

l21_arytm_1
(TMYn7ivUGT24spYvA3iWjn9TFB1WGT2AdEB)

October 27, 2020

Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_arytm_2 : \iota$ be given. Let $r1_arytm_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_arytm_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_arytm_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_arytm_3 : \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k2_arytm_2) \Rightarrow (\forall X2.(m1_subset_1 X2 k2_arytm_2) \Rightarrow ((r1_arytm_2 \\ & X0 X1) \Leftrightarrow (r1_arytm_2 (k7_arytm_2 X0 X2) (k7_arytm_2 X1 X2)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1_subset_1 X0 k2_arytm_2) \wedge (m1_subset_1 \\ & X1 k2_arytm_2)) \Rightarrow (m1_subset_1 (k1_arytm_1 X0 X1) k2_arytm_2) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k2_arytm_2) \Rightarrow (\forall X2.(m1_subset_1 X2 k2_arytm_2) \Rightarrow (((r1_arytm_2 \\ & X1 X0) \Rightarrow ((X2 = k1_arytm_1 X0 X1) \Leftrightarrow (k7_arytm_2 X2 X1 = X0))) \wedge ((\neg r1_arytm_2 \\ & X1 X0) \Rightarrow ((X2 = k1_arytm_1 X0 X1) \Leftrightarrow (X2 = k11_arytm_3)))))) \end{aligned} \quad (3)$$

Theorem 1

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k2_arytm_2) \Rightarrow (\forall X2.(m1_subset_1 X2 k2_arytm_2) \Rightarrow ((r1_arytm_2 \\ & X0 X1) \Rightarrow ((r1_arytm_2 (k7_arytm_2 X2 X0) X1) \Leftrightarrow (r1_arytm_2 X2 (k1_arytm_1 \\ & X1 X0)))))) \end{aligned}$$