# t106_member_1 (TMSkPAEZTTHdVPcprfhvMa9YaSKJQwzG7CC) 

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Let $v 2 \_$membered : $\iota \Rightarrow 0$ be given. Let $k$ 14_member_1 $^{2} \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 2 \_x$ xoole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 12 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 12 \_m e m b e r \_1 X 0\left(k 2 \_x b o o l e \_0 X 1 X 2\right)=k 2 \_x b o o l e \_0\right.$
(k12_member_1 X0 X1) (k12_member_1 X0 X2))))
Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 2 \_\right.$membered $\left.X 1\right) \Rightarrow\left(k 6 \_m e m b e r \_1\right.$
( $k 2 \_x$ boole_0 X0 X1) $=k 2 \_x b o o l e \_0$ ( $k 6 \_$member_1 X0) (k6_member_1
X1)))
Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_ \text {membered } X 0\right) \wedge\left(v 2 \_ \text {membered } X 1\right)\right) \Rightarrow( \\
\left.v 2 \_m e m b e r e d ~\left(k 2 \_x b o o l e \_0 X 0 X 1\right)\right) \tag{3}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 6 \_m e m b e r \_1 X 0\right)\right)$
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 12 \_ \text {member_ } 1 X 0\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right) \tag{5}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v2_membered $X 2) \Rightarrow\left(k 14 \_m e m b e r \_1 ~ X 0\left(k 2 \_x b o o l e \_0 X 1 X 2\right)=k 2 \_x b o o l e \_0\right.$
(k14_member_1 X0 X1) (k14_member_1 X0 X2))))

