

l79_funct_7

(TMMZ6mjt1MbaHHeUTQAvSEWLPZe383PHcMW)

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Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_numbers : \iota$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k9_setfam_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_relat_1 : \iota \Rightarrow \iota$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $r2_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_numbers : \iota$ be given. Let $k6_partfun1 : \iota \Rightarrow \iota$ be given. Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $k1_nat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $np_1 : \iota$ be given. Let $k3_relat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$m1_subset_1 \ k1_xboole_0 \ k4_ordinal1 \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o. \forall X2. \forall X3. \\ & \forall X4. ((k3_funct_2 \ k5_numbers \ X4 \ X3 \ k6_numbers = X2) \wedge ((\forall X5. \\ & (v7_ordinal1 \ X5) \Rightarrow (X1 \ X5 \ (k1_funct_1 \ X3 \ X5) \ (k3_funct_2 \ k5_numbers \\ & X4 \ X3 \ (k1_nat_1 \ X5 \ np_1)))))) \wedge ((k3_funct_2 \ k5_numbers \ X4 \ X0 \ k6_numbers = \\ & X2) \wedge ((\forall X5. (v7_ordinal1 \ X5) \Rightarrow (X1 \ X5 \ (k1_funct_1 \ X0 \ X5) \ (k3_funct_2 \\ & k5_numbers \ X4 \ X0 \ (k1_nat_1 \ X5 \ np_1)))))) \wedge (\forall X5. (v7_ordinal1 \\ & X5) \Rightarrow (\forall X6. (m1_subset_1 \ X6 \ X4) \Rightarrow (\forall X7. (m1_subset_1 \\ & X7 \ X4) \Rightarrow (\forall X8. (m1_subset_1 \ X8 \ X4) \Rightarrow (((X1 \ X5 \ X6 \ X7) \wedge (X1 \ X5 \ X6 \\ & X8)) \Rightarrow (X7 = X8)))))))))) \Rightarrow (r2_funct_2 \ k5_numbers \ X4 \ X3 \ X0) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((m1_subset_1 \ X2 \\ & (k1_zfmisc_1 \ (k2_zfmisc_1 \ X0 \ X1))) \wedge (m1_subset_1 \ X3 \ (k1_zfmisc_1 \\ & (k2_zfmisc_1 \ X0 \ X1)))) \Rightarrow ((r2_relset_1 \ X0 \ X1 \ X2 \ X3) \Leftrightarrow (X2 = X3)) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X1 (k1_zfmisc_1 X0))))\Rightarrow(\forall X2.(m2_subset_1 X2 X0 X1)\Leftrightarrow(m1_subset_1 X2 X1)) \quad (4)$$

Assume the following.

$$\forall X0.k9_setfam_1 X0 = k1_zfmisc_1 X0 \quad (5)$$

Assume the following.

$$k6_numbers = k1_xboole_0 \quad (6)$$

Assume the following.

$$k5_numbers = k4_ordinal1 \quad (7)$$

Assume the following.

$$(\neg v1_xboole_0 k4_ordinal1)\wedge(v3_ordinal1 k4_ordinal1) \quad (8)$$

Assume the following.

$$\forall X0.\neg v1_xboole_0 (k1_zfmisc_1 X0) \quad (9)$$

Assume the following.

$$\forall X0.m1_subset_1 (k9_setfam_1 X0) (k1_zfmisc_1 (k1_zfmisc_1 X0)) \quad (10)$$

Assume the following.

$$\forall X0.(v1_partfun1 (k6_partfun1 X0) X0)\wedge(m1_subset_1 (k6_partfun1 X0) (k1_zfmisc_1 (k2_zfmisc_1 X0 X0))) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.((\neg v1_xboole_0 X0)\wedge(((v1_funct_1 X2)\wedge((v1_funct_2 X2 X0 X1)\wedge(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))))))\wedge(m1_subset_1 X3 X0))\Rightarrow(m1_subset_1 (k3_funct_2 X0 X1 X2 X3) X1) \quad (12)$$

Theorem 1

$$\begin{aligned} & \forall X0.(v1_relat_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 k5_numbers) \Rightarrow \\ & (\forall X2.((v1_funct_1 X2) \wedge ((v1_funct_2 X2 k5_numbers (k9_setfam_1 \\ & (k2_zfmisc_1 (k1_relat_1 X0) (k1_relat_1 X0)))) \wedge (m1_subset_1 \\ & X2 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k9_setfam_1 (k2_zfmisc_1 \\ & (k1_relat_1 X0) (k1_relat_1 X0)))))))) \Rightarrow (\forall X3.((v1_funct_1 \\ & X3) \wedge ((v1_funct_2 X3 k5_numbers (k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 \\ & X0) (k1_relat_1 X0)))) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 \\ & k5_numbers (k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 X0) (k1_relat_1 \\ & X0)))))) \Rightarrow (((r2_relset_1 (k1_relat_1 X0) (k1_relat_1 X0) (k3_funct_2 \\ & k5_numbers (k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 X0) (k1_relat_1 \\ & X0))) X2 k6_numbers) (k6_partfun1 (k1_relat_1 X0))) \wedge ((\forall X4. \\ & (v7_ordinal1 X4) \Rightarrow (k3_funct_2 k5_numbers (k9_setfam_1 (k2_zfmisc_1 \\ & (k1_relat_1 X0) (k1_relat_1 X0))) X2 (k1_nat_1 X4 np_1) = k3_relat_1 \\ & X0 (k1_funct_1 X2 X4))) \wedge ((r2_relset_1 (k1_relat_1 X0) (k1_relat_1 \\ & X0) (k3_funct_2 k5_numbers (k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 \\ & X0) (k1_relat_1 X0))) X3 k6_numbers) (k6_partfun1 (k1_relat_1 \\ & X0))) \wedge (\forall X4.(v7_ordinal1 X4) \Rightarrow (k3_funct_2 k5_numbers (\\ & k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 X0) (k1_relat_1 X0))) X3 \\ & (k1_nat_1 X4 np_1) = k3_relat_1 X0 (k1_funct_1 X3 X4)))))) \Rightarrow (r2_funct_2 \\ & k5_numbers (k9_setfam_1 (k2_zfmisc_1 (k1_relat_1 X0) (k1_relat_1 \\ & X0))) X2 X3)))) \end{aligned}$$