

l50_polyred

(TMKXrdLa7SnhTGWTk51VT2Rj8M4cmr92S8c)

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Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k15_pre_poly : \iota \Rightarrow \iota$ be given. Let $v1_relat_2 : \iota \Rightarrow o$ be given. Let $v4_relat_2 : \iota \Rightarrow o$ be given. Let $v6_relat_2 : \iota \Rightarrow o$ be given. Let $v8_relat_2 : \iota \Rightarrow o$ be given. Let $v2_bagorder : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v7_struct_0 : \iota \Rightarrow o$ be given. Let $v13_algstr_0 : \iota \Rightarrow o$ be given. Let $v3_rlvect_1 : \iota \Rightarrow o$ be given. Let $v4_rlvect_1 : \iota \Rightarrow o$ be given. Let $l2_algstr_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v1_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_termord : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_polyred : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_termord : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k7_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $r2_polyred : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r2_termord : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $l2_struct_0 : \iota \Rightarrow o$ be given. Let $l1_struct_0 : \iota \Rightarrow o$ be given. Let $l1_algstr_0 : \iota \Rightarrow o$ be given. Let $k2_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1 X0) \Rightarrow (\forall X1.((v1_partfun1 X1 (k15_pre_poly \\
& \quad X0)) \wedge ((v1_relat_2 X1) \wedge ((v4_relat_2 X1) \wedge ((v6_relat_2 X1) \wedge ((\\
& \quad v8_relat_2 X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\
& \quad X0) (k15_pre_poly X0)))))))))) \Rightarrow (\forall X2.((\neg v2_struct_0 X2) \wedge \\
& \quad (l2_algstr_0 X2)) \Rightarrow (\forall X3.((v1_funct_1 X3) \wedge ((v1_funct_2 \\
& \quad X3 (k15_pre_poly X0) (u1_struct_0 X2)) \wedge ((v1_polynom1 X3 (k15_pre_poly \\
& \quad X0) X2) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\
& \quad X0) (u1_struct_0 X2)))))))))) \Rightarrow (\forall X4.((v1_funct_1 X4) \wedge ((v1_funct_2 \\
& \quad X4 (k15_pre_poly X0) (u1_struct_0 X2)) \wedge ((v1_polynom1 X4 (k15_pre_poly \\
& \quad X0) X2) \wedge (m1_subset_1 X4 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\
& \quad X0) (u1_struct_0 X2)))))))))) \Rightarrow ((r1_polyred X0 X1 X2 X3 X4) \Leftrightarrow (\neg r2_polyred \\
& \quad X0 X1 X2 X4 X3))))))
\end{aligned}$$

(1)

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly\ X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((v8_relat_2\ X1) \wedge ((v2_bagorder\ X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\\
& \quad \forall X2.((\neg v7_struct_0\ X2) \wedge ((v13_algstr_0\ X2) \wedge ((v3_rlvect_1\ X2) \wedge ((v4_rlvect_1\ X2) \wedge (l2_algstr_0\ X2)))))) \Rightarrow (\forall X3.((v1_funct_1\ X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))) \Rightarrow (\forall X4.((v1_funct_1\ X4) \wedge ((v1_funct_2\ X4\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X4\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))) \Rightarrow ((r2_polyred\ X0\ X1\ X2\ X3\ X4) \Leftrightarrow (\neg(\neg(r2_funct_2\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)\ X3\ (k7_polynom1\ X0\ X2)) \wedge (X4 \neq k7_polynom1\ X0\ X2)) \wedge (\neg r2_termord\ X0\ X1\ (k3_termord\ X0\ X1\ X2\ X3)\ (k3_termord\ X0\ X1\ X2\ X4)) \wedge (\neg(k3_termord\ X0\ X1\ X2\ X3 = k3_termord\ X0\ X1\ X2\ X4) \wedge (r2_polyred\ X0\ X1\ X2\ (k6_termord\ X0\ X1\ X2\ X3)\ (k6_termord\ X0\ X1\ X2\ X4)))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.(l2_struct_0\ X0) \Rightarrow (l1_struct_0\ X0) \tag{3}$$

