

t12\_matrix12  
(TMbT8cb1c3i6A2CvUpeY3LHCEQJfdVT7P63)

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Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v6\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v33\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v5\_group\_1 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k4\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $k12\_matrix\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_matrix\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_matrix12 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_matrix\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_matrix\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k4\_matrix\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_matrix\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_matrix\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1 X0) \Rightarrow (\forall X1.(v7\_ordinal1 X1) \Rightarrow (\forall X2. \\
& (v7\_ordinal1 X2) \Rightarrow (\forall X3. ((\neg v2\_struct\_0 X3) \wedge ((\neg v6\_struct\_0 \\
& X3) \wedge ((v13\_algstr\_0 X3) \wedge ((v33\_algstr\_0 X3) \wedge ((v3\_group\_1 X3) \wedge \\
& ((v5\_group\_1 X3) \wedge ((v2\_rlvect\_1 X3) \wedge ((v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 \\
& X3) \wedge ((v4\_vectsp\_1 X3) \wedge ((v5\_vectsp\_1 X3) \wedge (l6\_algstr\_0 X3)))))))))) \Rightarrow \\
& (\forall X4.(m1\_matrix\_1 X4 (u1\_struct\_0 X3) X1 X1) \Rightarrow (((X0 \in k4\_finseq\_1 \\
& (k12\_matrix\_1 X3 X1)) \wedge (X2 \in k4\_finseq\_1 (k12\_matrix\_1 X3 X1))) \Rightarrow \\
& (k4\_matrix\_6 X1 X3 (k1\_matrix12 X1 X1 X3 (k12\_matrix\_1 X3 X1) X0 X2) \\
& X4 = k1\_matrix12 X1 X1 X3 X4 X0 X2))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1 X0) \Rightarrow (\forall X1.(v7\_ordinal1 X1) \Rightarrow (\forall X2. \\
& (v7\_ordinal1 X2) \Rightarrow (\forall X3.(v7\_ordinal1 X3) \Rightarrow (\forall X4.( \\
& (\neg v2\_struct\_0 X4) \wedge ((\neg v6\_struct\_0 X4) \wedge ((v13\_algstr\_0 X4) \wedge (( \\
& v33\_algstr\_0 X4) \wedge ((v3\_group\_1 X4) \wedge ((v5\_group\_1 X4) \wedge ((v2\_rlvect\_1 \\
& X4) \wedge ((v3\_rlvect\_1 X4) \wedge ((v4\_rlvect\_1 X4) \wedge ((v4\_vectsp\_1 X4) \wedge \\
& ((v5\_vectsp\_1 X4) \wedge (l6\_algstr\_0 X4)))))))))) \Rightarrow (\forall X5. \\
& (m1\_matrix\_1 X5 (u1\_struct\_0 X4) X0 X1) \Rightarrow (((X2 \in k4\_finseq\_1 X5) \wedge \\
& (X3 \in k4\_finseq\_1 X5)) \Rightarrow (k1\_matrix12 X0 X1 X4 (k1\_matrix12 X0 X1 X4 \\
