

l29\_grnilp\_1  
(TMKPUltujVh8g5Y8rSoivriX1sWvYKTsnrH)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_group\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $l3\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v15\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_group\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_group\_3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_group\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k10\_group\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $g3\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u2\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_group\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_group\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_group\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1.(m1\_group\_2 X1 X0) \Rightarrow (\forall X2. \\ & (m1\_group\_2 X2 X0) \Rightarrow ((m1\_group\_2 X2 X1) \Leftrightarrow (g3\_algstr\_0 (u1\_struct\_0 \\ & (k10\_group\_2 X0 X2 X1)) (u2\_algstr\_0 (k10\_group\_2 X0 X2 X1)) = g3\_algstr\_0 \\ & (u1\_struct\_0 X2) (u2\_algstr\_0 X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1.(m1\_group\_2 X1 X0) \Rightarrow (\forall X2. \\ & (m1\_group\_2 X2 X0) \Rightarrow ((m1\_group\_2 (k10\_group\_2 X0 X1 X2) X1) \wedge (m1\_group\_2 \\ & (k10\_group\_2 X0 X1 X2) X2)))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1.(m1\_group\_2 X1 X0) \Rightarrow (\forall X2. \\ & (m1\_group\_2 X2 X0) \Rightarrow (\forall X3.(m1\_group\_2 X3 X0) \Rightarrow (r1\_group\_2 \\ & X0 (k10\_group\_2 X0 (k10\_group\_2 X0 X1 X2) X3) (k10\_group\_2 X0 X1 ( \\ & k10\_group\_2 X0 X2 X3)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1.(m1\_group\_2 X1 X0) \Rightarrow (\forall X2. \\ & (m1\_group\_6 X2 X0 X1) \Rightarrow (\forall X3.(m1\_group\_6 X3 X0 X1) \Rightarrow (k10\_group\_2 \\ & X0 X2 X3 = k10\_group\_2 X1 X2 X3)))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 \\ & X0) \wedge ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0)))) \wedge (((v15\_algstr\_0 X1) \wedge \\ & (m1\_group\_2 X1 X0)) \wedge ((v15\_algstr\_0 X2) \wedge (m1\_group\_2 X2 X0)))) \Rightarrow \\ & ((r1\_group\_2 X0 X1 X2) \Leftrightarrow (X1 = X2)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge \\ & ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0)))) \wedge (m1\_group\_2 X1 X0)) \Rightarrow (\forall X2. \\ & (m1\_group\_6 X2 X0 X1) \Leftrightarrow (m1\_group\_2 X2 X1)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 \\ & X0) \wedge ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0)))) \wedge (((v1\_group\_3 X1 X0) \wedge \\ & (m1\_group\_2 X1 X0)) \wedge (m1\_group\_2 X2 X0))) \Rightarrow (k3\_group\_6 X0 X1 X2 = \\ & k9\_group\_2 X0 X1 X2) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 \\ & X0) \wedge ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0)))) \wedge ((m1\_group\_2 X1 X0) \wedge \\ & (m1\_group\_2 X2 X0))) \Rightarrow (k10\_group\_2 X0 X1 X2 = k9\_group\_2 X0 X1 X2) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge (l3\_algstr\_0 \\ & X0))) \Rightarrow (\forall X1.(m1\_group\_2 X1 X0) \Rightarrow ((\neg v2\_struct\_0 X1) \wedge ((v2\_group\_1 \\ & X1) \wedge (l3\_algstr\_0 X1)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 \\ & X0) \wedge ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0)))) \wedge (((v1\_group\_3 X1 X0) \wedge \\ & (m1\_group\_2 X1 X0)) \wedge (m1\_group\_2 X2 X0))) \Rightarrow ((v15\_algstr\_0 (k3\_group\_6 \\ & X0 X1 X2)) \wedge ((v1\_group\_3 (k3\_group\_6 X0 X1 X2) X2) \wedge (m1\_group\_6 ( \\ & k3\_group\_6 X0 X1 X2) X0 X2))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge (v2\_group\_1 \\ & X0) \wedge (v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0))) \wedge ((m1\_group\_2 X1 X0) \wedge \\ & (m1\_group\_2 X2 X0)) \Rightarrow ((v15\_algstr\_0 (k10\_group\_2 X0 X1 X2)) \wedge \\ & m1\_group\_2 (k10\_group\_2 X0 X1 X2) X0)) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge (v2\_group\_1 \\ & X0) \wedge (v3\_group\_1 X0) \wedge (l3\_algstr\_0 X0))) \wedge ((m1\_group\_2 X1 X0) \wedge \\ & (m1\_group\_2 X2 X0)) \Rightarrow (k10\_group\_2 X0 X1 X2 = k10\_group\_2 X0 X2 X1) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge (v2\_group\_1 X0) \wedge (v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)) \Rightarrow (\forall X1. (m1\_group\_2 X1 X0) \Rightarrow (v3\_group\_1 \\ & X1)) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0. (l3\_algstr\_0 X0) \Rightarrow ((v15\_algstr\_0 X0) \Rightarrow (X0 = g3\_algstr\_0 \\ & (u1\_struct\_0 X0) (u2\_algstr\_0 X0))) \end{aligned} \quad (14)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge (v2\_group\_1 X0) \wedge (v3\_group\_1 \\ & X0) \wedge (l3\_algstr\_0 X0)) \Rightarrow (\forall X1. ((v15\_algstr\_0 X1) \wedge (m1\_group\_2 \\ & X1 X0)) \Rightarrow (\forall X2. (m1\_group\_2 X2 X0) \Rightarrow (\forall X3. (m1\_group\_2 \\ & X3 X0) \Rightarrow (((v1\_group\_3 X1 X3) \wedge (m1\_group\_6 X1 X0 X3)) \Rightarrow ((v1\_group\_3 \\ & (k10\_group\_2 X0 X1 X2) (k10\_group\_2 X0 X3 X2)) \wedge (m1\_group\_6 (k10\_group\_2 \\ & X0 X1 X2) X0 (k10\_group\_2 X0 X3 X2))))))) \end{aligned}$$