

t11_metric_3

(TMaRiMjqDEpgN77WHWMDmyZ3fB7poZfUPnT)

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Let $v2_struct.0 : \iota \Rightarrow o$ be given. Let $v6_metric.1 : \iota \Rightarrow o$ be given. Let $v7_metric.1 : \iota \Rightarrow o$ be given. Let $v8_metric.1 : \iota \Rightarrow o$ be given. Let $v9_metric.1 : \iota \Rightarrow o$ be given. Let $l1_metric.1 : \iota \Rightarrow o$ be given. Let $m1_subset.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u1_struct.0 : \iota \Rightarrow \iota$ be given. Let $k1_metric.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_metric.3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole.0 : \iota$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xtuple.0 : \iota \Rightarrow \iota$ be given. Let $k2_xtuple.0 : \iota \Rightarrow \iota$ be given. Let $v1_xboole.0 : \iota \Rightarrow o$ be given. Let $k3_domain.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_domain.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_domain.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $l1_struct.0 : \iota \Rightarrow o$ be given. Let $v1_funct.1 : \iota \Rightarrow o$ be given. Let $v1_funct.2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $k1_zfmisc.1 : \iota \Rightarrow \iota$ be given. Let $k7_square.1 : \iota \Rightarrow \iota$ be given. Let $k7_real.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_square.1 : \iota \Rightarrow \iota$ be given. Let $k4_metric.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \neg (X0 \neq k1_xboole.0) \wedge ((X1 \neq k1_xboole.0) \wedge \\ & (\neg \forall X2. (m1_subset.1 X2 (k2_zfmisc.1 X0 X1)) \Rightarrow (X2 = k4_tarski \\ & (k1_xtuple.0 X2) (k2_xtuple.0 X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1_xboole.0 X0) \wedge ((\neg v1_xboole.0 \\ & X1) \wedge (m1_subset.1 X2 (k2_zfmisc.1 X0 X1)))) \Rightarrow (k3_domain.1 X0 X1 \\ & X2 = k2_xtuple.0 X2) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1_xboole.0 X0) \wedge ((\neg v1_xboole.0 \\ & X1) \wedge (m1_subset.1 X2 (k2_zfmisc.1 X0 X1)))) \Rightarrow (k2_domain.1 X0 X1 \\ & X2 = k1_xtuple.0 X2) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1_xboole.0 X0) \wedge \\ & ((\neg v1_xboole.0 X1) \wedge ((m1_subset.1 X2 X0) \wedge (m1_subset.1 X3 X1)))) \Rightarrow \\ & (k1_domain.1 X0 X1 X2 X3 = k4_tarski X2 X3) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.((\neg v2_struct_0 X0)\wedge(l1_struct_0 X0))\Rightarrow(\neg v1_xboole_0 (u1_struct_0 X0)) \quad (5)$$

Assume the following.

$$v1_xboole_0 k1_xboole_0 \quad (6)$$

Assume the following.

