# t121_member_1 <br> (TMNv5iDmpNU5nyEtY8iBrveACVkE2rEq2qK) 

October 27, 2020

Let $v$ 1_membered : $\iota \Rightarrow 0$ be given. Let $k$ 15_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5$ _member_1 : $\iota \Rightarrow \iota$ be given. Let $k 13 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 7$ _member_1 : $\iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 13 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0\left(k 5 \_m e m b e r \_1 X 1\right)=k 5 \_m e m b e r \_1\left(k 13 \_m e m b e r \_1 X 0 X 1\right)\right)\right) \tag{1}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right) \tag{2}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1 X 0\left(k 7 \_m e m b e r \_1 X 1\right)\right)\right) \tag{4}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow(  \tag{5}\\
\left.k 13 \_m e m b e r \_1 X 0 X 1=k 13 \_m e m b e r \_1 X 1 X 0\right)
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right.$
$\left.\left.\left(k 5 \_m e m b e r \_1 X 0\right) X 1=k 5 \_m e m b e r \_1\left(k 15 \_m e m b e r \_1 X 0 X 1\right)\right)\right)$