& X5 X2 X3) X2 X3 = X5))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.((v7\_ordinal1\ X0)\wedge \\
& (((\neg v2\_struct\_0\ X1)\wedge(\neg v6\_struct\_0\ X1)\wedge(v13\_algstr\_0\ X1)\wedge \\
& ((v33\_algstr\_0\ X1)\wedge(v3\_group\_1\ X1)\wedge(v5\_group\_1\ X1)\wedge(v2\_rlvect\_1 \\
& X1)\wedge(v3\_rlvect\_1\ X1)\wedge(v4\_rlvect\_1\ X1)\wedge(v4\_vectsp\_1\ X1)\wedge \\
& ((v5\_vectsp\_1\ X1)\wedge(l6\_algstr\_0\ X1))))))\wedge(m1\_matrix\_1 \\
& X2\ (u1\_struct\_0\ X1)\ X0\ X0)\wedge(m1\_matrix\_1\ X3\ (u1\_struct\_0\ X1)\ X0\ X0))\Rightarrow \\
& (k4\_matrix\_6\ X0\ X1\ X2\ X3 = k4\_matrix\_3\ X1\ X2\ X3)
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.((v7\_ordinal1\ X0)\wedge \\
& (((\neg v2\_struct\_0\ X1)\wedge(\neg v6\_struct\_0\ X1)\wedge(v13\_algstr\_0\ X1)\wedge \\
& ((v33\_algstr\_0\ X1)\wedge(v3\_group\_1\ X1)\wedge(v5\_group\_1\ X1)\wedge(v2\_rlvect\_1 \\
& X1)\wedge(v3\_rlvect\_1\ X1)\wedge(v4\_rlvect\_1\ X1)\wedge(v4\_vectsp\_1\ X1)\wedge \\
& ((v5\_vectsp\_1\ X1)\wedge(l6\_algstr\_0\ X1))))))\wedge(m1\_matrix\_1 \\
& X2\ (u1\_struct\_0\ X1)\ X0\ X0)\wedge(m1\_matrix\_1\ X3\ (u1\_struct\_0\ X1)\ X0\ X0))\Rightarrow \\
& (m1\_matrix\_1\ (k4\_matrix\_6\ X0\ X1\ X2\ X3)\ (u1\_struct\_0\ X1)\ X0\ X0)
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\
& ((v7\_ordinal1\ X0)\wedge(v7\_ordinal1\ X1)\wedge(((\neg v2\_struct\_0\ X2)\wedge((\neg \\
& v6\_struct\_0\ X2)\wedge(v13\_algstr\_0\ X2)\wedge(v33\_algstr\_0\ X2)\wedge(v3\_group\_1 \\
& X2)\wedge(v5\_group\_1\ X2)\wedge(v2\_rlvect\_1\ X2)\wedge(v3\_rlvect\_1\ X2)\wedge \\
& (v4\_rlvect\_1\ X2)\wedge(v4\_vectsp\_1\ X2)\wedge(v5\_vectsp\_1\ X2)\wedge(l6\_algstr\_0 \\
& X2))))))\wedge(m1\_matrix\_1\ X3\ (u1\_struct\_0\ X2)\ X0\ X1)\wedge(v7\_ordinal1 \\
& X4)\wedge(v7\_ordinal1\ X5))\Rightarrow(m1\_matrix\_1\ (k1\_matrix12\ X0\ X1\ X2 \\
& X3\ X4\ X5)\ (u1\_struct\_0\ X2)\ X0\ X1)
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.(((\neg v2\_struct\_0\ X0)\wedge(l6\_algstr\_0\ X0))\wedge \\
& (v7\_ordinal1\ X1))\Rightarrow(m1\_matrix\_1\ (k12\_matrix\_1\ X0\ X1)\ (u1\_struct\_0 \\
& X0)\ X1\ X1)
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0)\Rightarrow(\forall X1.((\neg v2\_struct\_0\ X1)\wedge \\
& ((\neg v6\_struct\_0\ X1)\wedge(v13\_algstr\_0\ X1)\wedge(v33\_algstr\_0\ X1)\wedge \\
& (v3\_group\_1\ X1)\wedge(v5\_group\_1\ X1)\wedge(v2\_rlvect\_1\ X1)\wedge(v3\_rlvect\_1 \\
& X1)\wedge(v4\_rlvect\_1\ X1)\wedge(v4\_vectsp\_1\ X1)\wedge(v5\_vectsp\_1\ X1)\wedge \\
& (l6\_algstr\_0\ X1))))))\Rightarrow(\forall X2.(m1\_matrix\_1\ X2\ (u1\_struct\_0 \\
