

# l30\_homothet (TMF- FVEp3dPRthBHJm8tSEUdHWFGhZJQddvt)

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Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_diraf : \iota \Rightarrow o$  be given. Let  $v2\_diraf : \iota \Rightarrow o$  be given. Let  $l1\_analoaf : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $r2\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v7\_aff\_2 : \iota \Rightarrow o$  be given. Let  $r2\_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r5\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r3\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\ & (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & X0)) \Rightarrow ((r1\_aff\_1 X0 X1 X2 X3) \Rightarrow ((r1\_aff\_1 X0 X1 X3 X2) \wedge ((r1\_aff\_1 \\ & X0 X2 X1 X3) \wedge ((r1\_aff\_1 X0 X2 X3 X1) \wedge ((r1\_aff\_1 X0 X3 X1 X2) \wedge (r1\_aff\_1 \\ & X0 X3 X2 X1)))))))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\ & (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\ & (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\ & (u1\_struct\_0 X0)) \Rightarrow (\neg(X1 \neq X2) \wedge ((\neg(\neg(r2\_analoaf X0 X1 X2 X3 X4) \wedge \\ & (r2\_analoaf X0 X1 X2 X5 X6)) \wedge ((\neg(r2\_analoaf X0 X1 X2 X3 X4) \wedge (r2\_analoaf \\ & X0 X5 X6 X1 X2)) \wedge ((\neg(r2\_analoaf X0 X3 X4 X1 X2) \wedge (r2\_analoaf X0 X5 X6 \\ & X1 X2)) \wedge (\neg(r2\_analoaf X0 X3 X4 X1 X2) \wedge (r2\_analoaf X0 X1 X2 X5 X6)))))) \wedge \\ & (\neg r2\_analoaf X0 X3 X4 X5 X6)))))))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(( \\
& v1\_aff\_1 X2 X0) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow \\
& \quad (\exists X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \wedge \\
& \quad ((X1 \in X3) \wedge (r5\_aff\_1 X0 X2 X3))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X3.(m1\_subset\_1 \\
& X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (((r5\_aff\_1 X0 X2 X3) \wedge ((X1 \in \\
& X2) \wedge (X1 \in X3))) \Rightarrow (X2 = X3))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (u1\_struct\_0 X0))) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0))) \Rightarrow (((r2\_aff\_1 X0 X1 X2 X3) \wedge (r5\_aff\_1 X0 X3 X4)) \Rightarrow \\
& \quad (r2\_aff\_1 X0 X1 X2 X4))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\
& \quad (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\
& \quad ((r3\_aff\_1 X0 X1 X2) \Rightarrow ((v1\_aff\_1 X1 X0) \wedge (v1\_aff\_1 X2 X0))))))
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0))) \Rightarrow (\neg (r2\_aff\_1 X0 X1 X2 X3) \wedge ((\neg X1 \in X3) \wedge (X2 \in X3))))))
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& \quad (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\
& \quad ((\exists X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \wedge (\exists X3.( \\
& m1\_subset\_1 X3 (u1\_struct\_0 X0)) \wedge (r2\_aff\_1 X0 X2 X3 X1))) \Rightarrow (v1\_aff\_1 \\
& \quad X1 X0)))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0)) \Rightarrow (((X3 = k2\_aff\_1 X0 X1 X2) \Rightarrow ((X1 = X2) \vee ((v1\_aff\_1 \\
& X3 X0) \wedge ((X1 \in X3) \wedge ((X2 \in X3) \wedge (X1 \neq X2)))))) \wedge (((v1\_aff\_1 X3 X0) \wedge \\
& (X1 \in X3) \wedge (X2 \in X3)) \Rightarrow ((X1 = X2) \vee ((X1 \neq X2) \wedge (X3 = k2\_aff\_1 X0 X1 X2)))))))))) \Rightarrow \\
& (9)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0)) \Rightarrow (((v1\_aff\_1 X3 X0) \wedge (X1 \in X3)) \Rightarrow ((X2 \in X3) \Leftrightarrow (r2\_aff\_1 \\
& X0 X1 X2 X3)))))) \Rightarrow \\
& (10)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf \\
& X0) \wedge (l1\_analoaf X0))) \wedge ((m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\
& X0))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))) \Rightarrow ((r5\_aff\_1 \\
& X0 X1 X2) \Leftrightarrow (r3\_aff\_1 X0 X1 X2)) \\
& (11)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf \\
& X0) \wedge (l1\_analoaf X0))) \wedge ((m1\_subset\_1 X1 (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\
& X2 (u1\_struct\_0 X0)))) \Rightarrow (k2\_aff\_1 X0 X1 X2 = k1\_aff\_1 X0 X1 X2) \\
& (12)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow (\forall X7.(m1\_subset\_1 \\
& X7 (u1\_struct\_0 X0)) \Rightarrow (\forall X8.(m1\_subset\_1 X8 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X9.(m1\_subset\_1 X9 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\
& (((r2\_aff\_1 X0 X1 X2 X9) \wedge ((v7\_aff\_2 X0) \wedge ((X4 \in X9) \wedge ((X5 \in X9) \wedge (( \\
& r2\_analoaf X0 X4 X1 X5 X3) \wedge ((r2\_analoaf X0 X4 X2 X5 X6) \wedge ((r2\_aff\_1 \\
& X0 X3 X6 X9) \wedge ((X7 \in X9) \wedge ((X8 \in X9) \wedge (r2\_analoaf X0 X7 X1 X8 X3)))))))))) \Rightarrow \\
& ((X1 \in X9) \vee ((X3 \in X9) \vee (r2\_analoaf X0 X7 X2 X8 X6)))))))))) \Rightarrow \\
& (13)
\end{aligned}$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(((\neg v7\_struct\_0 X0)\wedge((v1\_diraf \\ X0)\wedge(l1\_analoaf X0)))\wedge((m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 \\ X2 (u1\_struct\_0 X0))))\Rightarrow(m1\_subset\_1 (k2\_aff\_1 X0 X1 X2) (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0))) \end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v7\_struct\_0 X0)\wedge((v1\_diraf X0)\wedge(l1\_analoaf X0)))\Rightarrow \\ (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0))\Rightarrow(\forall X2.(m1\_subset\_1 \\ X2 (u1\_struct\_0 X0))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0))\Rightarrow((X3 = k1\_aff\_1 X0 X1 X2)\Leftrightarrow(\forall X4.(m1\_subset\_1 \\ X4 (u1\_struct\_0 X0))\Rightarrow((X4 \in X3)\Leftrightarrow(r1\_aff\_1 X0 X1 X2 X4))))))) \end{aligned} \tag{15}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v7\_struct\_0 X0)\wedge((v1\_diraf X0)\wedge(l1\_analoaf X0)))\Rightarrow \\ (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0))\Rightarrow(\forall X2.(m1\_subset\_1 \\ X2 (u1\_struct\_0 X0))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ X0))\Rightarrow((r1\_aff\_1 X0 X1 X2 X3)\Leftrightarrow(r2\_analoaf X0 X1 X2 X1 X3)))))) \end{aligned} \tag{16}$$

