

## l36\_homothet

(TMXq8W18M6AiGr2CEnCBDix6DhrH1LmDBLi)

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Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_diraf : \iota \Rightarrow o$  be given. Let  $v2\_diraf : \iota \Rightarrow o$  be given. Let  $l1\_analoaf : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_homothet : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v8\_transgeo : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\ & (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\ & ((\exists X2. (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \wedge (\exists X3. ( \\ & m1\_subset\_1 X3 (u1\_struct\_0 X0)) \wedge (r2\_aff\_1 X0 X2 X3 X1))) \Rightarrow (v1\_aff\_1 \\ & X1 X0))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\ & (l1\_analoaf X0)))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\ & (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X4. \\ & ((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0)) \wedge ((v3\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\ & X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)))))) \Rightarrow \\ & (((r2\_aff\_1 X0 X1 X2 X3) \wedge (\forall X5. (m1\_subset\_1 X5 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X6. (m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow ((k3\_funct\_2 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X5 = X6) \Leftrightarrow ((X5 \in X3) \wedge (X5 = X6)) \vee \\ & ((\neg X5 \in X3) \wedge (\exists X7. (m1\_subset\_1 X7 (u1\_struct\_0 X0)) \wedge (\exists X8. \\ & (m1\_subset\_1 X8 (u1\_struct\_0 X0)) \wedge ((X7 \in X3) \wedge ((X8 \in X3) \wedge ((r2\_analoaf \\ & X0 X7 X1 X8 X5) \wedge ((r2\_analoaf X0 X7 X2 X8 X6) \wedge (r2\_aff\_1 X0 X5 X6 X3)))))))))) \Rightarrow \\ & ((X1 \in X3) \vee (v8\_transgeo X4 X0)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& \quad (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& \quad (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X4. \\
& \quad ((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& \quad X0)) \wedge ((v3\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\
& \quad X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)))))) \Rightarrow \\
& \quad (((r2\_aff\_1 X0 X1 X2 X3) \wedge (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow ((k3\_funct\_2 \\
& \quad (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X5 = X6) \Leftrightarrow ((X5 \in X3) \wedge (X5 = X6)) \vee \\
& \quad ((\neg X5 \in X3) \wedge (\exists X7.(m1\_subset\_1 X7 (u1\_struct\_0 X0)) \wedge (\exists X8. \\
& \quad (m1\_subset\_1 X8 (u1\_struct\_0 X0)) \wedge ((X7 \in X3) \wedge ((X8 \in X3) \wedge ((r2\_analoaf \\
& \quad X0 X7 X1 X8 X5) \wedge ((r2\_analoaf X0 X7 X2 X8 X6) \wedge (r2\_aff\_1 X0 X5 X6 X3)))))))))) \Rightarrow \\
& \quad (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (r2\_aff\_1 X0 X5 \\
& \quad (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X5) X3)))))) \Rightarrow \\
& \hspace{15em} (3)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& \quad (l1\_analoaf X0)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 \\
& \quad X1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge ((v3\_funct\_2 X1 (u1\_struct\_0 \\
& \quad X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad (u1\_struct\_0 X0) (u1\_struct\_0 X0)))))) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((r1\_homothet X0 X1 X2) \Leftrightarrow (( \\
& \quad v8\_transgeo X1 X0) \wedge ((v1\_aff\_1 X2 X0) \wedge ((\forall X3.(m1\_subset\_1 \\
& \quad X3 (u1\_struct\_0 X0)) \Rightarrow ((X3 \in X2) \Rightarrow (k3\_funct\_2 (u1\_struct\_0 X0) ( \\
& \quad u1\_struct\_0 X0) X1 X3 = X3))) \wedge (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (r2\_aff\_1 X0 X3 (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& \quad X0) X1 X3) X2)))))) \Rightarrow \\
& \hspace{15em} (4)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\ & (l1\_analoaf X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\ & (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0)) \Rightarrow (\forall X4. \\ & ((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0)) \wedge ((v3\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\ & X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0))))))) \Rightarrow \\ & (((r2\_aff\_1 X0 X1 X2 X3) \wedge (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow ((k3\_funct\_2 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X5 = X6) \Leftrightarrow (((X5 \in X3) \wedge (X5 = X6)) \vee \\ & ((\neg X5 \in X3) \wedge (\exists X7.(m1\_subset\_1 X7 (u1\_struct\_0 X0)) \wedge (\exists X8. \\ & (m1\_subset\_1 X8 (u1\_struct\_0 X0)) \wedge ((X7 \in X3) \wedge ((X8 \in X3) \wedge ((r2\_analoaf \\ & X0 X7 X1 X8 X5) \wedge ((r2\_analoaf X0 X7 X2 X8 X6) \wedge (r2\_aff\_1 X0 X5 X6 X3)))))))))) \Rightarrow \\ & ((X1 \in X3) \vee (r1\_homothet X0 X4 X3)))))) \end{aligned}$$