

# l22\_fomodel3 (TMZvQMqwLF- cYN2giN6tgwiQmPCn8zxrsxYE)

October 27, 2020

Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_relat\_2 : \iota \Rightarrow o$  be given. Let  $v8\_relat\_2 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v3\_relat\_2 X1) \wedge ( \\ & (v8\_relat\_2 X1) \wedge ((v1\_partfun1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X0)))))) \Rightarrow (\neg v1\_xboole\_0 (k8\_eqrel\_1 X0 X1))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (\neg v1\_xboole\_0 X1) \Rightarrow (\forall X2. ((v3\_relat\_2 \\ & X2) \wedge ((v8\_relat\_2 X2) \wedge ((v1\_partfun1 X2 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X1 X1)))))) \Rightarrow (\forall X3. (m2\_subset\_1 X3 (k1\_zfmisc\_1 \\ & X1) (k8\_eqrel\_1 X1 X2)) \Rightarrow (\forall X4. (m2\_subset\_1 X4 (k1\_zfmisc\_1 \\ & X1) (k8\_eqrel\_1 X1 X2)) \Rightarrow (((X0 \in X3) \wedge (X0 \in X4)) \Rightarrow (X3 = X4)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v3\_relat\_2 X3) \wedge \\ & ((v1\_partfun1 X3 X0) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X0)))))) \Rightarrow ((X1 \in k6\_eqrel\_1 X0 X0 X3 X2) \Leftrightarrow (k4\_tarski X1 X2 \in X3)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge(((v3\_relat\_2 \\ & X1)\wedge((v8\_relat\_2 X1)\wedge((v1\_partfun1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X0))))))\wedge(m1\_subset\_1 X2 X0)))\Rightarrow(k9\_eqrel\_1 X0 \\ & X1 X2 = k9\_relat\_1 X1 X2) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(m1\_subset\_1 X2 ( \\ & k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(k6\_eqrel\_1 X0 X1 X2 X3 = k9\_relat\_1 \\ & X2 X3) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.((v1\_partfun1 X1 X0)\wedge \\ & ((v3\_relat\_2 X1)\wedge((v8\_relat\_2 X1)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X0))))))\Rightarrow(\forall X2.\forall X3.\forall X4.( \\ & m2\_subset\_1 X4 (k1\_zfmisc\_1 X0) (k8\_eqrel\_1 X0 X1))\Rightarrow(((X2 \in X4)\wedge \\ & (X3 \in X4))\Rightarrow(k4\_tarSKI X2 X3 \in X1)))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))))\Rightarrow(\forall X2.(m2\_subset\_1 \\ & X2 X0 X1)\Rightarrow(m1\_subset\_1 X2 X0)) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(m1\_eqrel\_1 X1 X0)\Rightarrow(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k1\_zfmisc\_1 X0))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge(((v3\_relat\_2 \\ & X1)\wedge((v8\_relat\_2 X1)\wedge((v1\_partfun1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X0))))))\wedge(m1\_subset\_1 X2 X0)))\Rightarrow(m2\_subset\_1 \\ & (k9\_eqrel\_1 X0 X1 X2) (k1\_zfmisc\_1 X0) (k8\_eqrel\_1 X0 X1)) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v3\_relat\_2 X1)\wedge((v8\_relat\_2 X1)\wedge((v1\_partfun1 \\ & X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))))))\Rightarrow \\ & (m1\_eqrel\_1 (k8\_eqrel\_1 X0 X1) X0) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & X0))\Rightarrow(v1\_xboole\_0 X1)) \end{aligned} \quad (12)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_partfun1 X1 X0) \wedge \\ & ((v3\_relat\_2 X1) \wedge ((v8\_relat\_2 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X0)))))) \Rightarrow (\forall X2.(m2\_subset\_1 X2 (k1\_zfmisc\_1 \\ & X0) (k8\_eqrel\_1 X0 X1)) \Rightarrow (\forall X3.(m2\_subset\_1 X3 (k1\_zfmisc\_1 \\ & X0) (k8\_eqrel\_1 X0 X1)) \Rightarrow (\forall X4.\forall X5.((X4 \in X2) \wedge ((X5 \in \\ & X3) \wedge (k4\_tarski X4 X5 \in X1))) \Rightarrow (X2 = X3)))))) \end{aligned}$$