

# t12\_groeb\_3 (TMUYTuhdPp- pRvNUFCgq8JK829jPmtxWxtAJ)

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Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v5\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k15\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k4\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_vfunct\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_algstr\_1 : \iota \Rightarrow o$  be given. Let  $l2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v4\_algstr\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v13\_algstr\_0 X1) \wedge \\
& ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 X1) \wedge (l2\_algstr\_0 X1)))) \Rightarrow ( \\
& \forall X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k15\_pre\_poly X0) \\
& (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow ((r2\_funct\_2 (k15\_pre\_poly \\
& X0) (u1\_struct\_0 X1) (k4\_polynom1 X0 X1) (k5\_vfunct\_1 (k15\_pre\_poly \\
& X0) X1 X2) X2) (k7\_polynom1 X0 X1)) \wedge (r2\_funct\_2 (k15\_pre\_poly X0) \\
& (u1\_struct\_0 X1) (k4\_polynom1 X0 X1 X2) (k5\_vfunct\_1 (k15\_pre\_poly \\
& X0) X1 X2)) (k7\_polynom1 X0 X1)))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v1\_algstr\_1 X1) \wedge \\ & (l2\_algstr\_0 X1))) \Rightarrow (\forall X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 \\ & X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow (r2\_funct\_2 \\ & (k15\_pre\_poly X0) (u1\_struct\_0 X1) (k4\_polynom1 X0 X1 (k7\_polynom1 \\ & X0 X1) X2) X2)) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v4\_rlvect\_1 X1) \wedge \\ & (l2\_algstr\_0 X1))) \Rightarrow (\forall X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 \\ & X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow (r2\_funct\_2 \\ & (k15\_pre\_poly X0) (u1\_struct\_0 X1) (k4\_polynom1 X0 X1 X2 (k7\_polynom1 \\ & X0 X1) X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v3\_rlvect\_1 X1) \wedge \\ & ((v4\_rlvect\_1 X1) \wedge (l6\_algstr\_0 X1)))) \Rightarrow (\forall X2. ((v1\_funct\_1 \\ & X2) \wedge ((v1\_funct\_2 X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow \\ & (\forall X3. ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (k15\_pre\_poly X0) \\ & (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow (\forall X4. ((v1\_funct\_1 \\ & X4) \wedge ((v1\_funct\_2 X4 (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 \\ & X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \Rightarrow \\ & (r2\_funct\_2 (k15\_pre\_poly X0) (u1\_struct\_0 X1) (k4\_polynom1 X0 \\ & X1 (k4\_polynom1 X0 X1 X2 X3) X4) (k4\_polynom1 X0 X1 X2 (k4\_polynom1 \\ & X0 X1 X3 X4)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((v1\_funct\_1 X2) \wedge \\ & ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge (m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow ((r2\_funct\_2 X0 X1 X2 \\ & X3) \Rightarrow (r2\_funct\_2 X0 X1 X3 X2)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((v1\_funct\_1 X2) \wedge \\ & ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge (m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow ((r2\_funct\_2 X0 X1 X2 \\ & X3) \Leftrightarrow (X2 = X3)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge (l2\_struct\_0 X1)) \Rightarrow \\ & (\exists X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly \\ & X0) (u1\_struct\_0 X1)))) \wedge ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 X2 (k15\_pre\_poly \\ & X0)) \wedge ((v5\_relat\_1 X2 (u1\_struct\_0 X1)) \wedge ((v1\_funct\_1 X2) \wedge ((\neg \\ & v1\_xboole\_0 X2) \wedge ((v1\_partfun1 X2 (k15\_pre\_poly X0)) \wedge ((v1\_funct\_2 \\ & X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (v1\_polynom1 X2 (k15\_pre\_poly \\ & X0) X1)))))))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \exists X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1))) \wedge ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 X2 X0) \wedge ( \\ & v5\_relat\_1 X2 X1) \wedge ((v1\_funct\_1 X2) \wedge (v1\_funct\_2 X2 X0 X1)))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge (((\neg v2\_struct\_0 \\ & X1) \wedge (l2\_algstr\_0 X1)) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 (u1\_struct\_0 \\ & X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 (u1\_struct\_0 \\ & X1)))))))))) \Rightarrow ((v1\_funct\_1 (k5\_vfunct\_1 X0 X1 X2)) \wedge (v1\_partfun1 \\ & (k5\_vfunct\_1 X0 X1 X2) X0)) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0. (l6\_algstr\_0 X0) \Rightarrow ((l2\_algstr\_0 X0) \wedge (l5\_algstr\_0 X0)) \quad (10)$$

Assume the following.

$$\forall X0. (l2\_struct\_0 X0) \Rightarrow (l1\_struct\_0 X0) \quad (11)$$

Assume the following.

