

# t11\_ens\_1 (TMH- Bqm7BGQhhca6g7p1wDj56ZEGWA8Ljm6s)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k5\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_partfun1 : \iota \Rightarrow \iota$  be given. Let  $k3\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarSKI : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_ens\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\ & ((\neg v1\_xboole\_0 X1) \wedge ((m1\_subset\_1 X2 X0) \wedge (m1\_subset\_1 X3 X1)))) \Rightarrow \\ & (k1\_domain\_1 X0 X1 X2 X3 = k4\_tarSKI X2 X3) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. k2\_xtuple\_0 (k4\_tarSKI X0 X1) = X1 \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. k1\_xtuple\_0 (k4\_tarSKI X0 X1) = X0 \tag{3}$$

Assume the following.

$$\forall X0. \neg v1\_xboole\_0 (k1\_zfmisc\_1 X0) \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge (\neg v1\_xboole\_0 X1)) \Rightarrow \\ & (\neg v1\_xboole\_0 (k2\_zfmisc\_1 X0 X1)) \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0. (v1\_partfun1 (k6\_partfun1 X0) X0) \wedge (m1\_subset\_1 (k6\_partfun1 \\ & X0) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))) \end{aligned} \tag{6}$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge(m1\_subset\_1 X1 X0))\Rightarrow (m1\_subset\_1 (k5\_ens\_1 X0 X1) (k2\_ens\_1 X0)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge((m1\_subset\_1 X2 X0)\wedge(m1\_subset\_1 X3 X1))))\Rightarrow (m1\_subset\_1 (k1\_domain\_1 X0 X1 X2 X3) (k2\_zfmisc\_1 X0 X1)) \quad (8)$$

Assume the following.

$$\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow(k5\_ens\_1 X0 X1 = k1\_domain\_1 (k2\_zfmisc\_1 X0 X0) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 X1)) (k1\_domain\_1 X0 X0 X1 X1) (k6\_partfun1 X1))) \quad (9)$$

Assume the following.

$$\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k2\_ens\_1 X0))\Rightarrow(k4\_ens\_1 X0 X1 = k2\_xtuple\_0 (k1\_xtuple\_0 X1))) \quad (10)$$

Assume the following.

$$\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k2\_ens\_1 X0))\Rightarrow(k3\_ens\_1 X0 X1 = k1\_xtuple\_0 (k1\_xtuple\_0 X1))) \quad (11)$$

**Theorem 1**

$$\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow((k2\_xtuple\_0 (k5\_ens\_1 X0 X1) = k6\_partfun1 X1)\wedge((k3\_ens\_1 X0 (k5\_ens\_1 X0 X1) = X1)\wedge(k4\_ens\_1 X0 (k5\_ens\_1 X0 X1) = X1))))$$