# t11_member_1 (TMWHPhBujUMkWmoEUobkzQiZguszv4E775A) 

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Let $v 1_{\_}$membered : $\iota \Rightarrow 0$ be given. Let $v 1 \_x c m p l x_{-} 0: \iota \Rightarrow o$ be given. Let $k 1 \_b i n o p \_2: \iota \Rightarrow \iota$ be given. Let $k 5$ _member_1 $: \iota \Rightarrow \iota$ be given. Let m1_subset_1: $\iota \Rightarrow \iota \Rightarrow o$ be given. Let $k 2 \_n u m b e r s: \iota$ be given. Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(k 5 \_m e m b e r \_1\left(k 5 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{1}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(k 1 \_b i n o p \_2\left(k 1 \_b i n o p \_2 X 0\right)=X 0\right) \tag{2}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gathered}
\forall X 0 .(v 1 \text { _membered } X 0) \Rightarrow\left(k 5 \_ \text {_member_1 } X 0=\text { ReplSep }(\text { toset }( \right. \\
\left.\left.\lambda X 1: \iota . m 1 \_ \text {subset_1 X1 k2_numbers }\right)\right)(\lambda X 1: \iota . X 1 \in X 0)( \\
\left.\left.\lambda X 1: \iota . k 1 \_ \text {binop_2 } X 1\right)\right)
\end{gathered}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Leftrightarrow\left(\forall X 1 .(X 1 \in X 0) \Rightarrow\left(v 1 \_x c m p l x \_0 X 1\right)\right) \tag{5}
\end{equation*}
$$

## Theorem 1

$$
\begin{aligned}
& \forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(( \right. \\
& \left.\left.\quad X 1 \in X 0) \Leftrightarrow\left(k 1 \_b i n o p \_2 X 1 \in k 5 \_m e m b e r \_1 X 0\right)\right)\right)
\end{aligned}
$$