$$\forall X0. (l2\_algstr\_0 X0) \Rightarrow ((l2\_struct\_0 X0) \wedge (l1\_algstr\_0 X0)) \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge (l2\_struct\_0 X1)) \Rightarrow \\ & ((v1\_funct\_1 (k7\_polynom1 X0 X1)) \wedge ((v1\_funct\_2 (k7\_polynom1 \\ & X0 X1) (k15\_pre\_poly X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 (k7\_polynom1 \\ & X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 \\ & X1)))))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v2\_struct\_0 \\
& X1)\wedge((v13\_algstr\_0 X1)\wedge((v3\_rlvect\_1 X1)\wedge((v4\_rlvect\_1 X1)\wedge \\
& (l2\_algstr\_0 X1))))\wedge(((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 (k15\_pre\_poly \\
& X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k15\_pre\_poly X0) (u1\_struct\_0 X1))))\wedge((v1\_funct\_1 X3)\wedge(( \\
& v1\_funct\_2 X3 (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 \\
& X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1))))))\Rightarrow \\
& ((v1\_funct\_1 (k6\_polynom1 X0 X1 X2 X3)\wedge((v1\_funct\_2 (k6\_polynom1 \\
& X0 X1 X2 X3) (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 ( \\
& k6\_polynom1 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly \\
& X0) (u1\_struct\_0 X1))))))
\end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge(((\neg v2\_struct\_0 \\
& X1)\wedge(l2\_algstr\_0 X1))\wedge((v1\_funct\_1 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 X0) (u1\_struct\_0 X1))))))\Rightarrow((v1\_funct\_1 (k5\_vfunct\_1 \\
& X0 X1 X2))\wedge(m1\_subset\_1 (k5\_vfunct\_1 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0) (u1\_struct\_0 X1))))
\end{aligned} \tag{15}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge((v13\_algstr\_0 X1)\wedge \\
& ((v3\_rlvect\_1 X1)\wedge((v4\_rlvect\_1 X1)\wedge(l2\_algstr\_0 X1))))\Rightarrow( \\
& \forall X2.((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 (k15\_pre\_poly X0) \\
& (u1\_struct\_0 X1))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k15\_pre\_poly X0) (u1\_struct\_0 X1))))))\Rightarrow(\forall X3.((v1\_funct\_1 \\
& X3)\wedge((v1\_funct\_2 X3 (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 \\
& X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1))))))\Rightarrow \\
& (k6\_polynom1 X0 X1 X2 X3 = k4\_polynom1 X0 X1 X2 (k5\_vfunct\_1 (k15\_pre\_poly \\
& X0) X1 X3)))
\end{aligned} \tag{16}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge(\neg v1\_xboole\_0 X1))\Rightarrow \\
& (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow \\
& (((v1\_funct\_1 X2)\wedge(v1\_funct\_2 X2 X0 X1))\Rightarrow((v1\_funct\_1 X2)\wedge(( \\
& \neg v1\_xboole\_0 X2)\wedge(v1\_funct\_2 X2 X0 X1))))
\end{aligned} \tag{17}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.(v1\_xboole\_0 X0)\Rightarrow(\forall X2.(m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 X0)))\Rightarrow(v1\_xboole\_0 X2))
\end{aligned} \tag{18}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(l2\_algstr\_0 X0)\Rightarrow(((\neg v2\_struct\_0 X0)\wedge((v13\_algstr\_0 \\
& X0)\wedge((v3\_rlvect\_1 X0)\wedge(v4\_rlvect\_1 X0))))\Rightarrow((\neg v2\_struct\_0 X0)\wedge \\
& ((v1\_algstr\_1 X0)\wedge(v4\_algstr\_1 X0)))
\end{aligned} \tag{19}$$

Assume the following.

$$\forall X0.\forall X1.(v1\_xboole\_0 X0)\Rightarrow(\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v1\_xboole\_0 X2)) \quad (20)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow((v1\_partfun1 X2 X0)\Rightarrow(v1\_funct\_2 X2 X0 X1)) \quad (21)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0)\Rightarrow(v1\_funct\_1 X0) \quad (22)$$

Assume the following.

$$\forall X0.(l1\_struct\_0 X0)\Rightarrow((\neg v7\_struct\_0 X0)\Rightarrow(\neg v2\_struct\_0 X0)) \quad (23)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(v3\_ordinal1 X0)\Rightarrow(\forall X1.((\neg v7\_struct\_0 X1)\wedge \\ & ((v13\_algstr\_0 X1)\wedge((v5\_group\_1 X1)\wedge((v4\_vectsp\_1 X1)\wedge((v5\_vectsp\_1 \\ & X1)\wedge((v2\_rlvect\_1 X1)\wedge((v3\_rlvect\_1 X1)\wedge((v4\_rlvect\_1 X1)\wedge \\ & (l6\_algstr\_0 X1))))))))))\Rightarrow(\forall X2.((v1\_funct\_1 X2)\wedge((v1\_funct\_2 \\ & X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge((v1\_polynom1 X2 (k15\_pre\_poly \\ & X0) X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly \\ & X0) (u1\_struct\_0 X1)))))))\Rightarrow(\forall X3.((v1\_funct\_1 X3)\wedge((v1\_funct\_2 \\ & X3 (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge((v1\_polynom1 X3 (k15\_pre\_poly \\ & X0) X1)\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly \\ & X0) (u1\_struct\_0 X1)))))))\Rightarrow((r2\_funct\_2 (k15\_pre\_poly X0) (u1\_struct\_0 \\ & X1) (k6\_polynom1 X0 X1 X2 X3) (k7\_polynom1 X0 X1))\Rightarrow(r2\_funct\_2 ( \\ & k15\_pre\_poly X0) (u1\_struct\_0 X1) X2 X3)))))) \end{aligned}$$