

t10_funct_6
(TMP4DzxKEEjv5UFPDHPa13nubYiM1iatBEt)

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Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $k1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k1_funct_5 : \iota \Rightarrow \iota$ be given. Let $k3_funct_5 : \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k10_xtuple_0 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. (r1_tarski X0 X1) \Rightarrow (r1_tarski (k1_funct_2 X2 X0) (k1_funct_2 X2 X1)) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((v1_relat_1 X2) \wedge (v1_funct_1 X2)) \Rightarrow ((k9_xtuple_0 X2 = k2_zfmisc_1 X0 X1) \Rightarrow ((r1_tarski (k10_xtuple_0 (k1_funct_5 X2)) (k1_funct_2 X1 (k10_xtuple_0 X2))) \wedge (r1_tarski (k10_xtuple_0 (k3_funct_5 X2)) (k1_funct_2 X0 (k10_xtuple_0 X2)))))) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((v1_relat_1 X2) \wedge (v1_funct_1 X2)) \Rightarrow ((k9_xtuple_0 X2 = k2_zfmisc_1 X0 X1) \Rightarrow ((k2_zfmisc_1 X0 X1 = k1_xboole_0) \vee ((k9_xtuple_0 (k1_funct_5 X2) = X0) \wedge (k9_xtuple_0 (k3_funct_5 X2) = X1)))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((r1_tarski X0 X1) \wedge (r1_tarski X1 X2)) \Rightarrow (r1_tarski X0 X2) \quad (4)$$

Assume the following.

$$\forall X0. ((v1_relat_1 X0) \wedge (v1_funct_1 X0)) \Rightarrow ((v1_relat_1 (k3_funct_5 X0)) \wedge (v1_funct_1 (k3_funct_5 X0))) \quad (5)$$

Assume the following.

$$\forall X0. ((v1_relat_1 X0) \wedge (v1_funct_1 X0)) \Rightarrow ((v1_relat_1 (k1_funct_5 X0)) \wedge (v1_funct_1 (k1_funct_5 X0))) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(X2 = k1_funct_2 X0 X1) \Leftrightarrow (\forall X3. \\ & (X3 \in X2) \Leftrightarrow (\exists X4.((v1_relat_1 X4) \wedge (v1_funct_1 X4)) \wedge ((X3 = \\ & X4) \wedge ((k9_xtuple_0 X4 = X0) \wedge (r1_tarski (k10_xtuple_0 X4) X1)))))) \end{aligned} \quad (7)$$

Theorem 1

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((v1_relat_1 X3) \wedge \\ & (v1_funct_1 X3)) \Rightarrow ((X3 \in k1_funct_2 (k2_zfmisc_1 X0 X1) X2) \Rightarrow ((k2_zfmisc_1 \\ & X0 X1 = k1_xboole_0) \vee ((k1_funct_5 X3 \in k1_funct_2 X0 (k1_funct_2 \\ & X1 X2)) \wedge (k3_funct_5 X3 \in k1_funct_2 X1 (k1_funct_2 X0 X2)))))) \end{aligned}$$