

# l83\_o\_ring\_1

## (TMXBqCCKzj5ttzN7tCUSAzny3DkgopLmhwZ)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v12\_o\_ring\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finseq\_1 : \iota \Rightarrow o$  be given. Let  $k9\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_numbers : \iota$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k7\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $np\_0 : \iota$  be given. Let  $v1\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $m1\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k4\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v9\_o\_ring\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. \neg (X0 \in X1) \wedge ((m1\_subset\_1 X1 (k1\_zfmisc\_1 X2)) \wedge (v1\_xboole\_0 X2)) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finseq\_1 X1))) \Rightarrow ((X1 = k9\_finseq\_1 X0) \Leftrightarrow ((k3\_finseq\_1 X1 = np\_1) \wedge (k1\_funct\_1 X1 np\_1 = X0))) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (3)$$

Assume the following.

$$\forall X0.(v7\_ordinal1\ X0)\Rightarrow(\neg(r1\_xxreal\_0\ X0\ np\_1)\wedge((X0\neq k6\_numbers)\wedge(X0\neq np\_1))) \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1\ X0)\wedge((v1\_funct\_1\ X0)\wedge(v1\_finseq\_1\ X0)))\Rightarrow \\ (\forall X1.(v7\_ordinal1\ X1)\Rightarrow((X1\in k1\_relset\_1\ k5\_numbers\ X0)\Leftrightarrow \\ ((r1\_xxreal\_0\ np\_1\ X1)\wedge(r1\_xxreal\_0\ X1\ (k3\_finseq\_1\ X0)))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1\ X0)\wedge((v1\_funct\_1\ X0)\wedge(v1\_finseq\_1\ X0)))\Rightarrow \\ (\forall X1.((v1\_relat\_1\ X1)\wedge((v1\_funct\_1\ X1)\wedge(v1\_finseq\_1\ X1)))\Rightarrow \\ (k3\_finseq\_1\ (k7\_finseq\_1\ X0\ X1) = k2\_nat\_1\ (k3\_finseq\_1\ X0)\ (k3\_finseq\_1\ X1))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.(v7\_ordinal1\ X0)\Rightarrow(\forall X1.(v7\_ordinal1\ X1)\Rightarrow((\neg r1\_xxreal\_0\ (k1\_nat\_1\ X1\ np\_1)\ X0)\Leftrightarrow(r1\_xxreal\_0\ X0\ X1))) \quad (7)$$

Assume the following.

$$\forall X0.(v7\_ordinal1\ X0)\Rightarrow(\forall X1.(v7\_ordinal1\ X1)\Rightarrow(r1\_xxreal\_0\ X0\ (k2\_xcmplx\_0\ X0\ X1))) \quad (8)$$

Assume the following.

$$\begin{aligned} ((v2\_xxreal\_0\ np\_1)\wedge(m2\_subset\_1\ np\_1\ k1\_numbers\ k5\_numbers))\wedge \\ ((m1\_subset\_1\ np\_1\ k5\_numbers)\wedge(m1\_subset\_1\ np\_1\ k1\_numbers)) \end{aligned} \quad (9)$$

Assume the following.

$$(m2\_subset\_1\ np\_0\ k1\_numbers\ k5\_numbers)\wedge((m1\_subset\_1\ np\_0\ k5\_numbers)\wedge(m1\_subset\_1\ np\_0\ k1\_numbers)) \quad (10)$$

Assume the following.

$$k2\_xcmplx\_0\ np\_0\ np\_1 = np\_1 \quad (11)$$

Assume the following.

$$r1\_xxreal\_0\ np\_1\ np\_1 \quad (12)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0\ X0)\wedge(v1\_xxreal\_0\ X1))\Rightarrow(r1\_xxreal\_0\ X0\ X0) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))))\Rightarrow(\forall X2.(m2\_subset\_1 X2 X0 X1)\Leftrightarrow(m1\_subset\_1 X2 X1)) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.(m2\_finseq\_1 X1 X0)\Leftrightarrow(m1\_finseq\_1 X1 X0) \quad (15)$$

Assume the following.

$$\forall X0.k9\_finseq\_1 X0 = k5\_finseq\_1 X0 \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1\_finseq\_1 X1 X0)\wedge(m1\_finseq\_1 X2 X0))\Rightarrow(k8\_finseq\_1 X0 X1 X2 = k7\_finseq\_1 X1 X2) \quad (17)$$

Assume the following.

$$k6\_numbers = k1\_xboole\_0 \quad (18)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (19)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_finseq\_1 X0)))\Rightarrow(k4\_finseq\_1 X0 = k9\_xtuple\_0 X0) \quad (20)$$

Assume the following.

$$\forall X0.\forall X1.((m1\_subset\_1 X0 k5\_numbers)\wedge(v7\_ordinal1 X1))\Rightarrow(k2\_nat\_1 X0 X1 = k2\_xcmplx\_0 X0 X1) \quad (21)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1)\wedge(v4\_relat\_1 X1 X0))\Rightarrow(k1\_relset\_1 X0 X1 = k9\_xtuple\_0 X1) \quad (22)$$