Assume the following.

$$\forall X0.(l2_algstr_0\ X0) \Rightarrow ((l2_struct_0\ X0) \wedge (l1_algstr_0\ X0)) \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.((v3_ordinal1\ X0) \wedge (((v1_partfun1\ X1\ (k15_pre_poly\ X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((v8_relat_2\ X1) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \wedge ((\neg v2_struct_0\ X2) \wedge ((v13_algstr_0\ X2) \wedge ((v3_rlvect_1\ X2) \wedge ((v4_rlvect_1\ X2) \wedge (l2_algstr_0\ X2)))))) \wedge ((v1_funct_1\ X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))) \Rightarrow ((v1_funct_1\ (k6_termord\ X0\ X1\ X2\ X3)) \wedge ((v1_funct_2\ (k6_termord\ X0\ X1\ X2\ X3)\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ (k6_termord\ X0\ X1\ X2\ X3)\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ (k6_termord\ X0\ X1\ X2\ X3)\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly \\
& \quad X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((\\
& \quad v8_relat_2\ X1) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly \\
& \quad \quad X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\forall X2.((\neg v2_struct_0\ X2) \wedge \\
& \quad (l2_struct_0\ X2)) \Rightarrow (\forall X3.((v1_funct_1\ X3) \wedge ((v1_funct_2 \\
& \quad X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X3\ (k15_pre_poly \\
& \quad \quad X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly \\
& \quad \quad \quad X0)\ (u1_struct_0\ X2))))))) \Rightarrow (\forall X4.((v1_funct_1\ X4) \wedge ((v1_funct_2 \\
& \quad X4\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X4\ (k15_pre_poly \\
& \quad \quad X0)\ X2) \wedge (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly \\
& \quad \quad \quad X0)\ (u1_struct_0\ X2))))))) \Rightarrow ((r2_polyred\ X0\ X1\ X2\ X3\ X4) \Leftrightarrow ((r1_polyred \\
& \quad X0\ X1\ X2\ X3\ X4) \wedge (k2_polynom1\ (k15_pre_poly\ X0)\ X2\ X3 \neq k2_polynom1 \\
& \quad \quad (k15_pre_poly\ X0)\ X2\ X4))))))
\end{aligned} \tag{6}$$

Assume the following.

$$\forall X0.(l1_struct_0\ X0) \Rightarrow ((v2_struct_0\ X0) \Rightarrow (v7_struct_0\ X0)) \tag{7}$$

Theorem 1

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly \\
& \quad X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((\\
& \quad v8_relat_2\ X1) \wedge ((v2_bagorder\ X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1 \\
& \quad \quad (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\\
& \quad \forall X2.((\neg v7_struct_0\ X2) \wedge ((v13_algstr_0\ X2) \wedge ((v3_rlvect_1 \\
& \quad \quad X2) \wedge ((v4_rlvect_1\ X2) \wedge (l2_algstr_0\ X2)))))) \Rightarrow (\forall X3.((v1_funct_1 \\
& \quad X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1 \\
& \quad \quad X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1 \\
& \quad \quad \quad (k15_pre_poly\ X0)\ (u1_struct_0\ X2))))))) \Rightarrow (\forall X4.((v1_funct_1 \\
& \quad X4) \wedge ((v1_funct_2\ X4\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1 \\
& \quad \quad X4\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1 \\
& \quad \quad \quad (k15_pre_poly\ X0)\ (u1_struct_0\ X2))))))) \Rightarrow (((k3_termord\ X0\ X1 \\
& \quad X2\ X3 = k3_termord\ X0\ X1\ X2\ X4) \wedge (r1_polyred\ X0\ X1\ X2\ (k6_termord\ X0 \\
& \quad X1\ X2\ X3)\ (k6_termord\ X0\ X1\ X2\ X4))) \Rightarrow ((X4 = k7_polynom1\ X0\ X2) \vee (r1_polyred \\
& \quad \quad X0\ X1\ X2\ X3\ X4))))))
\end{aligned}$$