**Theorem 1**

$$\begin{aligned} \forall X0.((\neg v7\_struct\_0 X0)\wedge((v1\_diraf X0)\wedge((v2\_diraf X0)\wedge \\ (l1\_analoaf X0))))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ X0))\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0))\Rightarrow(\forall X3. \\ (m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(\forall X4.(m1\_subset\_1 X4 \\ (u1\_struct\_0 X0))\Rightarrow(\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0))\Rightarrow \\ (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0))\Rightarrow(\forall X7.(m1\_subset\_1 \\ X7 (u1\_struct\_0 X0))\Rightarrow(\forall X8.(m1\_subset\_1 X8 (u1\_struct\_0 \\ X0))\Rightarrow(\forall X9.(m1\_subset\_1 X9 (u1\_struct\_0 X0))\Rightarrow(\forall X10. \\ (m1\_subset\_1 X10 (k1\_zfmisc\_1 (u1\_struct\_0 X0))\Rightarrow(((r2\_aff\_1 \\ X0 X1 X2 X10)\wedge((v7\_aff\_2 X0)\wedge((X4 \in X10)\wedge((X5 \in X10)\wedge((r2\_analoaf \\ X0 X4 X1 X5 X3)\wedge((r2\_analoaf X0 X4 X2 X5 X6)\wedge((r2\_aff\_1 X0 X3 X6 X10)\wedge \\ ((X7 \in X10)\wedge((X8 \in X10)\wedge((r2\_analoaf X0 X7 X1 X8 X3)\wedge((r2\_aff\_1 X0 \\ X3 X9 X10)\wedge(r2\_analoaf X0 X7 X2 X8 X9))))))))))))))\Rightarrow((X1 \in X10)\vee(( \\ X3 \in X10)\vee(X9 = X6)))))))))) \end{aligned}$$