

## t119\_funct\_2

(TMQCFVw66xTLJuanmcLWZqqCYU4Un6DpX79)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $k1\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (1)$$

Assume the following.

$$\forall X0.\forall X1.(v1\_relat\_1 X1) \Rightarrow ((X0 \in X1) \Rightarrow (X0 = k4\_tarski (k1\_xtuple\_0 X0) (k2\_xtuple\_0 X0))) \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0) \wedge \\ & (((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1)))))) \wedge (m1\_subset\_1 X3 X0))) \Rightarrow (k3\_funct\_2 X0 \\ & X1 X2 X3 = k1\_funct\_1 X2 X3) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.v1\_relat\_1 (k2\_zfmisc\_1 X0 X1) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge (\neg v1\_xboole\_0 X1)) \Rightarrow (\neg v1\_xboole\_0 (k2\_zfmisc\_1 X0 X1)) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge \\ & ((\neg v1\_xboole\_0 X1)\wedge((\neg v1\_xboole\_0 X2)\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 \\ & X3 X0 (k2\_zfmisc\_1 X1 X2))\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 (k2\_zfmisc\_1 X1 X2))))))))))\Rightarrow((v1\_funct\_1 (k5\_funct\_2 X0 X1 \\ & X2 X3)\wedge((v1\_funct\_2 (k5\_funct\_2 X0 X1 X2 X3) X0 X2)\wedge(m1\_subset\_1 \\ & (k5\_funct\_2 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X2)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge \\ & ((\neg v1\_xboole\_0 X1)\wedge((\neg v1\_xboole\_0 X2)\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 \\ & X3 X0 (k2\_zfmisc\_1 X1 X2))\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 (k2\_zfmisc\_1 X1 X2))))))))))\Rightarrow((v1\_funct\_1 (k4\_funct\_2 X0 X1 \\ & X2 X3)\wedge((v1\_funct\_2 (k4\_funct\_2 X0 X1 X2 X3) X0 X1)\wedge(m1\_subset\_1 \\ & (k4\_funct\_2 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge \\ & (((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1))))))\wedge(m1\_subset\_1 X3 X0))\Rightarrow(m1\_subset\_1 ( \\ & k3\_funct\_2 X0 X1 X2 X3) X1) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(\neg v1\_xboole\_0 X1)\Rightarrow \\ & (\forall X2.(\neg v1\_xboole\_0 X2)\Rightarrow(\forall X3.((v1\_funct\_1 X3)\wedge \\ & ((v1\_funct\_2 X3 X0 (k2\_zfmisc\_1 X1 X2))\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 (k2\_zfmisc\_1 X1 X2))))))\Rightarrow(\forall X4.((v1\_funct\_1 \\ & X4)\wedge((v1\_funct\_2 X4 X0 X2)\wedge(m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X2))))))\Rightarrow((X4 = k5\_funct\_2 X0 X1 X2 X3)\Leftrightarrow(\forall X5.(m1\_subset\_1 \\ & X5 X0)\Rightarrow(k3\_funct\_2 X0 X2 X4 X5 = k2\_xtuple\_0 (k3\_funct\_2 X0 (k2\_zfmisc\_1 \\ & X1 X2) X3 X5)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.k4\_tarski X0 X1 = k2\_tarski (k2\_tarski X0 X1) (k1\_tarski X0) \quad (10)$$

Assume the following.

$$\begin{aligned}
& \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.(\neg v1\_xboole\_0 X1) \Rightarrow \\
& \quad (\forall X2.(\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge \\
& \quad ((v1\_funct\_2 X3 X0 (k2\_zfmisc\_1 X1 X2)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 X0 (k2\_zfmisc\_1 X1 X2)))))) \Rightarrow (\forall X4.((v1\_funct\_1 \\
& \quad X4) \wedge ((v1\_funct\_2 X4 X0 X1) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad X0 X1)))))) \Rightarrow ((X4 = k4\_funct\_2 X0 X1 X2 X3) \Leftrightarrow (\forall X5.(m1\_subset\_1 \\
& \quad X5 X0) \Rightarrow (k3\_funct\_2 X0 X1 X4 X5 = k1\_xtuple\_0 (k3\_funct\_2 X0 (k2\_zfmisc\_1 \\
& \quad X1 X2) X3 X5)))))))))
\end{aligned} \tag{11}$$

Assume the following.

$$\forall X0.\forall X1.k2\_tarSKI X0 X1 = k2\_tarSKI X1 X0 \tag{12}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.(\neg v1\_xboole\_0 X1) \Rightarrow \\
& \quad (\forall X2.(\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge \\
& \quad ((v1\_funct\_2 X3 X0 (k2\_zfmisc\_1 X1 X2)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 X0 (k2\_zfmisc\_1 X1 X2)))))) \Rightarrow (\forall X4.(m1\_subset\_1 \\
& \quad X4 X0) \Rightarrow (k3\_funct\_2 X0 (k2\_zfmisc\_1 X1 X2) X3 X4 = k4\_tarSKI (k3\_funct\_2 \\
& \quad X0 X1 (k4\_funct\_2 X0 X1 X2 X3) X4) (k3\_funct\_2 X0 X2 (k5\_funct\_2 X0 \\
& \quad X1 X2 X3) X4))))))
\end{aligned}$$