

## l43\_helly

(TMJXz1LCQLxpTMRQbYBWccExuzKDsLjoZHK)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $v1\_glib\_000 : \iota \Rightarrow o$  be given. Let  $v3\_glib\_002 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_glib\_000 : \iota \Rightarrow \iota$  be given. Let  $k13\_glib\_001 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_helly : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v5\_glib\_001 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m3\_glib\_001 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (k3\_xboole\_0 X1 (k1\_tarski X0) = k1\_tarski X0) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ & X0) \wedge ((v1\_finset\_1 X0) \wedge ((v1\_glib\_000 X0) \wedge (v3\_glib\_002 X0)))))) \Rightarrow \\ & (\forall X1. (m1\_subset\_1 X1 (k6\_glib\_000 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 \\ & X2 (k6\_glib\_000 X0)) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (k6\_glib\_000 \\ & X0)) \Rightarrow ((X3 \in k13\_glib\_001 X0 (k2\_helly X0 X1 X2)) \Leftrightarrow (k9\_subset\_1 ( \\ & k6\_glib\_000 X0) (k13\_glib\_001 X0 (k2\_helly X0 X1 X3)) (k13\_glib\_001 \\ & X0 (k2\_helly X0 X3 X2)) = k1\_tarski X3)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ & X0) \wedge ((v1\_finset\_1 X0) \wedge ((v1\_glib\_000 X0) \wedge (v3\_glib\_002 X0)))))) \Rightarrow \\ & (\forall X1. (m1\_subset\_1 X1 (k6\_glib\_000 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 \\ & X2 (k6\_glib\_000 X0)) \Rightarrow (k13\_glib\_001 X0 (k2\_helly X0 X1 X2) = k13\_glib\_001 \\ & X0 (k2\_helly X0 X2 X1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. k3\_xboole\_0 (k3\_xboole\_0 X0 X1) X2 = k3\_xboole\_0 X0 (k3\_xboole\_0 X1 X2) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 X0))\Rightarrow(k9\_subset\_1 X0 X1 X2 = k3\_xboole\_0 X1 X2) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X0)\wedge((v4\_relat\_1 \\ & X0 k5\_numbers)\wedge((v1\_funct\_1 X0)\wedge((v1\_finset\_1 X0)\wedge((v1\_glib\_000 \\ & X0)\wedge(v3\_glib\_002 X0))))))\wedge((m1\_subset\_1 X1 (k6\_glib\_000 X0))\wedge \\ & (m1\_subset\_1 X2 (k6\_glib\_000 X0))))\Rightarrow((v5\_glib\_001 (k2\_helly \\ & X0 X1 X2) X0)\wedge(m3\_glib\_001 (k2\_helly X0 X1 X2) X0)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v4\_relat\_1 X0 k5\_numbers)\wedge \\ & ((v1\_funct\_1 X0)\wedge((v1\_finset\_1 X0)\wedge(v1\_glib\_000 X0)))))\wedge(m3\_glib\_001 \\ & X1 X0))\Rightarrow((v1\_finset\_1 (k13\_glib\_001 X0 X1))\wedge(m1\_subset\_1 (k13\_glib\_001 \\ & X0 X1) (k1\_zfmisc\_1 (k6\_glib\_000 X0)))) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.k3\_xboole\_0 X0 X1 = k3\_xboole\_0 X1 X0 \quad (8)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(((v1\_relat\_1 X0)\wedge((v4\_relat\_1 X0 k5\_numbers)\wedge((v1\_funct\_1 \\ & X0)\wedge((v1\_finset\_1 X0)\wedge((v1\_glib\_000 X0)\wedge(v3\_glib\_002 X0))))))\Rightarrow \\ & (\forall X1.(m1\_subset\_1 X1 (k6\_glib\_000 X0))\Rightarrow(\forall X2.(m1\_subset\_1 \\ & X2 (k6\_glib\_000 X0))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (k6\_glib\_000 \\ & X0))\Rightarrow((X3 \in k13\_glib\_001 X0 (k2\_helly X0 X1 X2))\Rightarrow(k9\_subset\_1 ( \\ & k6\_glib\_000 X0) (k9\_subset\_1 (k6\_glib\_000 X0) (k13\_glib\_001 X0 \\ & (k2\_helly X0 X1 X2)) (k13\_glib\_001 X0 (k2\_helly X0 X2 X3))) (k13\_glib\_001 \\ & X0 (k2\_helly X0 X3 X1)) = k1\_tarski X3)))))) \end{aligned}$$