& X1)\ X0\ X0)\Rightarrow((v1\_matrix\_6\ X2\ X0\ X1)\Rightarrow(\forall X3.(m1\_matrix\_1\ X3 \\
& (u1\_struct\_0\ X1)\ X0\ X0)\Rightarrow((X3 = k5\_matrix\_6\ X0\ X1\ X2)\Leftrightarrow(r2\_matrix\_6 \\
& X0\ X1\ X3\ X2))))))
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0\ X1) \wedge \\
& ((\neg v6\_struct\_0\ X1) \wedge ((v13\_algstr\_0\ X1) \wedge ((v33\_algstr\_0\ X1) \wedge \\
& (v3\_group\_1\ X1) \wedge ((v5\_group\_1\ X1) \wedge ((v2\_rlvect\_1\ X1) \wedge ((v3\_rlvect\_1 \\
& X1) \wedge ((v4\_rlvect\_1\ X1) \wedge ((v4\_vectsp\_1\ X1) \wedge ((v5\_vectsp\_1\ X1) \wedge \\
& (l6\_algstr\_0\ X1)))))))))) \Rightarrow (\forall X2.(m1\_matrix\_1\ X2\ (u1\_struct\_0 \\
& X1)\ X0\ X0) \Rightarrow ((v1\_matrix\_6\ X2\ X0\ X1) \Leftrightarrow (\exists X3.(m1\_matrix\_1\ X3 \\
& (u1\_struct\_0\ X1)\ X0\ X0) \wedge (r2\_matrix\_6\ X0\ X1\ X2\ X3))))))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0\ X1) \wedge \\
& ((\neg v6\_struct\_0\ X1) \wedge ((v13\_algstr\_0\ X1) \wedge ((v33\_algstr\_0\ X1) \wedge \\
& (v3\_group\_1\ X1) \wedge ((v5\_group\_1\ X1) \wedge ((v2\_rlvect\_1\ X1) \wedge ((v3\_rlvect\_1 \\
& X1) \wedge ((v4\_rlvect\_1\ X1) \wedge ((v4\_vectsp\_1\ X1) \wedge ((v5\_vectsp\_1\ X1) \wedge \\
& (l6\_algstr\_0\ X1)))))))))) \Rightarrow (\forall X2.(m1\_matrix\_1\ X2\ (u1\_struct\_0 \\
& X1)\ X0\ X0) \Rightarrow (\forall X3.(m1\_matrix\_1\ X3\ (u1\_struct\_0\ X1)\ X0\ X0) \Rightarrow \\
& ((r2\_matrix\_6\ X0\ X1\ X2\ X3) \Leftrightarrow ((k4\_matrix\_3\ X1\ X2\ X3 = k4\_matrix\_3\ X1 \\
& X3\ X2) \wedge (k4\_matrix\_3\ X1\ X2\ X3 = k12\_matrix\_1\ X1\ X0))))))
\end{aligned} \tag{9}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.(v7\_ordinal1\ X1) \Rightarrow (\forall X2. \\
& (v7\_ordinal1\ X2) \Rightarrow (\forall X3.((\neg v2\_struct\_0\ X3) \wedge ((\neg v6\_struct\_0 \\
& X3) \wedge ((v13\_algstr\_0\ X3) \wedge ((v33\_algstr\_0\ X3) \wedge ((v3\_group\_1\ X3) \wedge \\
& ((v5\_group\_1\ X3) \wedge ((v2\_rlvect\_1\ X3) \wedge ((v3\_rlvect\_1\ X3) \wedge ((v4\_rlvect\_1 \\
& X3) \wedge ((v4\_vectsp\_1\ X3) \wedge ((v5\_vectsp\_1\ X3) \wedge (l6\_algstr\_0\ X3)))))))))) \Rightarrow \\
& (((X0 \in k4\_finseq\_1\ (k12\_matrix\_1\ X3\ X1)) \wedge (X2 \in k4\_finseq\_1\ (k12\_matrix\_1 \\
& X3\ X1))) \Rightarrow ((v1\_matrix\_6\ (k1\_matrix12\ X1\ X1\ X3\ (k12\_matrix\_1\ X3\ X1) \\
& X0\ X2)\ X1\ X3) \wedge (k5\_matrix\_6\ X1\ X3\ (k1\_matrix12\ X1\ X1\ X3\ (k12\_matrix\_1 \\
& X3\ X1)\ X0\ X2) = k1\_matrix12\ X1\ X1\ X3\ (k12\_matrix\_1\ X3\ X1)\ X0\ X2))))))
\end{aligned}$$