given. Let $k5_endalg : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_endalg : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u2_algstr_0 : \iota \Rightarrow \iota$ be given. Let $k5_struct_0 : \iota \Rightarrow \iota$ be given. Let $k5_binop_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\
 & \quad (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1_relat_1 \\
 & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0)))) \Rightarrow \\
 & \quad (\forall X3. (m2_pboole X3 X0 X1 X2) \Rightarrow (k8_pboole X3 (k2_msualg_3 \\
 & \quad X0 X2) = X3)))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\
 & \quad (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1_relat_1 \\
 & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0)))) \Rightarrow \\
 & \quad (\forall X3. (m2_pboole X3 X0 X1 X2) \Rightarrow (k8_pboole (k2_msualg_3 X0 \\
 & \quad X1) X3 = X3)))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1_relat_1 X1)\wedge((v4_relat_1 \\ & X1 X0)\wedge((v1_funct_1 X1)\wedge(v1_partfun1 X1 X0))))\wedge((\neg v1_xboole_0 \\ & X2)\wedge(m1_subset_1 X2 (k1_zfmisc_1 (k4_autalg_1 X0 X1 X1))))\Rightarrow(\\ & \forall X3.(m1_autalg_1 X3 X0 X1 X2)\Leftrightarrow(m1_subset_1 X3 X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\ & (((v1_relat_1 X1)\wedge((v4_relat_1 X1 X0)\wedge((v1_funct_1 X1)\wedge(v1_partfun1 \\ & X1 X0))))\wedge(((v1_relat_1 X2)\wedge((v2_relat_1 X2)\wedge((v4_relat_1 X2 \\ & X0)\wedge((v1_funct_1 X2)\wedge(v1_partfun1 X2 X0))))\wedge(((v1_relat_1 \\ & X3)\wedge((v2_relat_1 X3)\wedge((v4_relat_1 X3 X0)\wedge((v1_funct_1 X3)\wedge(\\ & v1_partfun1 X3 X0))))\wedge((m2_pboole X4 X0 X1 X2)\wedge(m2_pboole X5 X0 \\ & X2 X3))))\Rightarrow(k3_msualg_3 X0 X1 X2 X3 X4 X5 = k8_pboole X4 X5) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((l1_struct_0 X0)\wedge((v4_msualg_1 X1 X0)\wedge \\ & (l2_msualg_1 X1 X0)))\Rightarrow((v1_relat_1 (u3_msualg_1 X0 X1))\wedge((v2_relat_1 \\ & (u3_msualg_1 X0 X1))\wedge((v4_relat_1 (u3_msualg_1 X0 X1) (u1_struct_0 \\ & X0))\wedge((v1_funct_1 (u3_msualg_1 X0 X1))\wedge(v1_partfun1 (u3_msualg_1 \\ & X0 X1) (u1_struct_0 X0)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1_relat_1 X1)\wedge((v4_relat_1 \\ & X1 X0)\wedge((v1_funct_1 X1)\wedge(v1_partfun1 X1 X0))))\wedge((\neg v1_xboole_0 \\ & X2)\wedge(m1_subset_1 X2 (k1_zfmisc_1 (k4_autalg_1 X0 X1 X1))))\Rightarrow(\\ & \forall X3.(m1_autalg_1 X3 X0 X1 X2)\Rightarrow(m2_pboole X3 X0 X1 X1)) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.(l5_struct_0 X0)\Rightarrow(l1_struct_0 X0) \quad (7)$$

Assume the following.

