# t105_member_1 <br> (TMStj8NsaTfpA3nwn5NeqWybWeceQHAHnuz) 

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Let v2_membered : $\iota \Rightarrow 0$ be given. Let r1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 14 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 3 \_$xboole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 12 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k6_member_1 : $\iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v2_membered $X 2) \Rightarrow\left(r 1 \_t a r s k i\left(k 12 \_m e m b e r \_1 ~ X 0 ~\left(k 3 \_x b o o l e \_0 ~ X 1 ~\right.\right.\right.$
X2)) (k3_xboole_0 (k12_member_1 X0 X1) (k12_member_1 X0 X2)))))
(1)

Assume the following.
$\forall X 0 . \forall X 1 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d ~\left(k 3 \_x b o o l e \_0\right.\right.$
$X 1 X 0))$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d ~\left(k 6 \_m e m b e r \_1 X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.\right.  \tag{4}\\
\left.\left.X 0 X 1=k 12 \_m e m b e r \_1 X 0\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right)
\end{gather*}
$$

Assume the following.
$\forall X 0 . \forall X 1 .\left(\left(v 2 \_m e m b e r e d ~ X 0\right) \wedge\left(v 2 \_\right.\right.$membered $\left.\left.X 1\right)\right) \Rightarrow($
$\left.k 12 \_m e m b e r \_1 X 0 X 1=k 12 \_m e m b e r \_1 X 1 X 0\right)$

## Theorem 1

$\forall X 0 .\left(v 2 \_\right.$membered $\left.X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_\right.\right.$membered $\left.X 1\right) \Rightarrow(\forall X 2$.
$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(r 1 \_\right.$tarski $\left(k 14 \_m e m b e r \_1\left(k 3 \_x b o o l e \_0 ~ X 0 ~ X 1\right) ~\right) ~$