$$\forall X0.(l1_metric_1 X0)\Rightarrow(l1_struct_0 X0) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X2 (k2_zfmisc_1 X0 X1))))\Rightarrow(m1_subset_1 (k3_domain_1 X0 X1 X2) X1) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X2 (k2_zfmisc_1 X0 X1))))\Rightarrow(m1_subset_1 (k2_domain_1 X0 X1 X2) X0) \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0 X0)\wedge((v6_metric_1 X0)\wedge \\ & ((v7_metric_1 X0)\wedge(v8_metric_1 X0)\wedge((v9_metric_1 X0)\wedge(l1_metric_1 \\ & X0))))))\wedge((\neg v2_struct_0 X1)\wedge((v6_metric_1 X1)\wedge((v7_metric_1 \\ & X1)\wedge((v8_metric_1 X1)\wedge((v9_metric_1 X1)\wedge(l1_metric_1 X1))))))\Rightarrow \\ & ((v1_funct_1 (k10_metric_3 X0 X1))\wedge((v1_funct_2 (k10_metric_3 \\ & X0 X1) (k2_zfmisc_1 (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\ & X1)) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X1))) k1_numbers)\wedge \\ & (m1_subset_1 (k10_metric_3 X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 (\\ & k2_zfmisc_1 (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X1)) (\\ & k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X1))) k1_numbers)))))) \quad (10) \end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((v6_metric_1 X0) \wedge ((v7_metric_1 \\
& X0) \wedge ((v8_metric_1 X0) \wedge ((v9_metric_1 X0) \wedge (l1_metric_1 X0)))))) \Rightarrow \\
& (\forall X1.((\neg v2_struct_0 X1) \wedge ((v6_metric_1 X1) \wedge ((v7_metric_1 \\
& X1) \wedge ((v8_metric_1 X1) \wedge ((v9_metric_1 X1) \wedge (l1_metric_1 X1)))))) \Rightarrow \\
& (\forall X2.((v1_funct_1 X2) \wedge ((v1_funct_2 X2 (k2_zfmisc_1 (k2_zfmisc_1 \\
& (u1_struct_0 X0) (u1_struct_0 X1)) (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1))) k1_numbers) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\
& (k2_zfmisc_1 (k2_zfmisc_1 (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\
& X1)) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X1))) k1_numbers)))))) \Rightarrow \\
& ((X2 = k10_metric_3 X0 X1) \Leftrightarrow (\forall X3.(m1_subset_1 X3 (u1_struct_0 \\
& X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (u1_struct_0 X0)) \Rightarrow (\forall X5. \\
& (m1_subset_1 X5 (u1_struct_0 X1)) \Rightarrow (\forall X6.(m1_subset_1 X6 \\
& (u1_struct_0 X1)) \Rightarrow (\forall X7.(m1_subset_1 X7 (k2_zfmisc_1 (\\
& u1_struct_0 X0) (u1_struct_0 X1))) \Rightarrow (\forall X8.(m1_subset_1 \\
& X8 (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X1))) \Rightarrow (((X7 = k1_domain_1 \\
& (u1_struct_0 X0) (u1_struct_0 X1) X3 X5) \wedge (X8 = k1_domain_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1) X4 X6)) \Rightarrow (k1_metric_1 (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1)) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\
& X1)) X2 X7 X8 = k7_square_1 (k7_real_1 (k5_square_1 (k4_metric_1 \\
& X0 X3 X4)) (k5_square_1 (k4_metric_1 X1 X5 X6))))))))))))) \Rightarrow \\
& \hspace{10em} (11)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((v8_metric_1 X0) \wedge (l1_metric_1 \\
& X0)) \wedge ((m1_subset_1 X1 (u1_struct_0 X0)) \wedge (m1_subset_1 X2 (u1_struct_0 \\
& X0)))) \Rightarrow (k4_metric_1 X0 X1 X2 = k4_metric_1 X0 X2 X1) \\
& \hspace{10em} (12)
\end{aligned}$$

Theorem 1

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((v6_metric_1 X0) \wedge ((v7_metric_1 \\
& X0) \wedge ((v8_metric_1 X0) \wedge ((v9_metric_1 X0) \wedge (l1_metric_1 X0)))))) \Rightarrow \\
& (\forall X1.((\neg v2_struct_0 X1) \wedge ((v6_metric_1 X1) \wedge ((v7_metric_1 \\
& X1) \wedge ((v8_metric_1 X1) \wedge ((v9_metric_1 X1) \wedge (l1_metric_1 X1)))))) \Rightarrow \\
& (\forall X2.(m1_subset_1 X2 (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\
& X1))) \Rightarrow (\forall X3.(m1_subset_1 X3 (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1))) \Rightarrow (k1_metric_1 (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1)) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\
& X1)) (k10_metric_3 X0 X1) X2 X3 = k1_metric_1 (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X1)) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 \\
& X1)) (k10_metric_3 X0 X1) X3 X2))))))
\end{aligned}$$