$$\forall X0.(l4_algstr_0 X0)\Rightarrow((l3_struct_0 X0)\wedge(l3_algstr_0 X0)) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0)\wedge(l1_msualg_1 X0))\Rightarrow(\forall X1. \\ & (l3_msualg_1 X1 X0)\Rightarrow(l2_msualg_1 X1 X0)) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(l1_msualg_1 X0)\Rightarrow(l5_struct_0 X0) \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge \\ & (l1_msualg_1 X0))) \wedge ((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0))) \Rightarrow \\ & ((v22_algstr_0 (k6_endalg X0 X1)) \wedge (l4_algstr_0 (k6_endalg X0 \\ & X1))) \end{aligned} \tag{11}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge \\ & (l1_msualg_1 X0))) \wedge ((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0))) \Rightarrow \\ & ((v1_funct_1 (k5_endalg X0 X1)) \wedge (v1_funct_2 (k5_endalg X0 X1) \\ & (k2_zfmisc_1 (k4_endalg X0 X1) (k4_endalg X0 X1)) (k4_endalg X0 \\ & X1)) \wedge (m1_subset_1 (k5_endalg X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 \\ & (k2_zfmisc_1 (k4_endalg X0 X1) (k4_endalg X0 X1)) (k4_endalg X0 \\ & X1)))))) \end{aligned} \tag{12}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge \\ & (l1_msualg_1 X0))) \wedge ((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0))) \Rightarrow \\ & ((\neg v1_xboole_0 (k4_endalg X0 X1)) \wedge (m1_subset_1 (k4_endalg X0 \\ & X1) (k1_zfmisc_1 (k4_autalg_1 (u1_struct_0 X0) (u3_msualg_1 X0 \\ & X1) (u3_msualg_1 X0 X1)))))) \end{aligned} \tag{13}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 \\ & X0))) \Rightarrow (\forall X1. ((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0)) \Rightarrow \\ & (\forall X2. ((v22_algstr_0 X2) \wedge (l4_algstr_0 X2)) \Rightarrow ((X2 = k6_endalg \\ & X0 X1) \Leftrightarrow ((u1_struct_0 X2 = k4_endalg X0 X1) \wedge ((u2_algstr_0 X2 = k5_endalg \\ & X0 X1) \wedge (k5_struct_0 X2 = k2_msualg_3 (u1_struct_0 X0) (u3_msualg_1 \\ & X0 X1)))))) \end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 \\ & X0))) \Rightarrow (\forall X1. ((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0)) \Rightarrow \\ & (\forall X2. ((v1_funct_1 X2) \wedge ((v1_funct_2 X2 (k2_zfmisc_1 (k4_endalg \\ & X0 X1) (k4_endalg X0 X1)) (k4_endalg X0 X1)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ & (k2_zfmisc_1 (k2_zfmisc_1 (k4_endalg X0 X1) (k4_endalg X0 X1)) \\ & (k4_endalg X0 X1)))))) \Rightarrow ((X2 = k5_endalg X0 X1) \Leftrightarrow (\forall X3. (m1_autalg_1 \\ & X3 (u1_struct_0 X0) (u3_msualg_1 X0 X1) (k4_endalg X0 X1)) \Rightarrow (\forall X4. \\ & (m1_autalg_1 X4 (u1_struct_0 X0) (u3_msualg_1 X0 X1) (k4_endalg \\ & X0 X1)) \Rightarrow (k5_binop_1 (k4_endalg X0 X1) X2 X3 X4 = k3_msualg_3 (u1_struct_0 \\ & X0) (u3_msualg_1 X0 X1) (u3_msualg_1 X0 X1) (u3_msualg_1 X0 X1) X3 \\ & X4)))))) \end{aligned} \tag{15}$$

Assume the following.

$$\begin{aligned} & \forall X0.(l3_algstr_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_struct_0 \\ & X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u1_struct_0 X0)) \Rightarrow (k6_algstr_0 \\ & X0 X1 X2 = k5_binop_1 (u1_struct_0 X0) (u2_algstr_0 X0) X1 X2))) \end{aligned} \quad (16)$$

Theorem 1

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 \\ & X0))) \Rightarrow (\forall X1.((v4_msualg_1 X1 X0) \wedge (l3_msualg_1 X1 X0)) \Rightarrow \\ & (\forall X2.(m1_subset_1 X2 (u1_struct_0 (k6_endalg X0 X1))) \Rightarrow \\ & (\forall X3.(m1_subset_1 X3 (u1_struct_0 (k6_endalg X0 X1))) \Rightarrow \\ & ((X3 = k2_msualg_3 (u1_struct_0 X0) (u3_msualg_1 X0 X1)) \Rightarrow ((k6_algstr_0 \\ & (k6_endalg X0 X1) X2 X3 = X2) \wedge (k6_algstr_0 (k6_endalg X0 X1) X3 X2 = \\ & X2)))))) \end{aligned}$$