## t123 member_1 <br> (TMYKocWbpj2BJdt4k5bEHsyTdgE1xXp1cef)

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Let $v 1 \_$membered $: \iota \Rightarrow 0$ be given. Let $r$ 1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 15 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 11 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k9_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k5_member_1: $\iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.

X2) (k9_member_1 (k15_member_1 X0 X2) (k15_member_1 X1 X2)))))
Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right.$
$\left.\left.\quad\left(k 5 \_m e m b e r \_1 X 0\right) X 1=k 5 \_m e m b e r \_1\left(k 15 \_m e m b e r \_1 X 0 X 1\right)\right)\right)$

Assume the following.
$\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d \quad X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow($
$\left.v 1 \_m e m b e r e d ~\left(k 15 \_m e m b e r \_1 X 0 X 1\right)\right)$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1 X 0\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right) \tag{5}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v1_membered X2) $\Rightarrow\left(r 1 \_\right.$tarski $\left(k 15 \_m e m b e r \_1\right.$ ( $k 11 \_$member_1 X0 X1)
X2) (k11_member_1 (k15_member_1 X0 X2) (k15_member_1 X1 X2)))))

