# t103_member_1 (TMSNgqM99Zh71jMHgWNkE59TbhYrwp8cekC) 

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Let $v 2 \_$membered : $\iota \Rightarrow 0$ be given. Let $r 1 \_$tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 14 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 12 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow(\forall X 2 .\right. \\
\left(v 2 \_ \text {membered } X 2\right) \Rightarrow\left(\forall X 3 .\left(v 2 \_ \text {membered } X 3\right) \Rightarrow\left(\left(\left(r 1 \_\right.\right.\right. \text {tarski }\right. \\
\left.X 0 X 1) \wedge\left(r 1 \_t a r s k i X 2 X 3\right)\right) \Rightarrow\left(r 1 \_ t a r s k i ( k 1 2 \_ m e m b e r \_ 1 X 0 X 2 ) \left(k 12 \_m e m b e r \_1\right.\right. \\
X 1 X 3)))))) \tag{1}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 2 \_\right.$membered $\left.X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_\right.\right.$membered $\left.X 1\right) \Rightarrow(($
$r 1 \_$tarski $\left.X 0 X 1\right) \Rightarrow\left(r 1 \_\right.$tarski $\left.\left.\left.\left(k 6 \_m e m b e r \_1 X 0\right)\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right)\right)$

Assume the following.

$$
\left.\left.\begin{array}{rl}
\forall X 0 . \forall X 1 .\left(v 2 \_m e m b e r e d ~\right. & X 1) \Rightarrow  \tag{3}\\
& \left(\left(r 1 \_t a r s k i\right.\right. \\
X 0)
\end{array}\right) \quad X 1\right) \Rightarrow\left(v 2 \_\right. \text {membered }
$$

Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 6 \_m e m b e r \_1 X 0\right)\right)$
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 12 \_m e m b e r \_1 X 0\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right) \tag{5}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(\forall X 3 .\left(v 2 \_m e m b e r e d ~ X 3\right) \Rightarrow\left(\left(\left(r 1 \_t a r s k i\right.\right.\right.\right.$
X0 X1) $\wedge\left(r 1 \_\right.$tarski $\left.\left.X 2 X 3\right)\right) \Rightarrow\left(r 1 \_t a r s k i\left(k 14 \_m e m b e r \_1 X 0 X 2\right)\left(k 14 \_m e m b e r \_1\right.\right.$ X1 X3))))))