Assume the following.

$$\forall X0.\forall X1.((v7\_ordinal1 X0)\wedge(m1\_subset\_1 X1 k5\_numbers))\Rightarrow(k1\_nat\_1 X0 X1 = k2\_xcmplx\_0 X0 X1) \quad (23)$$

Assume the following.

$$\begin{aligned} &\forall X0.(v7\_ordinal1 X0)\Rightarrow(\forall X1.(v7\_ordinal1 X1)\Rightarrow(\forall X2. \\ &((\neg v2\_struct\_0 X2)\wedge(l6\_algstr\_0 X2))\Rightarrow(\forall X3.(m2\_finseq\_1 \\ &X3 (u1\_struct\_0 X2))\Rightarrow(((v12\_oring\_1 X3 X2)\wedge((r1\_xxreal\_0 X0 \\ &(k3\_finseq\_1 X3))\wedge(r1\_xxreal\_0 X1 (k3\_finseq\_1 X3))))\Rightarrow((X0 = \\ &k6\_numbers)\vee((X1 = k6\_numbers)\vee(v12\_oring\_1 (k8\_finseq\_1 ( \\ &u1\_struct\_0 X2) X3 (k12\_finseq\_1 (u1\_struct\_0 X2) (k1\_algstr\_0 \\ &X2 (k7\_partfun1 (u1\_struct\_0 X2) X3 X0) (k7\_partfun1 (u1\_struct\_0 \\ &X2) X3 X1)))))) X2)))))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0\ X1) \wedge \\
& (l6\_algstr\_0\ X1)) \Rightarrow (\forall X2.(m2\_finseq\_1\ X2\ (u1\_struct\_0\ X1)) \Rightarrow \\
& (\forall X3.(m2\_finseq\_1\ X3\ (u1\_struct\_0\ X1)) \Rightarrow ((r1\_xxreal\_0 \\
& X0\ (k3\_finseq\_1\ X2)) \Rightarrow ((X0 = k6\_numbers) \vee (k7\_partfun1\ (u1\_struct\_0 \\
& X1)\ (k8\_finseq\_1\ (u1\_struct\_0\ X1)\ X3\ X2)\ (k2\_nat\_1\ (k3\_finseq\_1 \\
& X3)\ X0) = k7\_partfun1\ (u1\_struct\_0\ X1)\ X2\ X0))))))
\end{aligned} \tag{25}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0\ X0) \wedge (l6\_algstr\_0\ X0)) \Rightarrow (\forall X1. \\
& (m2\_finseq\_1\ X1\ (u1\_struct\_0\ X0)) \Rightarrow (\forall X2.(m2\_finseq\_1\ X2 \\
& (u1\_struct\_0\ X0)) \Rightarrow (((v12\_o\_ring\_1\ X1\ X0) \wedge (v12\_o\_ring\_1\ X2\ X0)) \Rightarrow \\
& (v12\_o\_ring\_1\ (k8\_finseq\_1\ (u1\_struct\_0\ X0)\ X1\ X2)\ X0))))
\end{aligned} \tag{26}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0\ X0) \wedge (l6\_algstr\_0\ X0)) \Rightarrow (\forall X1. \\
& (m2\_finseq\_1\ X1\ (u1\_struct\_0\ X0)) \Rightarrow (\forall X2.(m2\_finseq\_1\ X2 \\
& (u1\_struct\_0\ X0)) \Rightarrow (\forall X3.(m2\_finseq\_1\ X3\ (u1\_struct\_0\ X0)) \Rightarrow \\
& ((X1 = k8\_finseq\_1\ (u1\_struct\_0\ X0)\ X2\ X3) \Leftrightarrow ((k4\_finseq\_1\ X1 = k2\_finseq\_1 \\
& (k2\_nat\_1\ (k3\_finseq\_1\ X2)\ (k3\_finseq\_1\ X3))) \wedge ((\forall X4.( \\
& v7\_ordinal1\ X4) \Rightarrow ((X4 \in k4\_finseq\_1\ X2) \Rightarrow (k7\_partfun1\ (u1\_struct\_0 \\
& X0)\ X1\ X4 = k7\_partfun1\ (u1\_struct\_0\ X0)\ X2\ X4))) \wedge (\forall X4.(v7\_ordinal1 \\
& X4) \Rightarrow ((X4 \in k4\_finseq\_1\ X3) \Rightarrow (k7\_partfun1\ (u1\_struct\_0\ X0)\ X1\ (k2\_nat\_1 \\
& (k3\_finseq\_1\ X2)\ X4) = k7\_partfun1\ (u1\_struct\_0\ X0)\ X3\ X4))))))))))
\end{aligned} \tag{27}$$

Assume the following.

$$\forall X0.v1\_finseq\_1\ (k5\_finseq\_1\ X0) \tag{28}$$

Assume the following.

$$(\neg v1\_xboole\_0\ k4\_ordinal1) \wedge (v3\_ordinal1\ k4\_ordinal1) \tag{29}$$

