# t108_member_1 (TMdqoQmyYVbRdhVk4sKWqZrSvqPejdd4Hdo) 

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Let $v 2$ _membered $: \iota \Rightarrow 0$ be given. Let $k 14 \_$member_1 $: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k12_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k6_member_1 : $\iota \Rightarrow \iota$ be given. Assume the following

$$
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow(\forall X 2 \text {. }\right.
$$

$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 12 \_m e m b e r \_1\right.$ ( $\left.k 12 \_m e m b e r \_1 X 0 X 1\right) X 2=k 12 \_m e m b e r \_1$ X0 (k12_member_1 X1 X2))))

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_ \text {membered } X 0\right) \wedge\left(v 2 \_ \text {_membered } X 1\right)\right) \Rightarrow(  \tag{2}\\
\left.v 2 \_ \text {_membered }\left(k 12 \_m e m b e r \_1 X 0 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 6 \_m e m b e r \_1 X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 12 \_ \text {member_1 X0 }\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right) \tag{4}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 2 \_m e m b e r e d \quad X 2\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.$ ( $k 12 \_m e m b e r \_1 X 0 X 1$ ) X2 $=k 12 \_m e m b e r \_1$ X0 (k14_member_1 X1 X2))))

