# t109_member_1 (TMXaPyuvwxSeteB3pFxPGKCRGbPWW7AevVJ) 

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Let $v 2 \_$membered $: \iota \Rightarrow 0$ be given. Let $k 12 \_$member_ $1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 14 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 2 \_\right.$membered $\left.X 1\right) \Rightarrow(\forall X 2$.
$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 14 \_m e m b e r \_1\right.$ (k12_member_1 X0 X1) X2 $=k 12 \_m e m b e r \_1$ X0 (k14_member_1 X1 X2))))
(1)

Assume the following.
$\forall X 0 . \forall X 1 .\left(\left(v 2 \_m e m b e r e d \quad X 0\right) \wedge\left(v 2 \_\right.\right.$membered $\left.\left.X 1\right)\right) \Rightarrow($
$\left.v 2 \_m e m b e r e d ~\left(k 14 \_m e m b e r \_1 X 0 X 1\right)\right)$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_m e m b e r e d X 0\right) \wedge\left(v 2 \_ \text {membered } X 1\right)\right) \Rightarrow( \\
\left.k 12 \_m e m b e r \_1 X 0 X 1=k 12 \_m e m b e r \_1 X 1 X 0\right) \tag{3}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 2 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 12 \_m e m b e r \_1\right.$ ( $\left.k 14 \_m e m b e r \_1 X 0 X 1\right) X 2=k 14 \_m e m b e r \_1$ (k12_member_1 X0 X2) X1)))

