

## t10\_modcat\_1

(TMaKn6U239TGAJt9poFHapDy8H2Xh9hcvRi)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_modcat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m4\_modcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_modcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_mod\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_mod\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_mod\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_modcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_modcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\ & X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge ( \\ & (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0)))))))) \Rightarrow \\ & (\forall X1. (m1\_modcat\_1 X1 X0) \Rightarrow (\forall X2. (m4\_modcat\_1 X2 X0 \\ & (k4\_modcat\_1 X0 X1) \Rightarrow (\forall X3. (m4\_modcat\_1 X3 X0 (k4\_modcat\_1 \\ & X0 X1) \Rightarrow ((k5\_modcat\_1 X0 X1 X2 = k6\_modcat\_1 X0 X1 X3) \Rightarrow (k8\_mod\_2 \\ & X0 X2 X3 \in k4\_modcat\_1 X0 X1)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\ & X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge ( \\ & (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0)))))))) \Rightarrow \\ & (\forall X1. (m1\_modcat\_1 X1 X0) \Rightarrow (\forall X2. (m4\_modcat\_1 X2 X0 \\ & (k4\_modcat\_1 X0 X1) \Rightarrow (k6\_modcat\_1 X0 X1 X2 = k3\_mod\_2 X0 X2))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\ & X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge ( \\ & (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0)))))))) \Rightarrow \\ & (\forall X1. (m1\_modcat\_1 X1 X0) \Rightarrow (\forall X2. (m4\_modcat\_1 X2 X0 \\ & (k4\_modcat\_1 X0 X1) \Rightarrow (k5\_modcat\_1 X0 X1 X2 = k2\_mod\_2 X0 X2))) \end{aligned} \tag{3}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (v13\_algstr\_0 X0) \wedge (v2\_rlvect\_1 \\ & X0) \wedge (v3\_rlvect\_1 X0) \wedge (v4\_rlvect\_1 X0) \wedge (v3\_group\_1 X0) \wedge \\ & (v4\_vectsp\_1 X0) \wedge (v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0)))))) \Rightarrow \\ & (\forall X1.(m1\_modcat\_1 X1 X0) \Rightarrow (\forall X2.(m4\_modcat\_1 X2 X0 \\ & (k4\_modcat\_1 X0 X1)) \Rightarrow (\forall X3.(m4\_modcat\_1 X3 X0 (k4\_modcat\_1 \\ X0 X1)) \Rightarrow ((k2\_mod\_2 X0 X2 = k3\_mod\_2 X0 X3) \Rightarrow (k8\_mod\_2 X0 X2 X3 \in k4\_modcat\_1 \\ X0 X1)))))) \end{aligned}$$