

# l31\_autalg\_1

(TMY4N1CCZSxqwEPCPzUPnep6kV2onGykRMw)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_autalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_autalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_msualg\_3 : \iota \Rightarrow o$  be given. Let  $v2\_msualg\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m2\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r4\_msualg\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_msualg\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_autalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l2\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_relat\_1 : \iota \Rightarrow o$  be given. Let  $l5\_struct\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (l1\_msualg\_1 X0))) \Rightarrow (\forall X1. (l3\_msualg\_1 X1 X0) \Rightarrow (\forall X2. (l3\_msualg\_1 X2 X0) \Rightarrow (\forall X3. (m2\_pboole X3 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1) (u3\_msualg\_1 X0 X2)) \Rightarrow ((r4\_msualg\_3 X0 X1 X2 X3) \Leftrightarrow ((r1\_msualg\_3 X0 X1 X2 X3) \wedge ((v2\_msualg\_3 X3 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1) (u3\_msualg\_1 X0 X2)) \wedge (v1\_msualg\_3 X3))))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. (((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0)))) \wedge ((\neg v1\_xboole\_0 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k4\_autalg\_1 X0 X1 X1)))))) \Rightarrow (\forall X3. (m1\_autalg\_1 X3 X0 X1 X2) \Leftrightarrow (m1\_subset\_1 X3 X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((l1\_struct\_0 X0)\wedge((v4\_msualg\_1 X1 X0)\wedge \\ & (l2\_msualg\_1 X1 X0)))\Rightarrow((v1\_relat\_1 (u3\_msualg\_1 X0 X1))\wedge((v2\_relat\_1 \\ & (u3\_msualg\_1 X0 X1))\wedge((v4\_relat\_1 (u3\_msualg\_1 X0 X1) (u1\_struct\_0 \\ & X0))\wedge((v1\_funct\_1 (u3\_msualg\_1 X0 X1))\wedge(v1\_partfun1 (u3\_msualg\_1 \\ & X0 X1) (u1\_struct\_0 X0))))))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge((v4\_relat\_1 \\ & X1 X0)\wedge((v1\_funct\_1 X1)\wedge(v1\_partfun1 X1 X0))))\wedge((\neg v1\_xboole\_0 \\ & X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k4\_autalg\_1 X0 X1 X1))))\Rightarrow( \\ & \forall X3.(m1\_autalg\_1 X3 X0 X1 X2)\Rightarrow(m2\_pboole X3 X0 X1 X1)) \end{aligned} \quad (5)$$

Assume the following.

$$\forall X0.(l5\_struct\_0 X0)\Rightarrow(l1\_struct\_0 X0) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge(l1\_msualg\_1 X0))\Rightarrow(\forall X1. \\ & (l3\_msualg\_1 X1 X0)\Rightarrow(l2\_msualg\_1 X1 X0)) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.(l1\_msualg\_1 X0)\Rightarrow(l5\_struct\_0 X0) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge \\ & (l1\_msualg\_1 X0)))\wedge((v4\_msualg\_1 X1 X0)\wedge(l3\_msualg\_1 X1 X0)))\Rightarrow \\ & ((\neg v1\_xboole\_0 (k5\_autalg\_1 X0 X1))\wedge(m1\_subset\_1 (k5\_autalg\_1 \\ & X0 X1) (k1\_zfmisc\_1 (k4\_autalg\_1 (u1\_struct\_0 X0) (u3\_msualg\_1 \\ & X0 X1) (u3\_msualg\_1 X0 X1)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge(l1\_msualg\_1 \\ & X0)))\Rightarrow(\forall X1.((v4\_msualg\_1 X1 X0)\wedge(l3\_msualg\_1 X1 X0))\Rightarrow \\ & (\forall X2.((\neg v1\_xboole\_0 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k4\_autalg\_1 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1) (u3\_msualg\_1 \\ & X0 X1))))\Rightarrow((X2 = k5\_autalg\_1 X0 X1)\Leftrightarrow(\forall X3.(m2\_pboole X3 \\ & (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1) (u3\_msualg\_1 X0 X1))\Rightarrow((X3 \in \\ & X2)\Leftrightarrow(r4\_msualg\_3 X0 X1 X1 X3)))))) \end{aligned} \quad (10)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge (l1\_msualg\_1 \\ & X0)) \Rightarrow (\forall X1.((v4\_msualg\_1 X1 X0) \wedge (l3\_msualg\_1 X1 X0)) \Rightarrow \\ & (\forall X2.(m1\_autalg\_1 X2 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1) \\ & (k5\_autalg\_1 X0 X1)) \Rightarrow ((v1\_msualg\_3 X2) \wedge (v2\_msualg\_3 X2 (u1\_struct\_0 \\ & X0) (u3\_msualg\_1 X0 X1) (u3\_msualg\_1 X0 X1)))))) \end{aligned}$$