

## l21\_fomodel3

(TMLUEjQXzqUVSfifhVnnASyFN6Lt48xqW6j)

October 27, 2020

Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_relat\_2 : \iota \Rightarrow o$  be given. Let  $v8\_relat\_2 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_2 : \iota \Rightarrow o$  be given. Let  $k6\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. ((v1\_relat\_2 X4) \wedge ((v3\_relat\_2 X4) \wedge ((v8\_relat\_2 X4) \wedge ((v1\_partfun1 X4 X0) \wedge \\ & (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))))))) \Rightarrow (((X1 \in k6\_eqrel\_1 X0 X0 X4 X2) \wedge (X3 \in k6\_eqrel\_1 X0 X0 X4 X2)) \Rightarrow (k4\_tarski X1 X3 \in X4)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2. (m2\_subset\_1 X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. ((v3\_relat\_2 X1) \wedge ((v8\_relat\_2 X1) \wedge ((v1\_partfun1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0)))))) \Rightarrow (k8\_eqrel\_1 X0 X1 = k7\_eqrel\_1 X0 X1) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_eqrel\_1 X1 X0)\Rightarrow(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k1\_zfmisc\_1 X0))) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((v3\_relat\_2 X1)\wedge((v8\_relat\_2 X1)\wedge((v1\_partfun1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))))))\Rightarrow (m1\_eqrel\_1 (k8\_eqrel\_1 X0 X1) X0) \quad (7)$$

Assume the following.

$$\begin{aligned} &\forall X0.\forall X1.((v3\_relat\_2 X1)\wedge((v8\_relat\_2 X1)\wedge((v1\_partfun1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))))))\Rightarrow \\ &(\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k1\_zfmisc\_1 X0)))\Rightarrow \\ &((X2 = k7\_eqrel\_1 X0 X1)\Leftrightarrow(\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 X0))\Rightarrow \\ &((X3 \in X2)\Leftrightarrow(\exists X4.(X4 \in X0)\wedge(X3 = k6\_eqrel\_1 X0 X0 X1 X4)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge((v3\_relat\_2 X0)\wedge(v8\_relat\_2 X0)))\Rightarrow ((v1\_relat\_1 X0)\wedge(v1\_relat\_2 X0)) \quad (9)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(v1\_xboole\_0 X1)) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v1\_relat\_1 X2) \quad (11)$$

Assume the following.

$$\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_eqrel\_1 X1 X0)\Rightarrow(\neg v1\_xboole\_0 X1)) \quad (12)$$

### Theorem 1

$$\begin{aligned} &\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.((v1\_partfun1 X1 X0)\wedge \\ &((v3\_relat\_2 X1)\wedge((v8\_relat\_2 X1)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ &(k2\_zfmisc\_1 X0 X0))))))\Rightarrow(\forall X2.\forall X3.\forall X4.( \\ &m2\_subset\_1 X4 (k1\_zfmisc\_1 X0) (k8\_eqrel\_1 X0 X1))\Rightarrow(((X2 \in X4)\wedge \\ &(X3 \in X4))\Rightarrow(k4\_tarski X2 X3 \in X1)))) \end{aligned}$$