Assume the following.

$$\forall X0.(v1\_relat\_1\ (k5\_finseq\_1\ X0)) \wedge (v1\_funct\_1\ (k5\_finseq\_1\ X0)) \tag{30}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.(m2\_finseq\_1\ X1\ X0) \Rightarrow ((v1\_funct\_1\ X1) \wedge \\
& (v1\_finseq\_1\ X1) \wedge (m1\_subset\_1\ X1\ (k1\_zfmisc\_1\ (k2\_zfmisc\_1\ k5\_numbers \\
& X0))))))
\end{aligned} \tag{31}$$

Assume the following.

$$\forall X0.\forall X1.(m1\_finseq\_1 X1 X0)\Rightarrow((v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1)\wedge(v1\_finseq\_1 X1)) \quad (32)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1\_finseq\_1 X1 X0)\wedge(m1\_finseq\_1 X2 X0))\Rightarrow(m2\_finseq\_1 (k8\_finseq\_1 X0 X1 X2) X0) \quad (33)$$

Assume the following.

$$m1\_subset\_1 k5\_numbers (k1\_zfmisc\_1 k1\_numbers) \quad (34)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_finseq\_1 X0)))\Rightarrow(m2\_subset\_1 (k3\_finseq\_1 X0) k1\_numbers k5\_numbers) \quad (35)$$

Assume the following.

$$\forall X0.\forall X1.((m1\_subset\_1 X0 k5\_numbers)\wedge(v7\_ordinal1 X1))\Rightarrow(m2\_subset\_1 (k2\_nat\_1 X0 X1) k1\_numbers k5\_numbers) \quad (36)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge(l6\_algstr\_0 X0))\Rightarrow(\forall X1. \\ & (m2\_finseq\_1 X1 (u1\_struct\_0 X0))\Rightarrow((v12\_oring\_1 X1 X0)\Leftrightarrow((k3\_finseq\_1 \\ & X1\neq k6\_numbers)\wedge(\forall X2.(v7\_ordinal1 X2)\Rightarrow(\neg(X2\neq k6\_numbers)\wedge \\ & ((r1\_xxreal\_0 X2 (k3\_finseq\_1 X1))\wedge((\neg v9\_oring\_1 (k7\_partfun1 \\ & (u1\_struct\_0 X0) X1 X2) X0)\wedge(\forall X3.(v7\_ordinal1 X3)\Rightarrow(\forall X4. \\ & (v7\_ordinal1 X4)\Rightarrow(\neg((k7\_partfun1 (u1\_struct\_0 X0) X1 X2 = k6\_algstr\_0 \\ & X0 (k7\_partfun1 (u1\_struct\_0 X0) X1 X3) (k7\_partfun1 (u1\_struct\_0 \\ & X0) X1 X4))\vee(k7\_partfun1 (u1\_struct\_0 X0) X1 X2 = k1\_algstr\_0 X0 \\ & (k7\_partfun1 (u1\_struct\_0 X0) X1 X3) (k7\_partfun1 (u1\_struct\_0 \\ & X0) X1 X4))))\wedge((X3\neq k6\_numbers)\wedge((\neg r1\_xxreal\_0 X2 X3)\wedge((X4\neq k6\_numbers)\wedge \\ & (\neg r1\_xxreal\_0 X2 X4)))))))))) \quad (37) \end{aligned}$$

Assume the following.

$$\forall X0.\forall X1.((m1\_subset\_1 X0 k5\_numbers)\wedge(v7\_ordinal1 X1))\Rightarrow(k2\_nat\_1 X0 X1 = k2\_nat\_1 X1 X0) \quad (38)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k4\_ordinal1)\Rightarrow(v7\_ordinal1 X0) \quad (39)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_finseq\_1 X0)))\Rightarrow \\ & ((v1\_relat\_1 X0)\wedge((v4\_relat\_1 X0 k5\_numbers)\wedge((v1\_funct\_1 X0)\wedge \\ & (v1\_finseq\_1 X0)))) \quad (40) \end{aligned}$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0) \Rightarrow (v1\_xxreal\_0 X0) \quad (41)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0) \Rightarrow (v1\_xreal\_0 X0) \quad (42)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (l6\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m2\_finseq\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m2\_finseq\_1 X2 \\ & (u1\_struct\_0 X0)) \Rightarrow (((v12\_oring\_1 X1 X0) \wedge (v12\_oring\_1 X2 X0)) \Rightarrow \\ & (v12\_oring\_1 (k8\_finseq\_1 (u1\_struct\_0 X0) (k8\_finseq\_1 (u1\_struct\_0 \\ & X0) X1 X2) (k12\_finseq\_1 (u1\_struct\_0 X0) (k1\_algstr\_0 X0) (k7\_partfun1 \\ & (u1\_struct\_0 X0) X1 (k3\_finseq\_1 X1)) (k7\_partfun1 (u1\_struct\_0 \\ & X0) X2 (k3\_finseq\_1 X2)))))) X0)))) \end{aligned}$$