

# t11\_mod\_4 (TMJXxUT- Phk3gHcyvq14vZAbfYjKYqmhaT3E)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l1\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_mod\_4 : \iota \Rightarrow \iota$  be given. Let  $k3\_mod\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_binop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_mod\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_mod\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_binop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v36\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_algstr\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. (\neg v1\_xboole\_0 X1) \Rightarrow \\
& \quad (\forall X2. (\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3. ((v1\_funct\_1 X3) \wedge \\
& \quad ((v1\_funct\_2 X3 (k2\_zfmisc\_1 X1 X2) X0) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 (k2\_zfmisc\_1 X1 X2) X0)))))) \Rightarrow (\forall X4. (m1\_subset\_1 \\
& \quad X4 X1) \Rightarrow (\forall X5. (m1\_subset\_1 X5 X2) \Rightarrow (k2\_binop\_1 X1 X2 X0 X3 X4 \\
& \quad X5 = k2\_binop\_1 X2 X1 X0 (k1\_mod\_4 X1 X2 X0 X3) X5 X4))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. \forall X5. \\
& \quad ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge (((v1\_funct\_1 X3) \wedge (( \\
& \quad v1\_funct\_2 X3 (k2\_zfmisc\_1 X0 X1) X2) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1) X2)))))) \wedge ((m1\_subset\_1 X4 X0) \wedge \\
& \quad (m1\_subset\_1 X5 X1)))))) \Rightarrow (k2\_binop\_1 X0 X1 X2 X3 X4 X5 = k1\_binop\_1 \\
& \quad X3 X4 X5)
\end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\exists X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)) \wedge (\neg v1\_xboole\_0 X1)) \tag{3}$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 (u1\_struct\_0 X0)) \quad (4)$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0) \wedge (l6\_algstr\_0 X0)) \Rightarrow ((\neg v2\_struct\_0 (k2\_mod\_4 X0)) \wedge (v36\_algstr\_0 (k2\_mod\_4 X0))) \quad (5)$$

Assume the following.

$$\forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge (\neg v1\_xboole\_0 X1)) \Rightarrow (\neg v1\_xboole\_0 (k2\_zfmisc\_1 X0 X1)) \quad (6)$$

Assume the following.

$$\forall X0. (l6\_algstr\_0 X0) \Rightarrow ((l2\_algstr\_0 X0) \wedge (l5\_algstr\_0 X0)) \quad (7)$$

Assume the following.

$$\forall X0. (l2\_struct\_0 X0) \Rightarrow (l1\_struct\_0 X0) \quad (8)$$

Assume the following.

$$\forall X0. (l2\_algstr\_0 X0) \Rightarrow ((l2\_struct\_0 X0) \wedge (l1\_algstr\_0 X0)) \quad (9)$$

Assume the following.

$$\forall X0. (l1\_struct\_0 X0) \Rightarrow (\forall X1. (l1\_vectsp\_1 X1 X0) \Rightarrow (l2\_algstr\_0 X1)) \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge (l6\_algstr\_0 X0)) \wedge (((\neg v2\_struct\_0 X1) \wedge (l1\_vectsp\_1 X1 X0)) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)) (u1\_struct\_0 X1)))))) \Rightarrow ((v1\_funct\_1 (k4\_mod\_4 X0 X1 X2)) \wedge ((v1\_funct\_2 (k4\_mod\_4 X0 X1 X2) (k2\_zfmisc\_1 (u1\_struct\_0 (k3\_mod\_4 X0 X1)) (u1\_struct\_0 (k2\_mod\_4 X0))) (u1\_struct\_0 (k3\_mod\_4 X0 X1))) \wedge (m1\_subset\_1 (k4\_mod\_4 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 (k3\_mod\_4 X0 X1)) (u1\_struct\_0 (k2\_mod\_4 X0))) (u1\_struct\_0 (k3\_mod\_4 X0 X1)))))))))) \quad (11) \end{aligned}$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge (l6\_algstr\_0 X0)) \Rightarrow ((v36\_algstr\_0 (k2\_mod\_4 X0)) \wedge (l6\_algstr\_0 (k2\_mod\_4 X0))) \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge \\ & ((\neg v1\_xboole\_0 X1)\wedge((\neg v1\_xboole\_0 X2)\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 \\ & X3 (k2\_zfmisc\_1 X0 X1) X2)\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1) X2))))))))\Rightarrow((v1\_funct\_1 (k1\_mod\_4 X0 X1 X2 \\ & X3))\wedge((v1\_funct\_2 (k1\_mod\_4 X0 X1 X2 X3) (k2\_zfmisc\_1 X1 X0) X2)\wedge \\ & (m1\_subset\_1 (k1\_mod\_4 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 X1 X0) X2)))))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge(l6\_algstr\_0 X0))\Rightarrow(\forall X1. \\ & ((\neg v2\_struct\_0 X1)\wedge(l1\_vectsp\_1 X1 X0))\Rightarrow(\forall X2.((v1\_funct\_1 \\ & X2)\wedge((v1\_funct\_2 X2 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X1)) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)) (u1\_struct\_0 \\ & X1))))))\Rightarrow(k4\_mod\_4 X0 X1 X2 = k1\_mod\_4 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X1) (u1\_struct\_0 X1) X2))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge(\neg v1\_xboole\_0 X1))\Rightarrow \\ & (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow \\ & (((v1\_funct\_1 X2)\wedge(v1\_funct\_2 X2 X0 X1))\Rightarrow((v1\_funct\_1 X2)\wedge(( \\ & \neg v1\_xboole\_0 X2)\wedge(v1\_funct\_2 X2 X0 X1)))))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v1\_xboole\_0 X0)\Rightarrow(\forall X2.(m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 X0)))\Rightarrow(v1\_xboole\_0 X2)) \end{aligned} \quad (16)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0)\Rightarrow(v1\_funct\_1 X0) \quad (17)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge(l6\_algstr\_0 X0))\Rightarrow(\forall X1. \\ & ((\neg v2\_struct\_0 X1)\wedge(l1\_vectsp\_1 X1 X0))\Rightarrow(\forall X2.((v1\_funct\_1 \\ & X2)\wedge((v1\_funct\_2 X2 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X1)) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)) (u1\_struct\_0 \\ & X1))))))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(\forall X4. \\ & (m1\_subset\_1 X4 (u1\_struct\_0 (k2\_mod\_4 X0)))\Rightarrow(\forall X5.(m1\_subset\_1 \\ & X5 (u1\_struct\_0 X1))\Rightarrow(\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 \\ & (k3\_mod\_4 X0 X1)))\Rightarrow(((X3 = X4)\wedge(X5 = X6))\Rightarrow(k2\_binop\_1 (u1\_struct\_0 \\ & (k3\_mod\_4 X0 X1)) (u1\_struct\_0 (k2\_mod\_4 X0)) (u1\_struct\_0 (k3\_mod\_4 \\ & X0 X1)) (k4\_mod\_4 X0 X1 X2) X6 X4 = k2\_binop\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X1) (u1\_struct\_0 X1) X2 X3 X5)))))) \end{aligned}$$